

13 Explain stereochemistry of electrocyclic reaction for 4π system under E/hν condition by FMO method

1 Explain the 1,3-dipolar cycloaddition reaction and chelotropic reactions with mechanism.

2 What is sharpless asymmetric epoxidation?

3 Explain the interconversion of cyclohexane

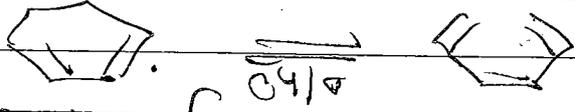
4 Explain 1,3-butadiene under thermal (hν) condition by co-relation diagram method.

5 What are cycloaddition reaction & explain the cycloaddition between the two molecules of ethylene (2π+2π) system.

6 Why on thermal reaction cis-3,4-dimethylcyclobutane gives (2E,4Z)-2,4-hexadiene while trans isomer gives the (2E,4E)-2,4-hexadiene.

7 What are sigmatropic rearrangement & explain 1,3-sigmatropic rearrangement by FMO method.

8 For following transformation, predict whether these transformation are thermally or photochemically allowed.



9 What do you understand by term suprafacial & antarafacial overlapping & explain allowed of 2π+2π system is photochemically allowed process.

10 What are sigmatropic rearrangement & explain cope of 1,3-sigmatropic rearrangement with mechanism.

11 Write the help of FMO & explain 2+2 cycloaddition is photochemically allowed.

12 With the help of correlation diagram, discuss 'real' is a thermally allowed process.

13 Explain stereochemistry of electrocyclic reaction for 4π system under E/hν condition by FMO method.

Pericyclic Reaction

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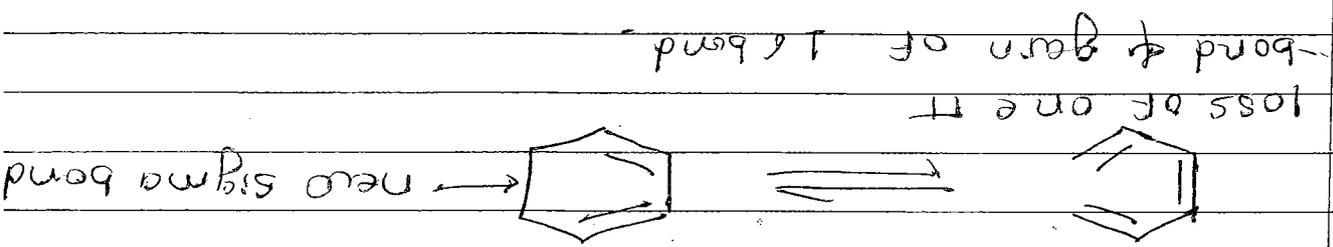
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Pericyclic reactions are defined as the reaction that occur by a concerted cyclic shift of electrons. These reactions are concerted means reactant bonds are broken and product bonds are formed at the same time without intermediates.

Pericyclic reactions involve a cyclic shift of electrons. The word pericyclic means around the circle. Pericyclic reactions are characterised by a cyclic transition state involving the π -bonds. The reaction are unaffected by solvent or catalyst.

Pericyclic reactions are induced by thermally (by heating) or photochemically (by irradiation). Pericyclic reactions are stereospecific.

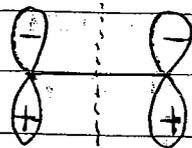


Symmetry in molecular orbital :

A π -molecular orbital possesses either mirror plane symmetry or centre of symmetry. Both symmetries are not present together in a give molecular orbital.

Some molecular orbitals have the symmetry about the mirror plane (m) which bisects the molecular orbitals and is perpendicular to the

Plane of the molecule.



→ mirror plane \perp to the plane of the molecule

Both orbitals are mirror images to each other. hence in this MO there is plane of symmetry, abbreviated as $m(s)$.



both orbitals are not mirror images to each other. thus in this MO there is mirror plane. asymmetry, abbreviated as $m(a)$

Co symmetry s

The centre of symmetry is a point in the molecular axis from which if lines are drawn on one side and extended an equal distance on the other side, will meet the same phases of orbitals.



Centre of molecular axis

both orbitals are symmetrical with respect to center of the molecular axis. thus

in this MO there is centre of symmetry. abbreviated as (σ_{CS}) .

construction of π molecular orbitals \rightarrow

1) The number of molecular orbitals is always equal to the number of atomic p-orbitals. A π -electron system derived from the interaction of number of p-orbitals.

2) Half of the molecular orbitals are bonding molecular orbitals and remaining half are antibonding molecular orbitals (ABMO's). Number of p-orbitals equal to number of carbon atom upto conjugation.

3) The plus and minus signs used in drawing these orbitals indicate the phase of the wave function.

5) π molecular orbitals abbreviated as $\psi_1, \psi_2, \psi_3, \dots, \psi_n$.

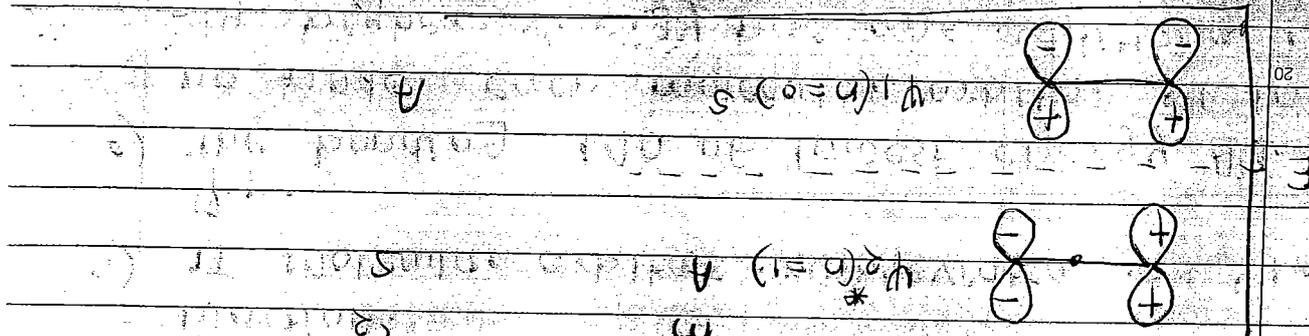
6) The bonding MO of lowest energy ψ_1 has no node. Each molecular orbital of increasing higher energy has one additional node. Node as the position where lobes changes its sign.

1) Frontier orbitals of ethylene:

π -molecular orbitals of ethylene from the two p-atomic orbitals of the two carbons.

Let us examine symmetry properties of π -orbitals of ethylene in ground state and also in the excited state. The ground state π -orbital is symmetric (s) with the mirror plane (m) & asymmetric (a) with the vertical axis.

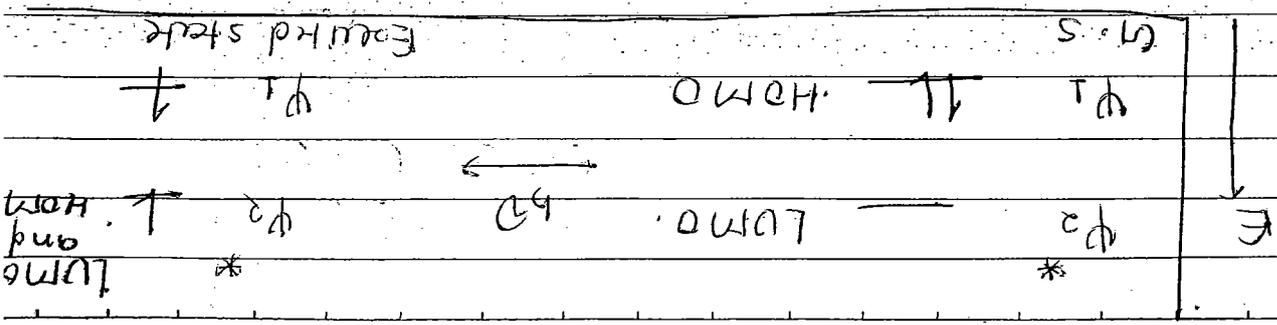
on the other hand, the antibonding orbital (π^*) of ethylene is asymmetric with the vertical axis and symmetric with the vertical axis. The following diagram shows the symmetry properties of molecular orbital of ethylene.



When ethylene absorbs a photon of proper wavelength the π is promoted from the ground state to excited state.

The orbital π^* becomes HOMO and π becomes LUMO of the ground state.

The species with the promoted π^* is excited state. The orbital π becomes HOMO as well as LUMO of the excited state.



2) 1,3-butadiene \rightarrow

In 1,3-butadiene there are four p-orbitals in the molecule and their combination gives us an approximate set of four molecular π -orbitals having different energies.

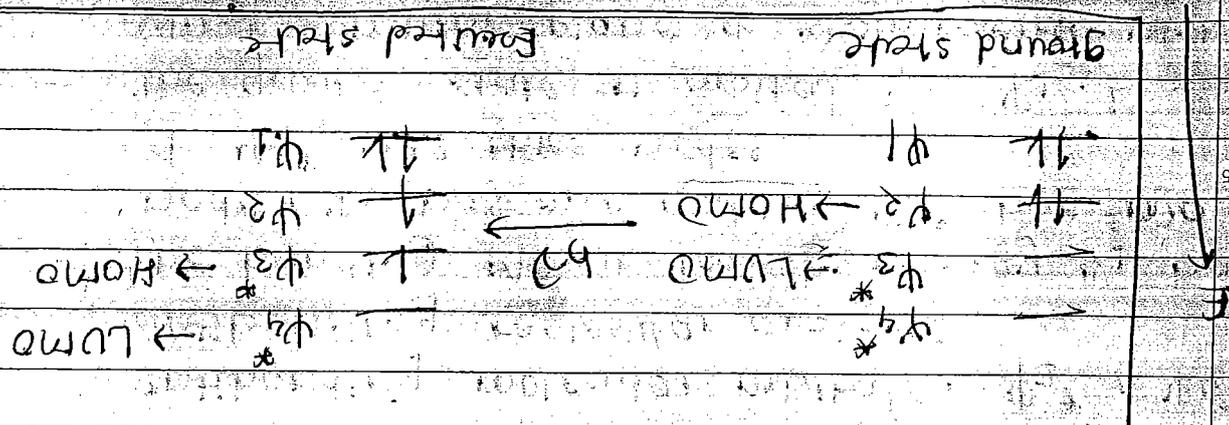
In 1,3-butadiene, four p-orbitals are used in the formation of the π MO's, thus four π MO's results, which we shall abbreviate as $\psi_1, \psi_2, \psi_3, \psi_4$.

Half of the molecular orbitals have lower energy. These are called bonding molecular orbitals, ψ_1 & ψ_2 are bonding MO's.

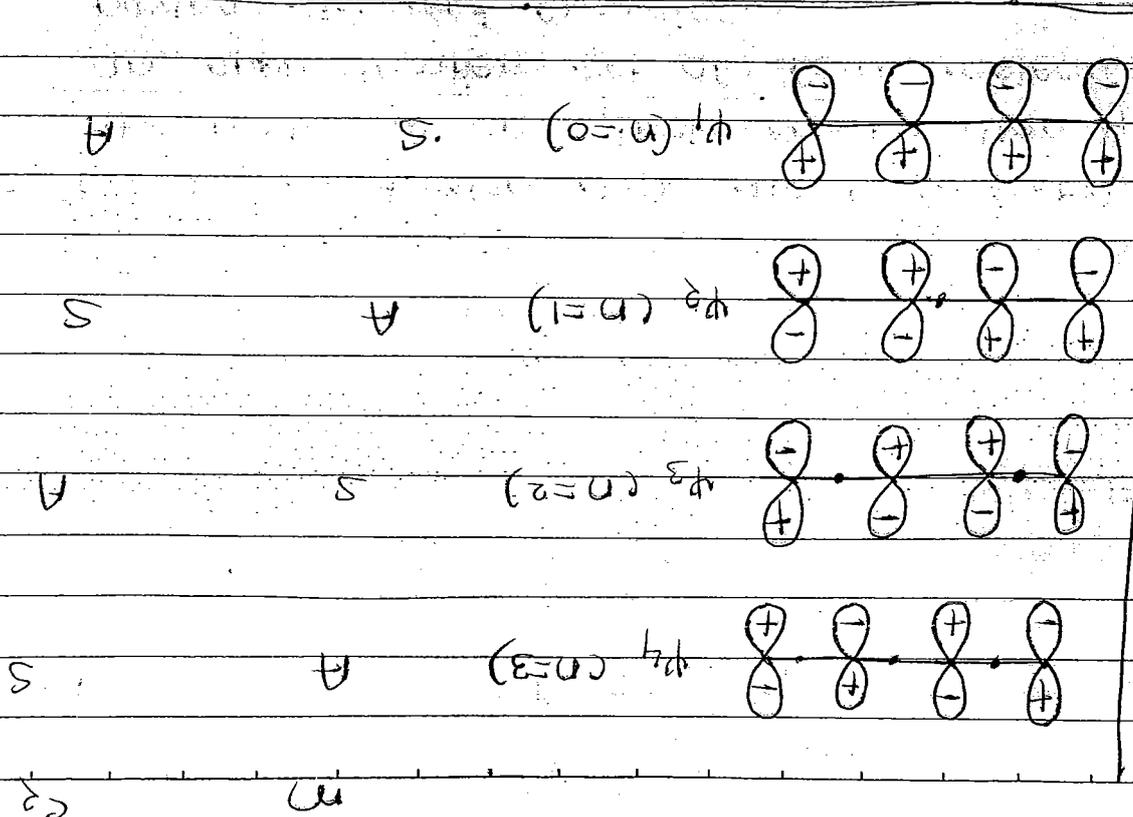
The other half have energy. These are called antibonding molecular orbitals, ψ_3^* & ψ_4^* are antibonding molecular orbitals.

The bonding MO of lowest energy ψ_1 has no node, ψ_2 has one node, ψ_3^* has two nodes & ψ_4^* has three nodes.

The ground state π orbital i.e. ψ_1 is symmetric w.r.t. mirror plane of asymmetric w.r.t. vertical axis. ψ_2 is asymmetric w.r.t. mirror plane and symmetric w.r.t. vertical axis.



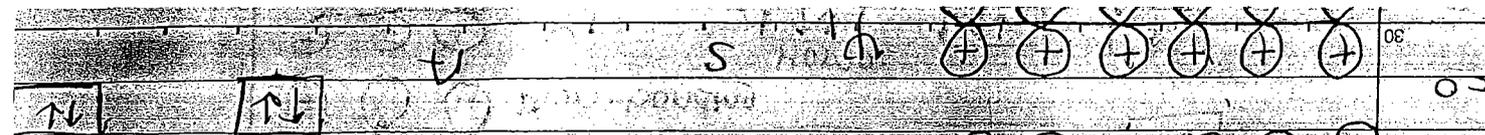
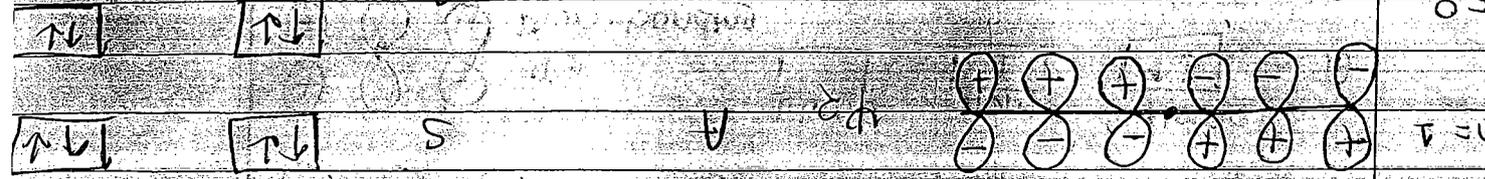
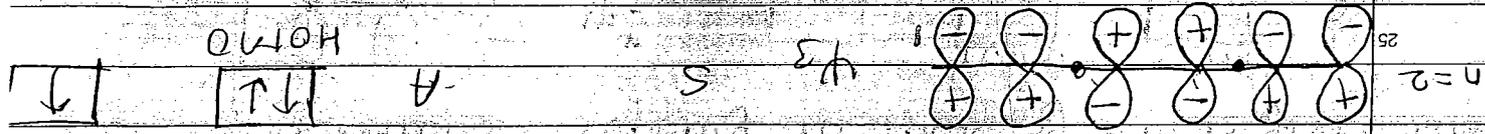
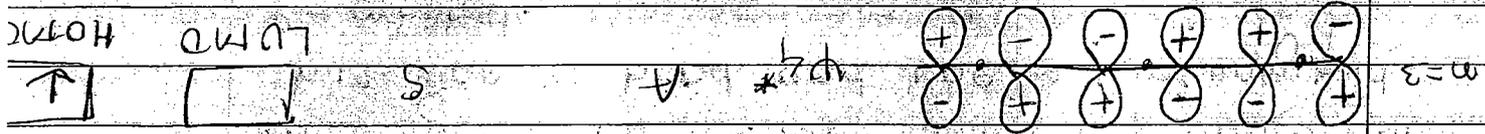
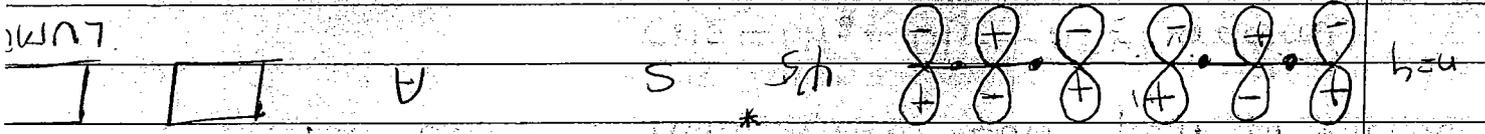
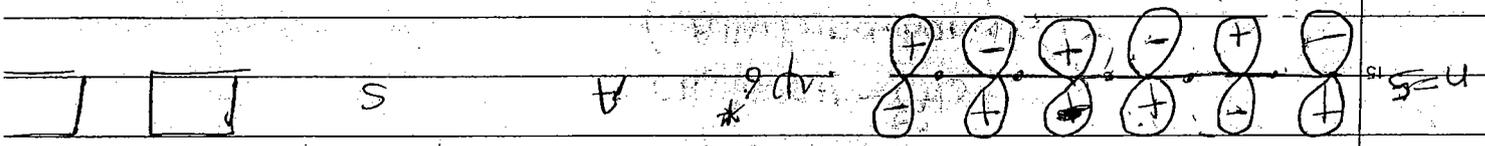
When 1,3-butadiene absorbs a photon of proper wavelength an e^- is promoted from ground state to excited state. ψ_2 is HOMO & ψ_3^* is LUMO. The orbital ψ_3^* becomes HOMO and ψ_4^* becomes LUMO of the excited state.



3 Frontier orbitals of 1,3,5-hexatriene

The six p electrons of hexatriene are occupied in the first three molecular orbitals (ψ_1, ψ_2, ψ_3) while the remaining three higher energy molecular orbitals (ψ_4, ψ_5, ψ_6) remain unoccupied in the ground state.

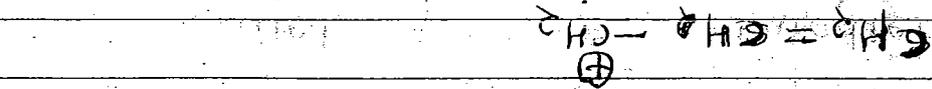
In the ground state of 1,3,5-hexatriene, the orbital ψ_3 become HOMO & ψ_4^* become LUMO. The species with the promoted electron is an excited state of 1,3,5-hexatriene. The orbital ψ_4^* become HOMO and ψ_5^* become LUMO of the excited state.



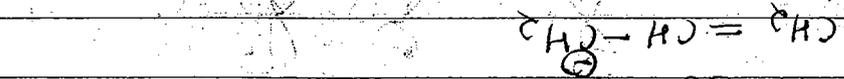
4 Frontier orbitals of allyl systems

The allyl system (cation, anion, or radical) has three carbon and three p-orbitals. hence, three molecular orbitals.

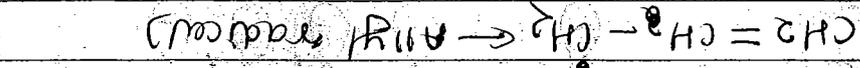
conjugated unbranched ions (cation & anions) and radical have an odd number of carbons. First member of these classes are allyl carbocation, allyl carbanion and allyl free radical.



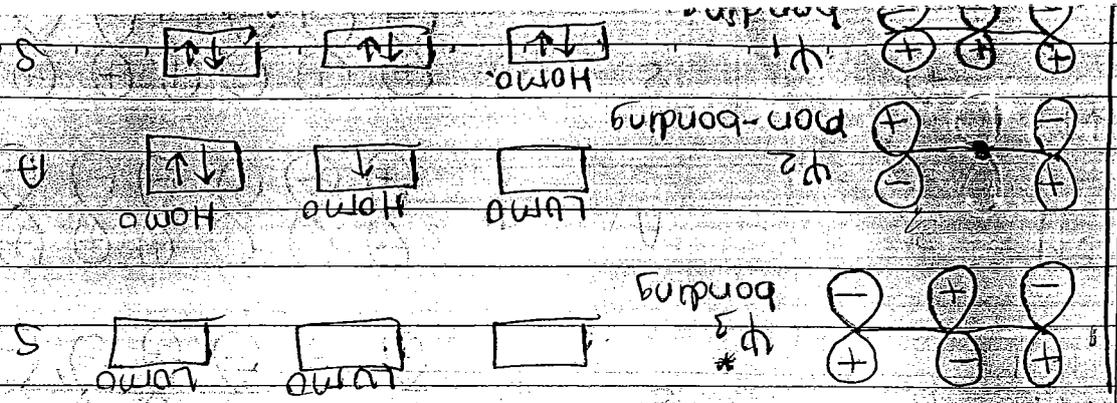
(allyl carbocation)
This system has three isolated p-orbitals and has only one π bond.



(allyl carbanion)
This system has three isolated p-orbitals and has one π bond & one lone pair of electrons.



This system has three isolated p-orbitals and has one π bond and one e⁻ in unhybrid p-orbital.
Electron occupancy in these systems is given below



The MOs of such species follow many of the

same patterns as those of conjugated polyenes

The MOs of allyl are shown in fig.

This figure show too important differences bet

ween these MOs. and those of conjugated

polyenes.

First, one MO is neither bonding molecular orbit

or antibonding molecular orbital but has the

same energy as the isolated p-orbitals. this

MO is called non-bonding molecular orbital.

The non-bonding molecular orbital in the allyl

system is ψ_2 . The remaining MOs are bonding

and antibonding MOs.

Second, in some of the MOs node pass

through carbon atom.

For example, in allyl free radical there is node

on the central carbon atom of ψ_2 .

Notice that cations, anions and free radicals

involving the same π -system have the same

molecular orbitals, because all three species

contain same number of p-orbitals. these

species differ only in the no. of π -electrons

as shown in electron occupancy column.

Theory of pericyclic reactions:

pericyclic reactions are defined as reactions that

occur by concerted cyclic shift of e.

Woodward and Hoffmann symmetry of molecular

orbital that participate in the chemical reaction

determines the course of the reaction. it is

called as conservation of orbital symmetry

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25

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15

10

5

-

-

-

-

(continued)
 If symmetry is conserved during the course of the reaction then reaction will take place and process is known as symmetry allowed process.
 If symmetry is not conserved during the course of the reaction the reaction is known as symmetry-forbidden process.

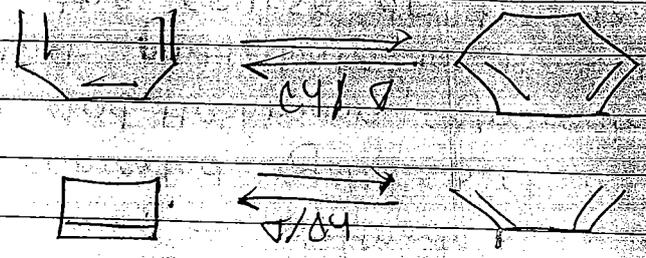
Classification of pericyclic reactions :-
 There are four major types of pericyclic reactions
 ① Electrocyclic reaction ② cycloaddition reaction
 ③ sigmatropic rearrangement ④ intramolecular transfer reaction.

② Pericyclic reactions can be explained by three method.

- a) frontier molecular orbital method (FMO)
- b) perturbation molecular orbital (PMO)
- c) Woodward-Hoffmann correlation diagram.

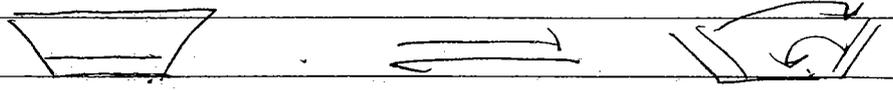
① Electrocyclic Reactions :-

A electrocyclic reaction is the concerted interconversion of conjugated polyene and a cycloalkene or photochemically.



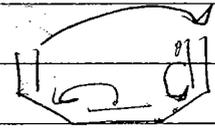
All electrocyclic reactions are reversible reactions, open-chain partner of the reaction is always a conjugated system where as cyclic partner may or may not contain conjugated system.

In electrocyclic reactions either a ring is formed with the generation of a new σ bond and the loss of a π bond (i.e. gain of one σ bond and loss of one π -bond) or ring is broken with the loss of one σ bond and gain of one π bond.



(loss of one σ bond and gain of one π bond)

and gain of one π bond and loss of one σ bond



(loss of one π bond and gain of one σ bond)

and gain of one σ bond and loss of one π bond



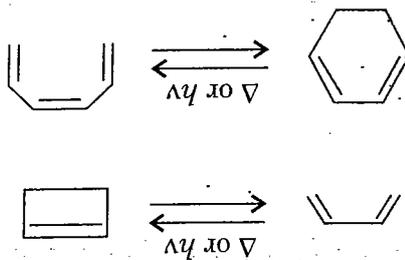
Formation of σ bond & loss of π bond

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5

Electrocyclic Reactions

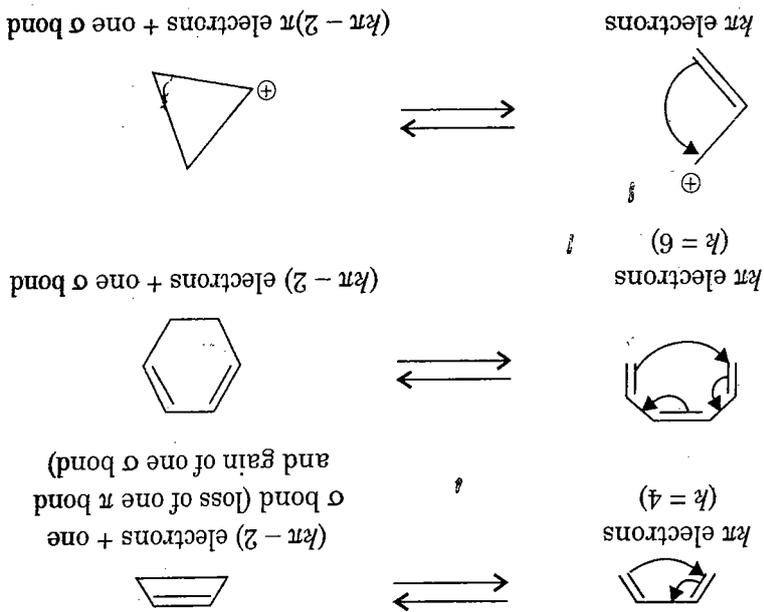
2.1 INTRODUCTION

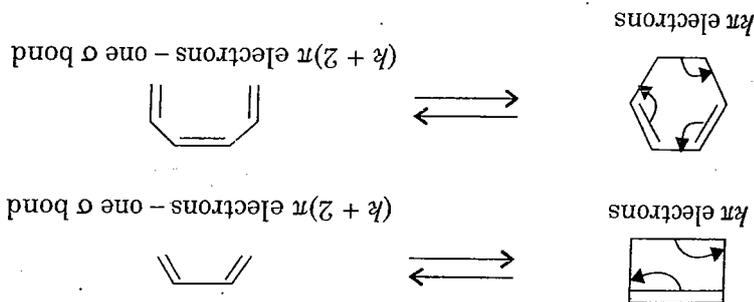
An electrocyclic reaction is the concerted interconversion of a conjugated polyene and a cycloalkene. Electrocyclic reactions are induced either thermally or photochemically.



All electrocyclic reactions are reversible reactions. Open-chain partner of the reaction is always a conjugated system whereas cyclic partner may or may not contain conjugated system.

In electrocyclic reactions either a ring is formed with the generation of a new σ bond and the loss of a π bond (i.e., gain of one σ bond and loss of one π bond) or ring is broken with the loss of one σ bond and gain of one π bond.





Thus electrocyclic reactions can be classified into two categories:

(i) Electrocyclic opening of the ring, and

(ii) Electrocyclic closure of the conjugated system.

In electrocyclic closure of the ring (or ring closing electrocyclic reaction) if the π system of the open-chain partner contains $k\pi$ electrons, the corresponding cyclic partner contains $(k - 2)\pi$ electrons and one additional σ bond. In ring opening electrocyclic reaction if ring partner contains $k\pi$ electrons, the open chain partner will contain $(k + 2)\pi$ electrons with the loss of one σ bond.

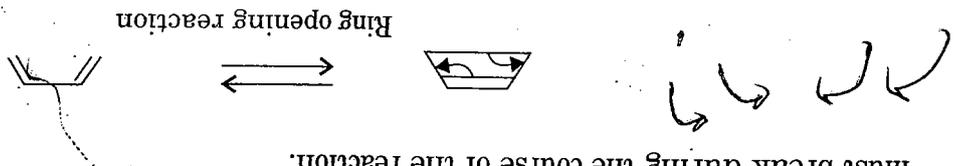
There are two possible stereochemistries for the ring-opening and ring-closing of electrocyclic reactions. They are:

1. Conrotatory process (or motion), and
2. Disrotatory process (motion).

2.2 CONROTATORY AND DISROTATORY MOTIONS IN RING-OPENING REACTIONS

The most common example of the ring opening reaction is the conversion of cyclobutene to 1,3-butadiene.

This conversion can only be possible if a σ (*sigma*) bond between C_3-C_4 of cyclobutene must break during the course of the reaction.



This σ (*sigma*) bond may break in two ways. *First*, the two atomic orbital components of the σ (*sigma*) bond may both rotate in the same direction, clockwise or counter-clockwise. This process is known as **conrotatory motion** (Fig. 2.1).

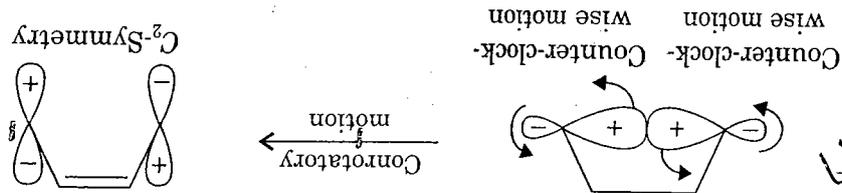
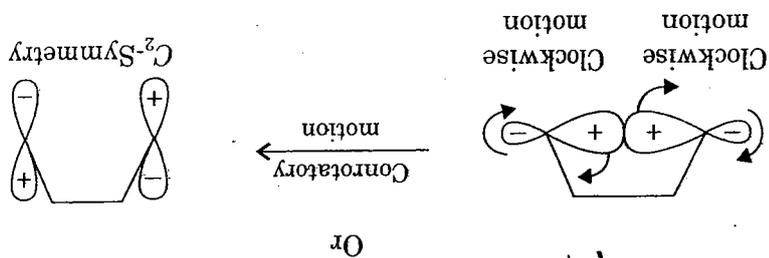


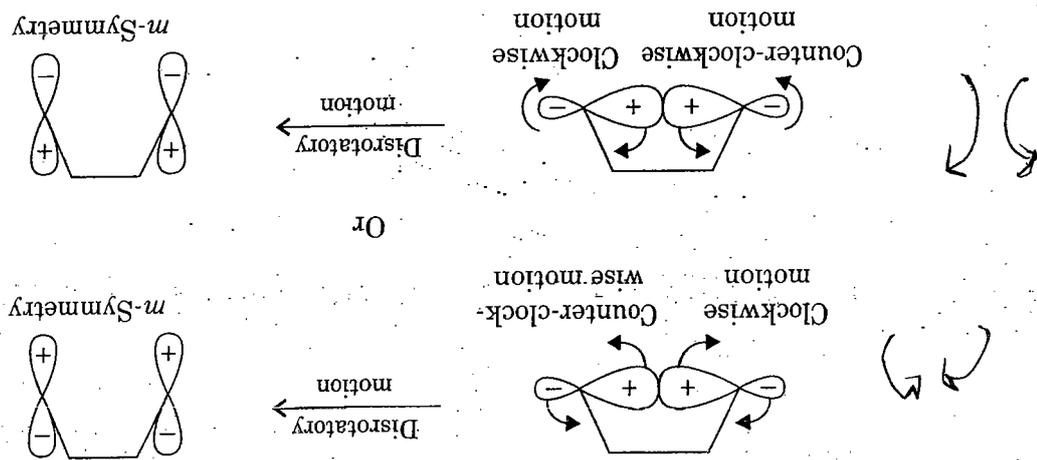
Fig. 2.1 Conrotatory ring-opening



Or

Second, the atomic orbitals may rotate in opposite directions, one clockwise and the other counter-clockwise. This process of ring-opening is known as **disrotatory motion** and the

(Fig. 2.2)



Or

The substituents present on the carbons of the rotating orbitals may also rotate in the same direction of the rotating orbitals. Thus in the conrotatory motion substituents rotate in the same direction (Fig. 2.3) and in disrotatory motion substituents rotate in the opposite directions (Fig. 2.4).

Fig. 2.2 Disrotatory ring-opening

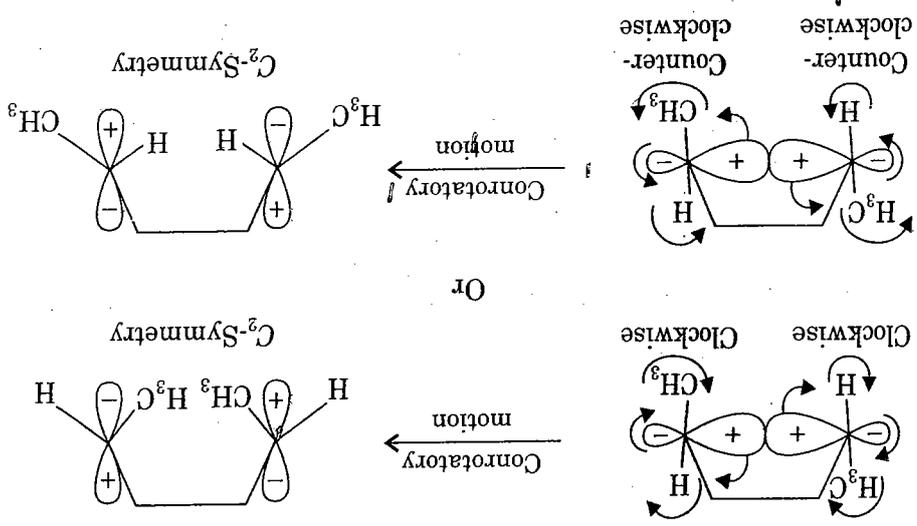


Fig. 2.3 Conrotatory ring-opening, orbitals and groups migrate in the same direction

2.3 CONROTATORY AND DISROTATORY MOTION IN RING-CLOSING REACTIONS

When an electrocyclic reaction takes place, the carbon at each end of the conjugated π system must turn in a concerted fashion so that the p orbitals can overlap (and rehybridised) to form a bond that closes the ring. This turning can also occur in two stereochemically distinct ways. In a conrotatory closure the orbitals and groups of the two carbon atoms turn in the same direction, clockwise or counter-clockwise (Fig. 2.5).

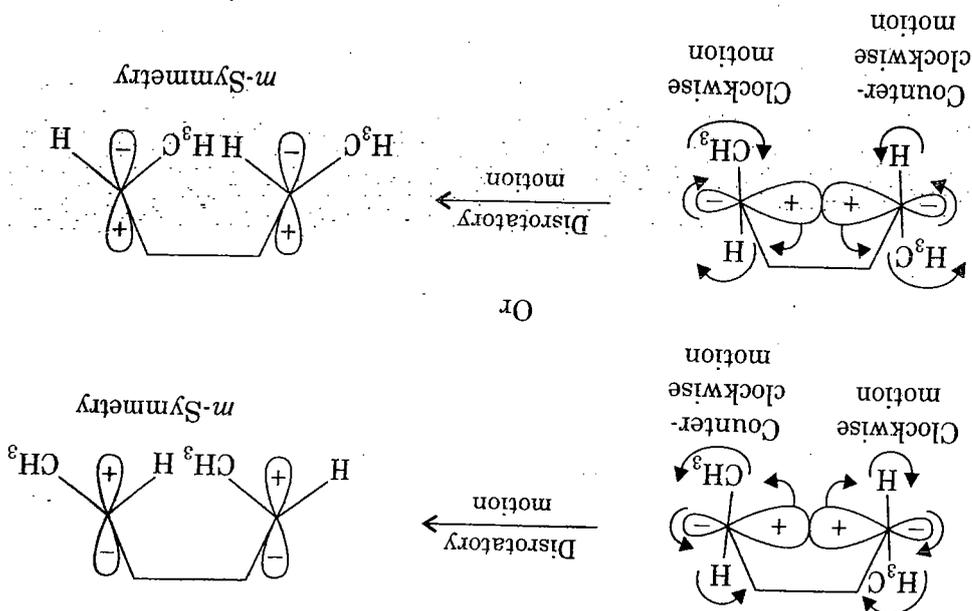
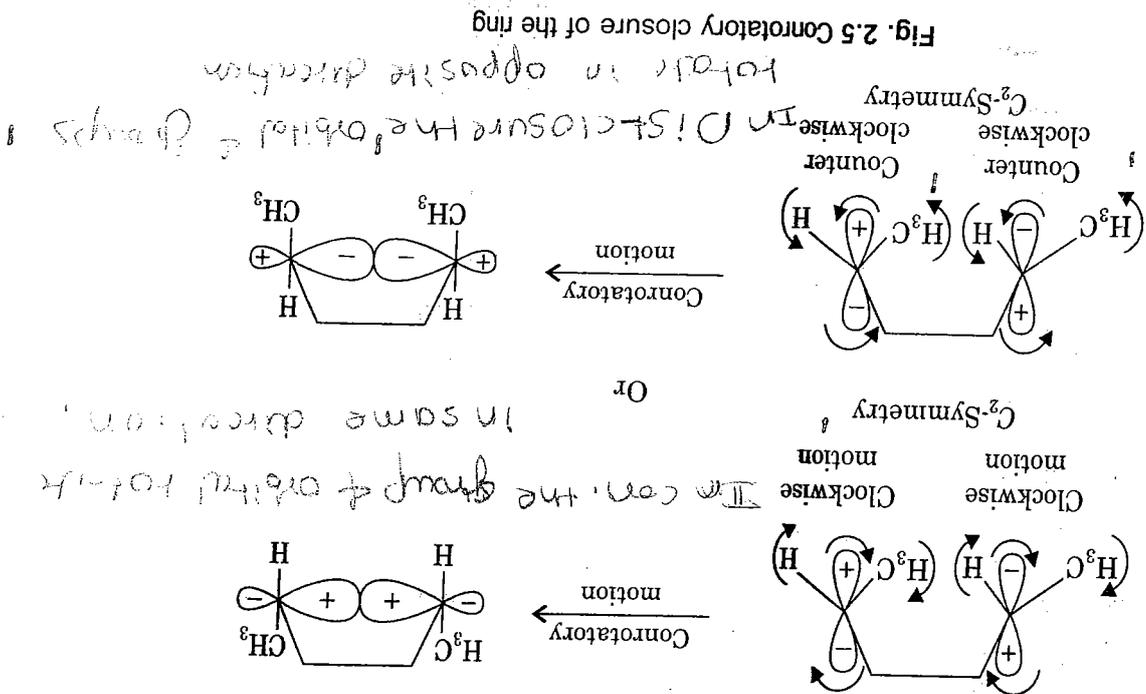


Fig. 2.4 Disrotatory ring-opening, orbitals and groups migrate in the opposite directions



In a disrotatory closure the orbitals and groups of the two carbon atoms turn in the opposite direction, one clockwise and other counter-clockwise (Fig. 2.6).

Fig. 2.5 Conrotatory closure of the ring

DISROTATORY ORBITAL GROUPS
rotate in opposite direction

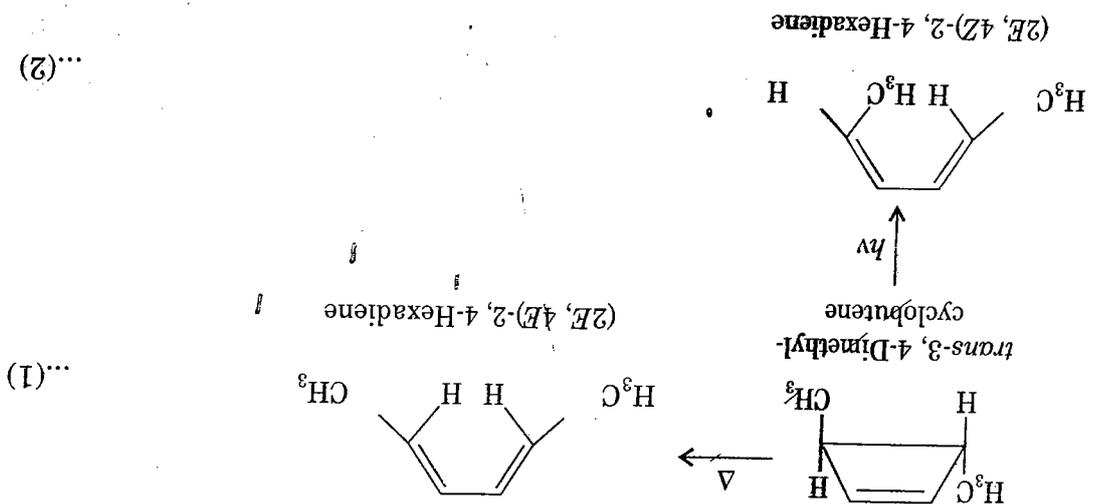
Or, the group & orbital rotate in same direction.

From these examples it is clear that orbitals having *m*-symmetry always give disrotatory motion. (Fig. 2.4 and Fig. 2.6) whereas orbitals having *C₂*-symmetry give conrotatory motion (Fig. 2.3 and Fig. 2.5).

The reason behind this rule can be easily understood by recalling that overlap of wave functions of the same sign is bonding (and symmetry allowed reaction) whereas overlap of wave functions of opposite sign is antibonding (and symmetry forbidden process). Electrocyclic reactions are highly stereospecific. An intriguing feature about electrocyclic reactions is that the stereochemistry of the product is dependent on whether the reaction is thermally induced or photo-induced.

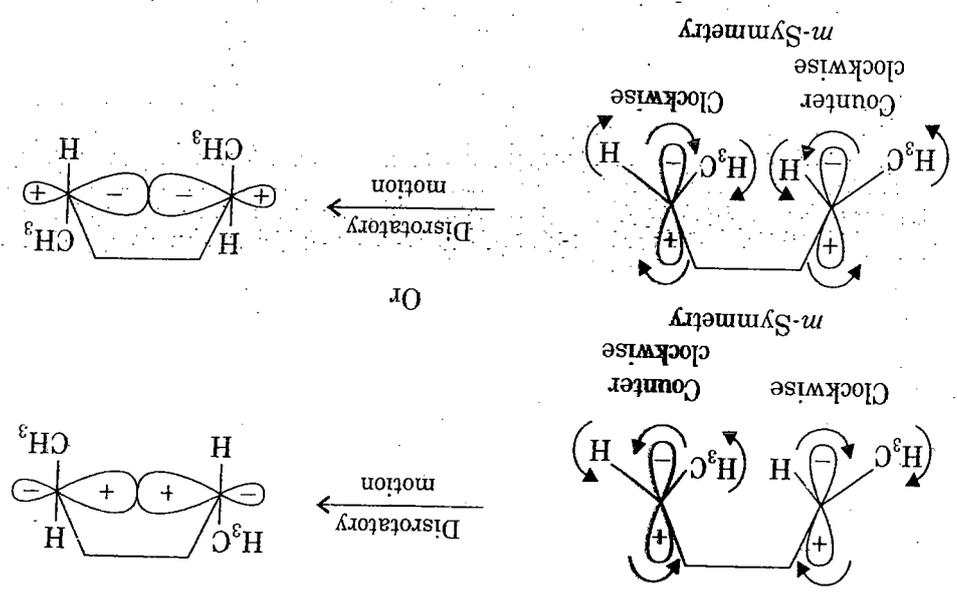
2.3.1 Open Chain Conjugated System having 4n Conjugated Electrons

Let us consider the simplest example in which a cyclobutene derivative opens to a 1, 3-butadiene derivative, i.e., open-chain conjugated system has 4n conjugated π electrons. In thermal condition *trans*-3, 4-dimethylcyclobutene gives (2*E*, 4*E*)-2, 4-hexadiene. Thus, this reaction is completely stereospecific. In the photochemical condition the same substrate gives (2*E*, 4*Z*)-2, 4-hexadiene. In this case too, the reaction is completely stereospecific. Thus the reaction can be performed thermally or photochemically, and under either condition the reaction is completely stereospecific.

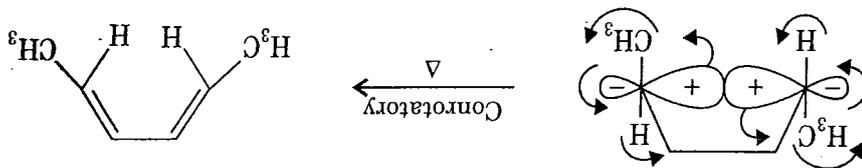


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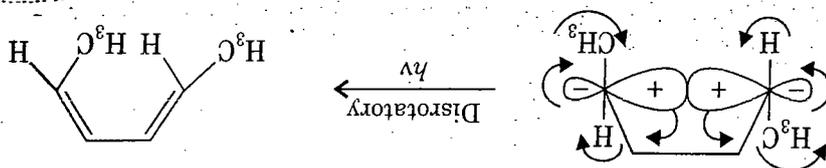
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Stereochemistry of the thermal reaction-1 (of the $4n$ system) can only be explained if process should be conrotatory.



Stereochemistry of the photochemical reaction-2 (of the $4n, \pi$ system) can only be explained if process should be disrotatory.



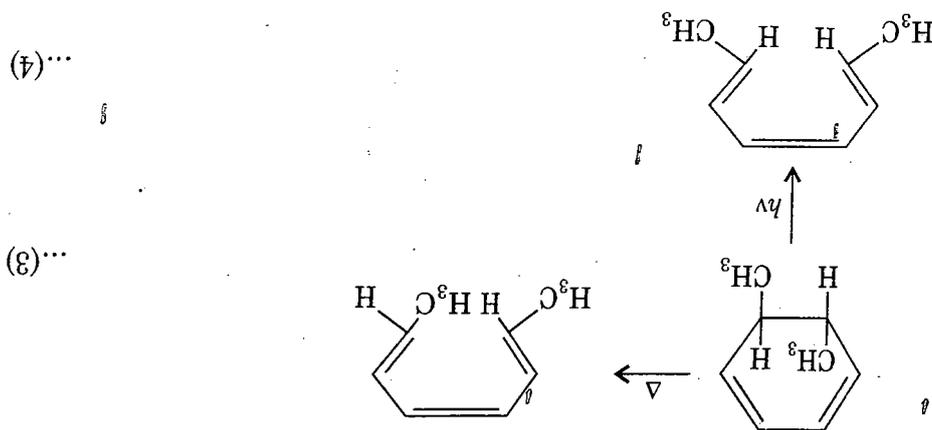
From the above two examples it is clear that thermally induced electrocyclic reaction involving $4n$ conjugated electrons require conrotatory motion and photochemically induced electrocyclic reaction require disrotatory motion.

2.3.2 Open Chain Conjugated System having $(4n + 2)\pi$ Conjugated Electrons

The simplest example of this category is the ring-opening of 1,3-cyclohexadiene into 1,3,5-hexatriene.



In thermal condition 5,6-*trans*-dimethyl-1,3-cyclohexadiene is converted exclusively to (2*E*, 4*Z*, 6*Z*)-2,4,6-octatriene. In the photochemical condition the same substrate is converted exclusively to (2*E*, 4*Z*, 6*E*)-2,4,6-octatriene.



These two conversions are also highly stereospecific. Stereochemistry of these two reactions (i.e., reaction-3 and 4) can only be explained if process is disrotatory in thermal condition and conrotatory in photochemical condition.

On the basis of these experimental results the stereochemistry of electrocyclic reactions can be summarised by noting that thermally induced electrocyclic reactions involving $4n$ electrons require conrotatory motion. Under similar conditions, electrocyclic reactions involving $(4n + 2)\pi$ electrons follow disrotatory motion. Similarly, photo-induced electrocyclic reactions involving $4n\pi$ electrons require disrotatory motion. Under similar conditions, electrocyclic reactions involving $(4n + 2)\pi$ electrons follow conrotatory motion. A summary of the type of motion to be expected from different polyenes under thermal and photochemical conditions is shown in Table 2.1.

Table 2.1

Number of π electrons	Condition (mode of activation)	Motion
$4n$	(i) Thermal (ii) Photochemical	Conrotatory Disrotatory
$4n + 2$	(i) Thermal (ii) Photochemical	Disrotatory Conrotatory

The above experimental results can be explained by the four theories given for pericyclic reactions.

2.4 FRONTIER MOLECULAR ORBITAL (FMO) METHOD

A methodology for quickly predicting whether a given pericyclic reaction is allowed by examining the symmetry of the highest occupied molecular orbital (HOMO) (in case of unimolecular reaction) and, if the reaction is bimolecular, the lowest unoccupied molecular orbital (LUMO) of the second partner.

Thus, electrocyclic reaction is analysed by HOMO of the open chain partner because reaction is unimolecular reaction. The stereochemistry of an electrocyclic process is determined by the symmetry of the highest occupied molecular orbital (HOMO) of the open chain partner, regardless of which way the reaction actually runs. In thermal condition HOMO is always ground state HOMO whereas in photochemical condition HOMO is always first excited state HOMO.

If the highest occupied molecular orbital has m symmetry, the process will be disrotatory. On the other hand, if HOMO has C_2 symmetry then the process will be conrotatory (Table 2.2).

Table 2.2

Symmetry in HOMO	Mode of rotation
m -Symmetry	Disrotatory
C_2 -Symmetry	Conrotatory

For any electrocyclic reaction there are two conrotatory and two disrotatory modes of ring cleavage and ring closure. The two conrotatory modes can give same or different products. Similarly, the two disrotatory modes can also give the same or different products.

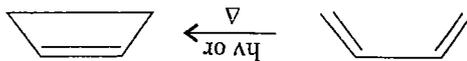
1,3-butadiene by FMO method

Now we are in a position to consider specific examples of the application of the FMO method.

2.4.1 Cyclisation of 4π Systems 1,3-butadiene into cyclobutene under Δ/hν.

1. Electrocyclic ring-closure reaction given by butadiene: 1,3-butadiene is the

first member of the conjugated polyene having 4π electrons.



Thermal-induced cyclisation: When 1,3-butadiene is heated, reaction takes place from the ground state. The electrons that are used for the σ (sigma) bond formation are in the HOMO (ψ_2 in this case). Pertinent p orbitals in ground state HOMO has C_2 -symmetry. For the new σ (sigma) bond to form, rotation must be conrotatory. Disrotatory motion would not place the in-phase lobes together.

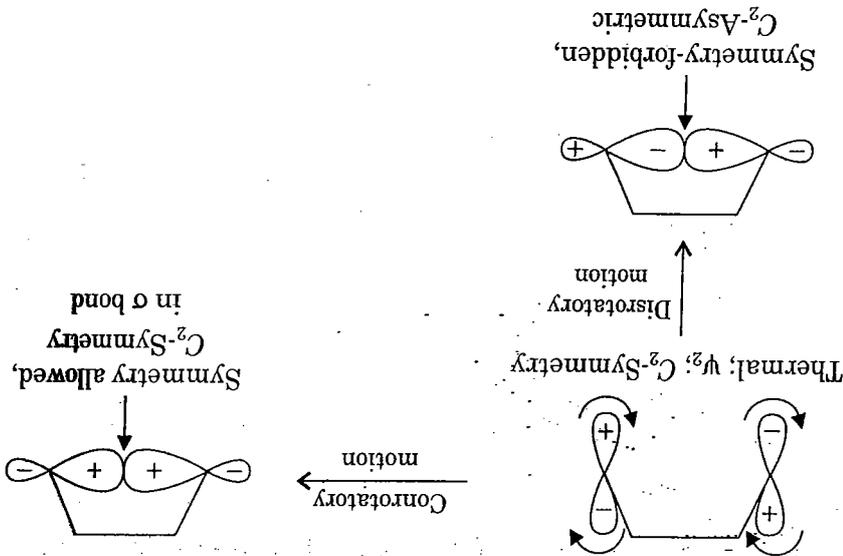
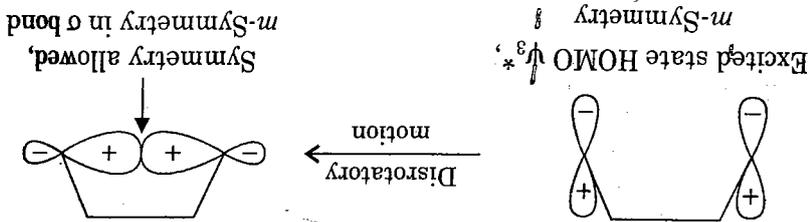


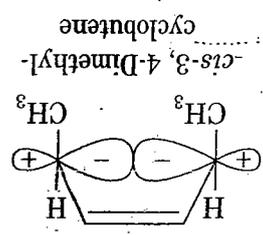
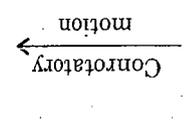
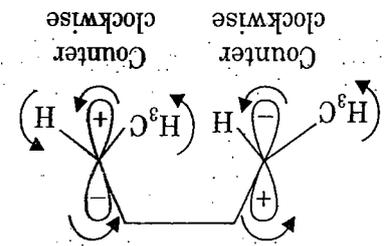
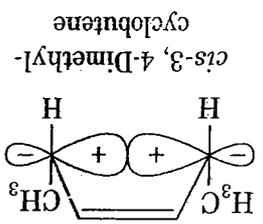
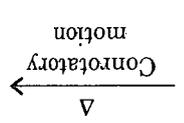
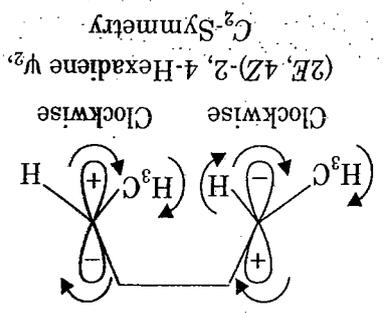
Photo-induced cyclisation: In photo-induced cyclisation, the first excited HOMO of 1,3-butadiene is ψ_3^* which has m symmetry. For the new σ (sigma) bond to form, rotation must be disrotatory.



Let us return to (2E, 4Z)-2,4-hexadiene to see why the *cis*-3,4-dimethylcyclobutene results from the thermal cyclisation and the *trans*-isomer from the photo cyclisation.

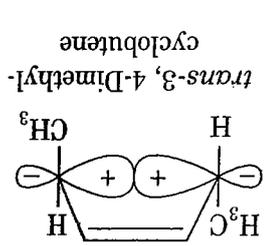
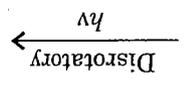
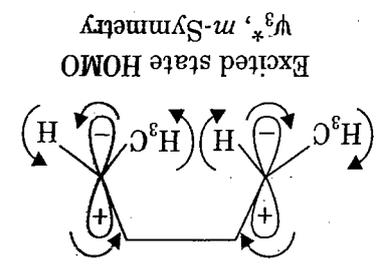
Stereochemistry: In the case of the thermal cyclisation the ground state HOMO is ψ_2 which has C_2 -symmetry. Thus, conrotatory motion is required for σ (sigma) bond formation. Both methyl

groups rotate in the same direction, as a result they end up on the same side of the ring or *cis* is the product.



Or

In the case of photocyclisation the excited state HOMO is ψ_3^* which has *m*-symmetry. Thus, disrotatory motion is required for the σ bond formation. In disrotatory motion, one of the methyl groups, rotates up and the other rotates down. The result is that both methyl groups are *trans* in the product.



Problem 1: Show both conrotatory processes for the thermal electrocyclic conversion of (2E, 4E)-2,4-hexadiene into 3,4-dimethylcyclobutene. Explain why the two processes are equally likely?

Solution: The two different conrotatory motions are as follows:

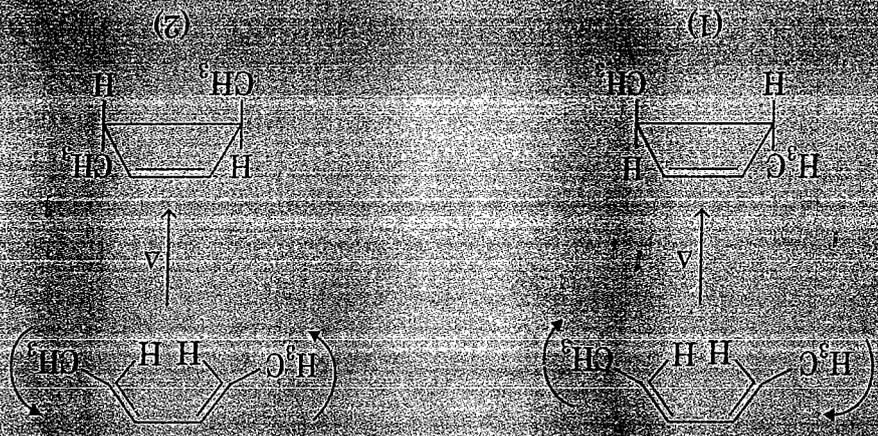
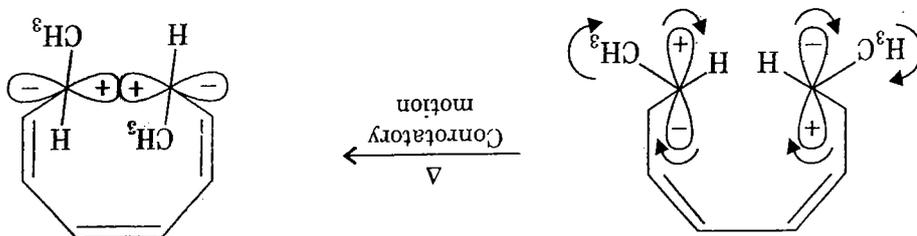
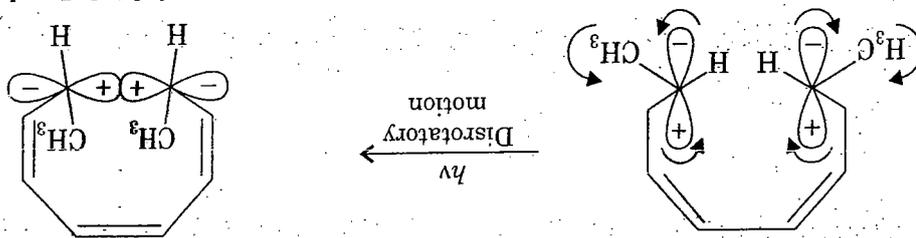


Photo-induced cyclisation: In case of photo-induced cyclisation the excited state HOMO is ψ_5^* which has *m*-symmetry. Thus disrotatory motion is the mode of cyclisation.

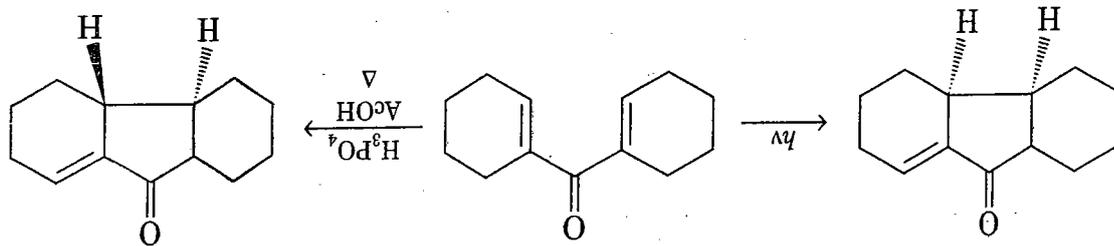
trans-7, 8-Dimethyl-1, 3, 5-cyclooctatriene



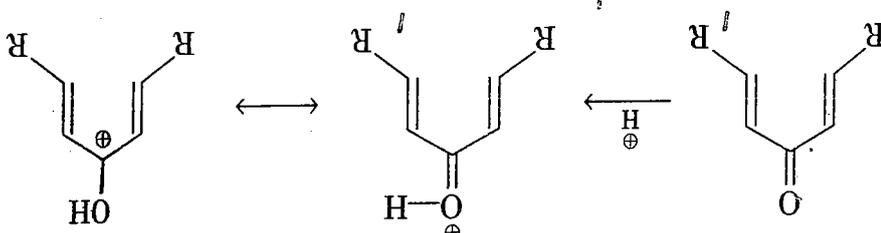
cis-7, 8-Dimethyl-1, 3, 5-cyclooctatriene



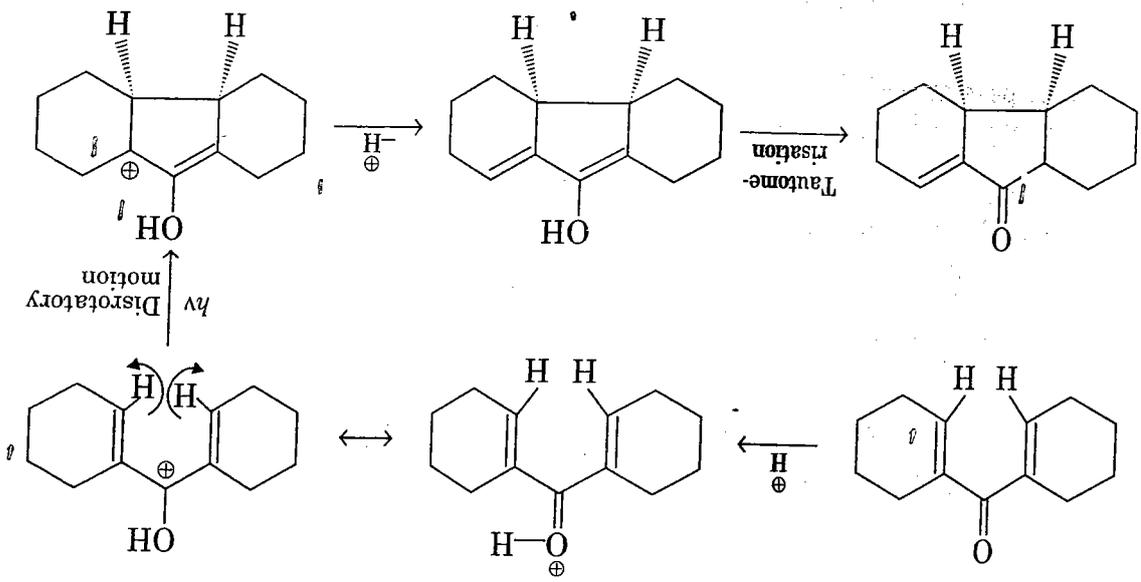
4. Nazarov cyclisation: Nazarov cyclisation is given by 1, 4-pentadiene-3-one and its derivatives. The product of the reaction is cyclopentenone. The reaction is conrotatory electrocyclic ring-closure under thermal condition and disrotatory ring-closure under photochemical conditions.



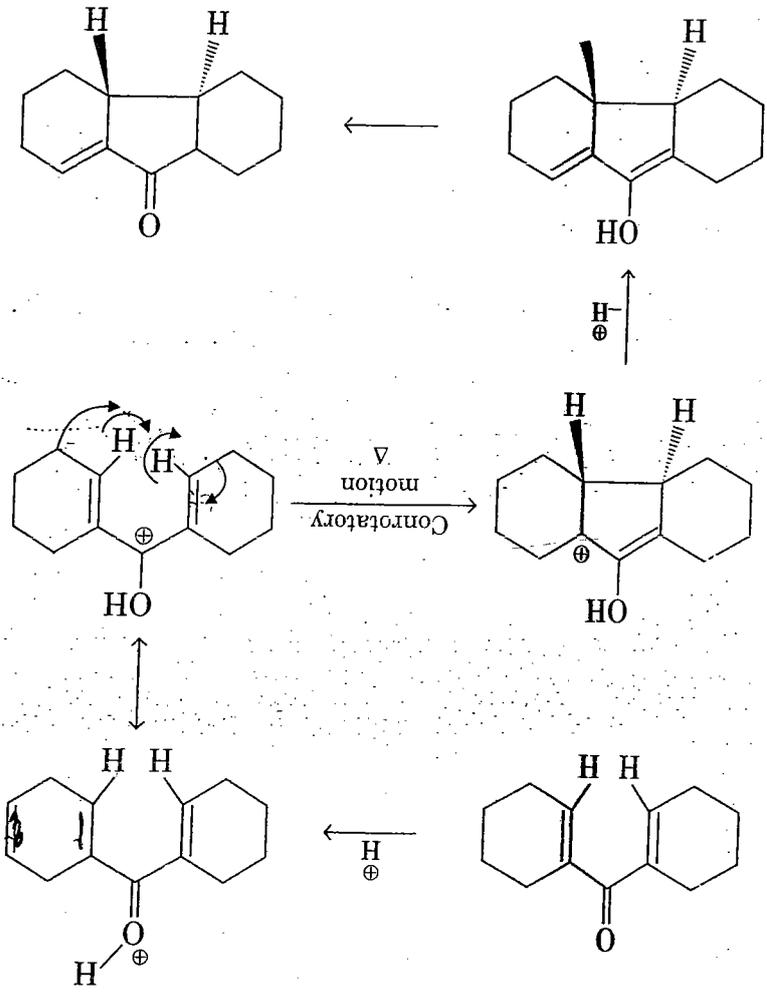
Nazarov cyclisations require acid. Under acidic condition the substrate converts into cation which has 4π conjugated electrons.



Under thermal condition, the motion is conrotatory and under photochemical conditions, the motion is disrotatory because the conjugated system has $(4n)\pi$ conjugated electrons.



The reaction under photochemical conditions



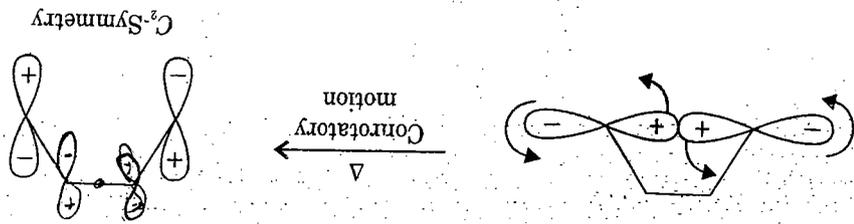
The reaction under thermal condition

Zero/odd node - σ
 even node - π

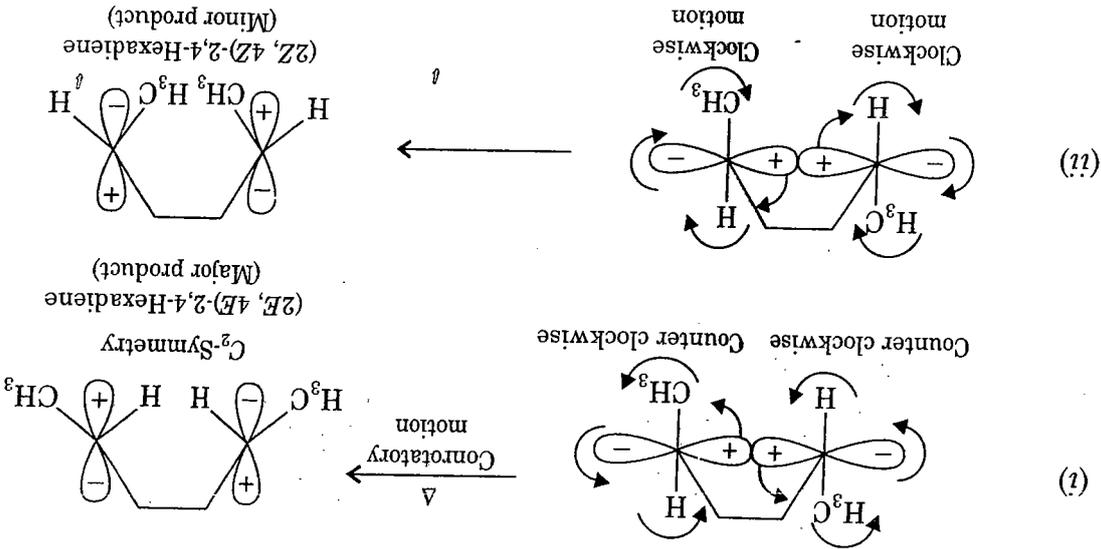
Why on thermal condⁿ cis-3/4-dimethylcyclobutane gives (2E,4E)-2,4-hexadiene while trans gives (2E,4E) 2,4-hexadiene

Conversion of cyclobutene to butadiene

(A) **Thermal-induced ring opening:** In the ring-opening reactions stereochemistry of the product is determined by the symmetry of the ground state HOMO of the open-chain partner. The ground state HOMO of butadiene and its derivative will be ψ_2 , which has C_2 -symmetry. The cyclobutene ring must open in such a fashion that the σ bond orbitals transform into the HOMO of the product having C_2 -symmetry. To get C_2 -symmetry in the product HOMO, motion should be conrotatory in the ring opening of the reaction.
 Even - C_2
 Odd/zero - m

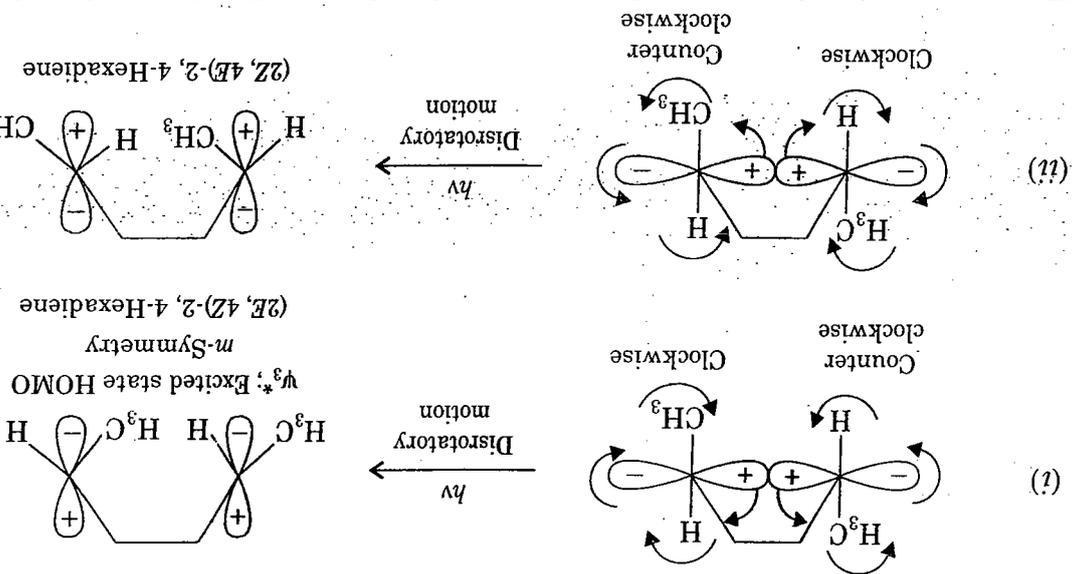


Thus, if the open-chain polyene has $4n\pi$ electrons then the process is always conrotatory in thermal condition whether the reaction is ring-closure or ring opening. Let us take the stereochemistry of the ring opening of *trans*-3,4-dimethylcyclobutene. There is possibility of two modes of conrotatory motion, counter clockwise and clockwise motions.



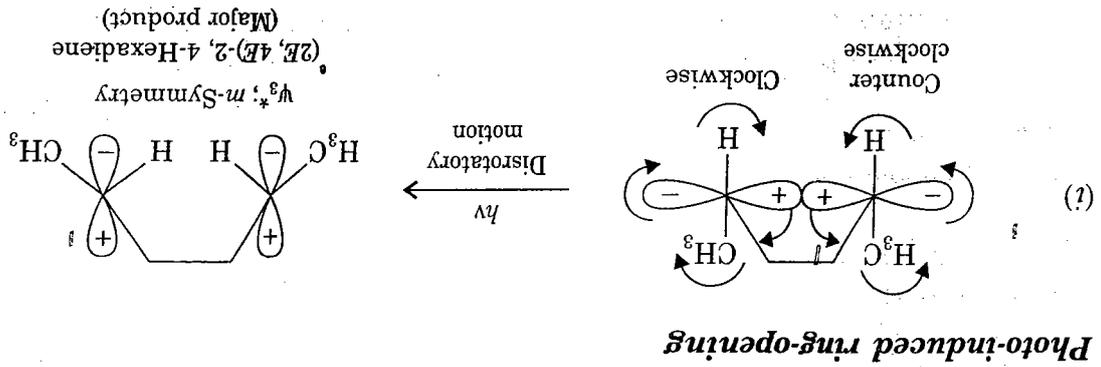
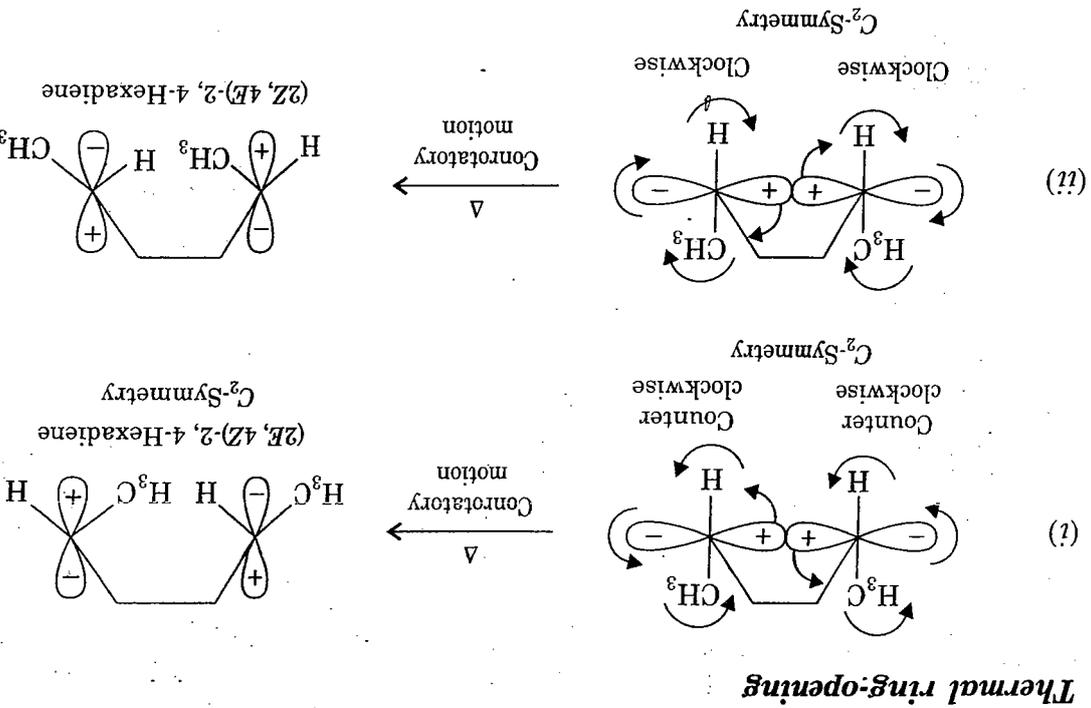
Thus, the thermal process is conrotatory with two products possible in the above case. The conrotation in the second case (clockwise rotation) leads to severe steric interactions between two methyl groups. This interaction is avoided in the first process (rotation is counter clockwise) in which two methyl groups move away from each other, and this is the favoured process.

(B) **Photo-induced ring opening:** The photo state HOMO of the open chain butadiene and its derivative will be ψ_3^* which has *m*-symmetry. Thus, the cyclobutene ring must open in such a fashion that the σ bond orbitals transform into the excited state HOMO of the product having *m*-symmetry. To get *m*-symmetry in excited state HOMO of the product, motion should be disrotatory in the ring-opening of the reaction. There is also possibility of two modes of disrotatory motion.



Thus, photo-induced process is disrotatory with either possible disrotation giving same product.

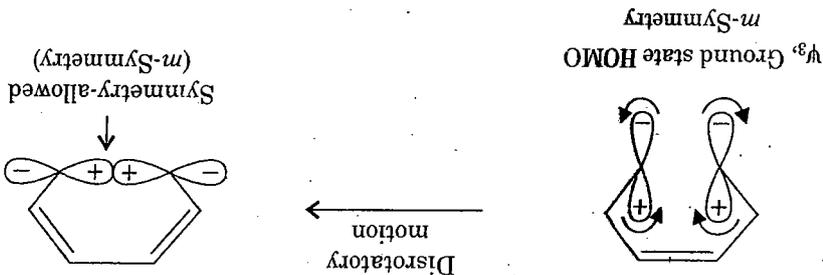
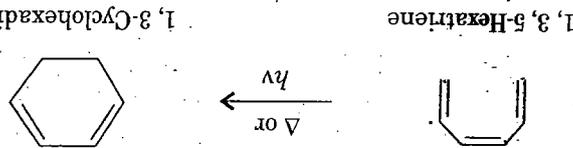
Let us take the conversion of *cis*-3, 4-dimethylcyclobutene into 2, 4-hexadiene.



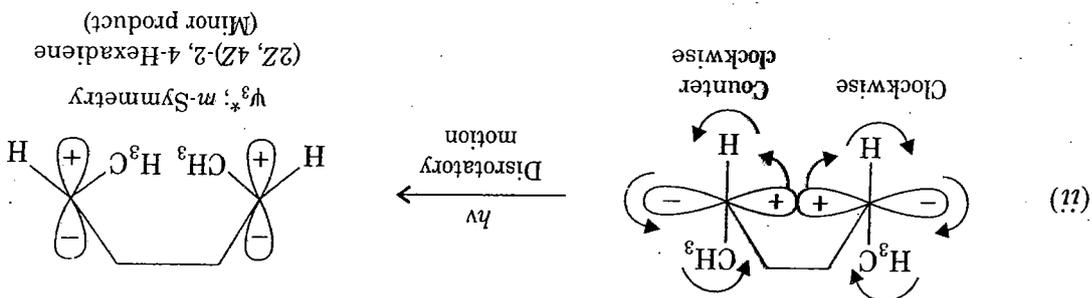
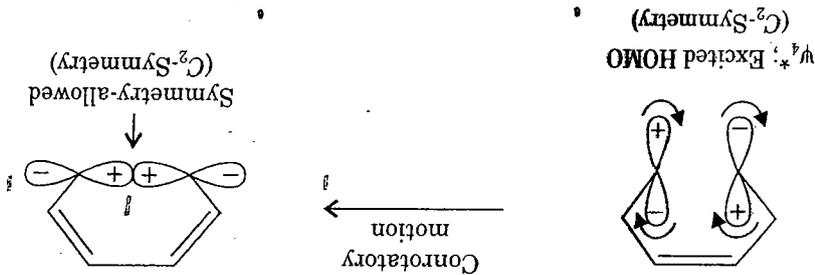
In case of *cis*-3,4-dimethylcyclobutene, the thermal process is conrotatory with either possible conrotation giving the same product. The photochemical process is disrotatory with two possible products.

1,3,5-Hexatriene is the most common example of the polyene having $(4n + 2)\pi$ conjugated electrons.

1. Electrocyclic ring-closure reaction given by 1,3,5-hexatriene



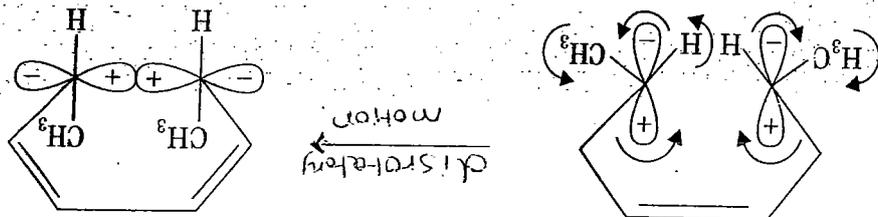
(B) **Photo-induced cyclisation:** When an electron of 1,3,5-hexatriene is promoted by photon absorption, ψ_4^* becomes the HOMO. This excited state HOMO has C_2 -symmetry. Therefore, photo-induced cyclisation proceeds by conrotatory motion.



2.4.3 Cyclisation of $(4n + 2)\pi$ Systems **Interconversion of 1,3,5-hexatriene \rightleftharpoons 1,3-cyclohexadiene under $\Delta/h\nu$ by FMO method**

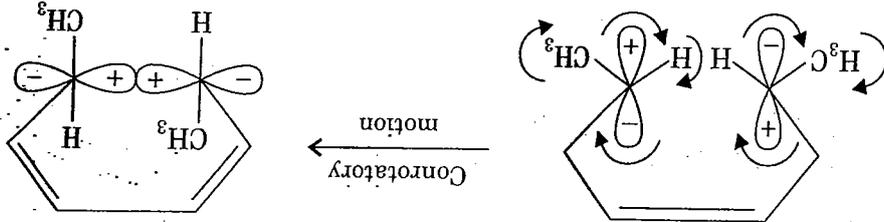
Consider the stereochemistry of the thermal and photo-induced closure of (2*E*, 4*Z*, 6*E*)-2, 4, 6-octatriene to 5, 6-dimethyl-1, 3-cyclohexadiene.

(A) **Thermal-induced cyclisation:** In the case of the thermal induced cyclisation, the ground state HOMO is ψ_3 which has *m*-symmetry. Thus, disrotatory motion is required for sigma bond formation. In disrotatory motion substituents rotate in the opposite directions



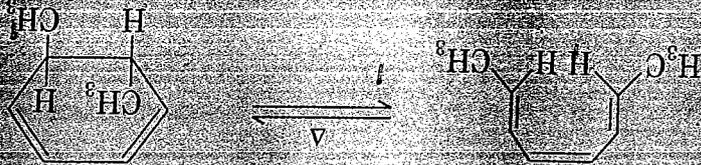
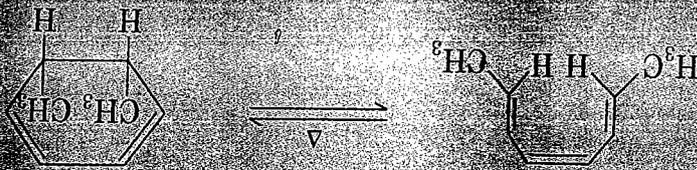
cis-5, 6-Dimethyl-1, 3-cyclohexadiene

(B) **Photo-induced cyclisation:** In case of photo-induced cyclisation, the excited state HOMO is ψ_4^* which has C_2 -symmetry. Therefore, conrotatory motion is required for σ (sigma) bond formation. In conrotatory motion substituents rotate in the same direction.

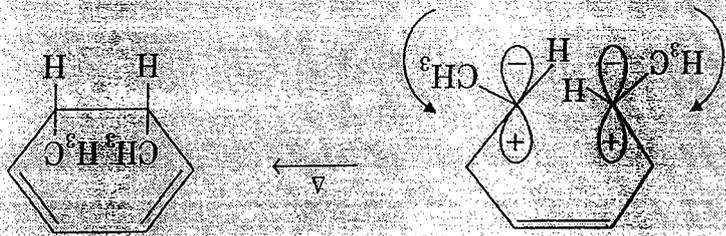


trans-5, 6-Dimethyl-1, 3-cyclohexadiene

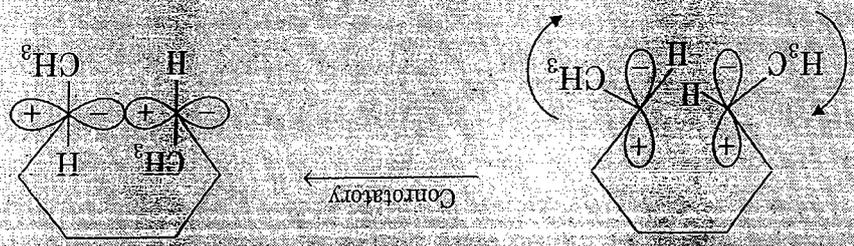
Problem 2: Which one of the following electrocyclic reactions should occur readily by a concerted mechanism?



Solution: Reaction 1 is a disrotatory reaction involving $(4n + 2)\pi$ electrons because this will give *cis* product. This reaction is allowed reaction. This reaction, therefore, can occur readily by a concerted mechanism.



Reaction 2 is a conrotatory reaction involving $(4n + 2)\pi$ electrons because conrotatory motion will give *trans* product. It does not allow because the reaction is symmetry forbidden reaction,

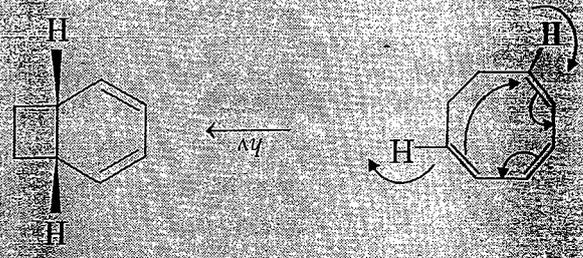


Thus, the reaction does not occur readily.

Problem 3: Complete the following reaction and give stereochemistry of the product.

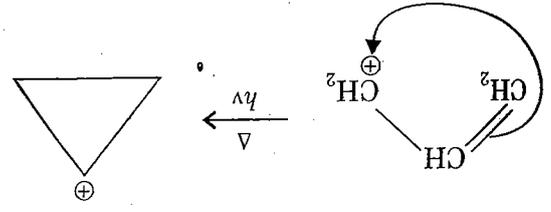
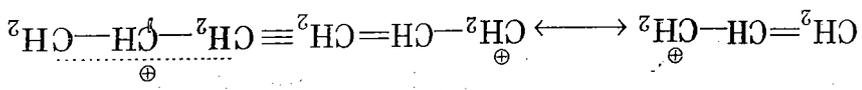


Solution: Reaction is photo-induced reaction. Reactant has $(4n + 2)\pi$ electrons. Its excited HOMO is ψ_4^g which has g_2 symmetry. Thus, motion is conrotatory motion.

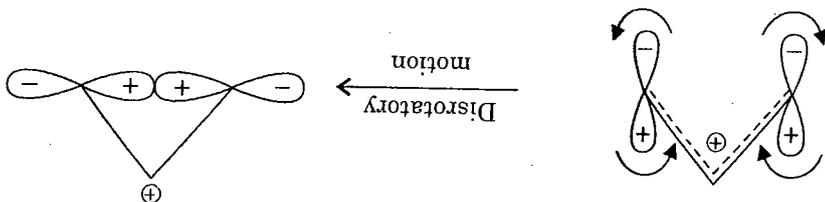


2. Electrocyclic ring-closure reaction given by allyl carbocation

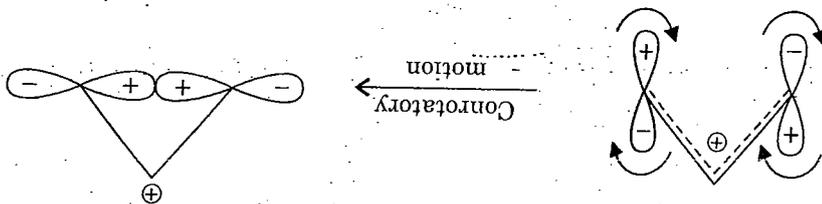
Allyl carbocation contains $(4n + 2)\pi$ conjugated electrons.



(A) **Thermal-induced cyclisation:** HOMO of the allyl carbocation in the ground state is ψ_1 which has *m*-symmetry. Therefore, disrotatory motion is the mode of cyclisation in the thermal condition.



(B) **Photo-induced cyclisation:** HOMO of the allyl carbocation in the excited state is ψ_2 which has C_2 -symmetry. Thus, conrotatory motion is required for σ (*sigma*) bond formation.



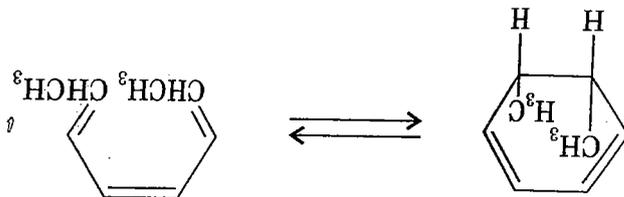
2.4.4 Electrocyclic Ring-opening in which Polyene has $(4n + 2)\pi$ Electrons

1. Conversion of 1, 3-cyclohexadiene to 1, 3, 5-hexatriene system

The most common example of this class is the conversion of 1, 3-cyclohexadiene to 1, 3, 5-hexatriene.



Let us take the example of the ring opening of a *cis*-5, 6-dimethyl-1, 3-cyclohexadiene into 2, 4, 6-octatriene.



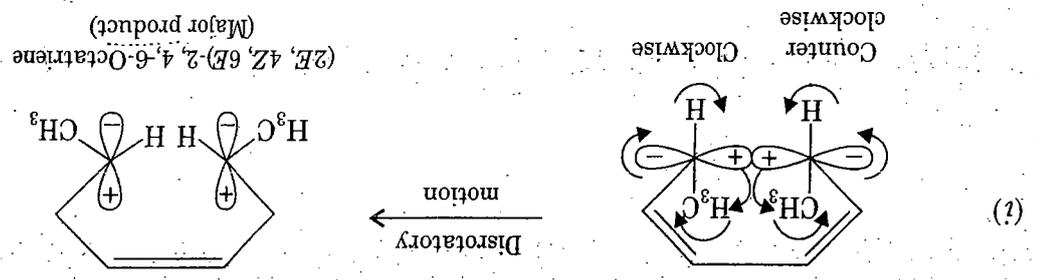
(A) **Thermal ring-opening:** As mentioned earlier that in the ring opening reactions stereochemistry of product is determined by the symmetry of the ground state HOMO of the open-chain partner. The ground state HOMO of the triene will be ψ_3 which has *m*-symmetry. The cyclohexadiene ring therefore, must open in such a fashion that σ bond orbitals transform into the ground state HOMO of the product having *m*-symmetry. To get *m*-symmetry in the HOMO of the product, motion should be disrotatory in the ring opening of the reaction.

The above results can be obtained in short as follows:



Ground state HOMO is ψ_3 which has *m*-symmetry. Therefore, motion is disrotatory.

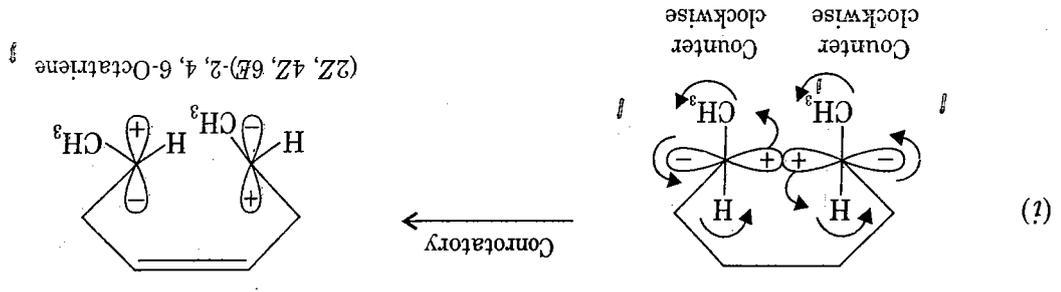
Two modes of disrotatory motions can take place as follows:



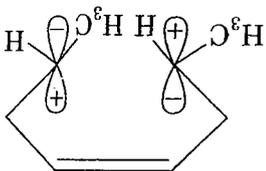
Thus, the thermal process is disrotatory with two possible products, one is major and the other is minor due to the steric reasons.

(B) **Photo-induced ring-opening:** The photo state HOMO of the triene system is ψ_4^* which has C_2 -symmetry. To get C_2 -symmetry in the product, motion should be conrotatory in the ring opening reaction.

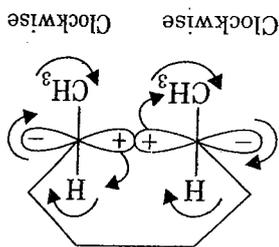
Consider the two modes of conrotatory motions:



(2E, 4Z, 6Z)-2, 4, 6-Octatriene



Conrotatory motion



(?)

In this case either possible conrotation giving the same product.

2. Thermal electrocyclic reaction given by (2E, 4Z, 6Z, 8E)-2, 4, 6, 8-decatriene

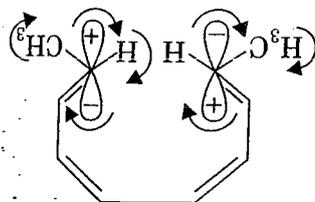
The thermally induced electrocyclic reaction of (2E, 4Z, 6Z, 8E)-2, 4, 6, 8-decatriene provide elegant examples of electrocyclic reactions.

The starting tetraene forms a cyclooctatriene at room temperature. The tetraene is a 4n polye; therefore, conrotatory motion is the expected mode of cyclisation. Indeed the *trans*-cyclooctatriene is heated above room temperature, another electrocyclic ring closure occurs. However, the cyclooctatriene is a (4n + 2)π polye; therefore, this thermally induced electrocyclic reaction proceeds with disrotatory motion, and a *cis* ring junction is formed.

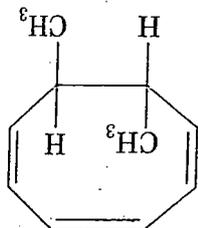
4n, π system, ground state HOMO is

ψ_4 which has C_2 -symmetry.

Thus, motion is conrotatory



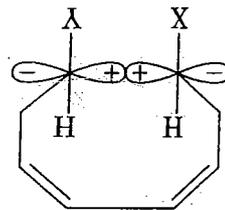
Conrotatory



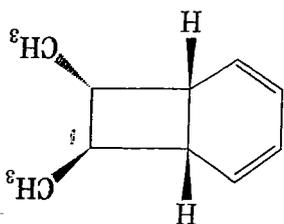
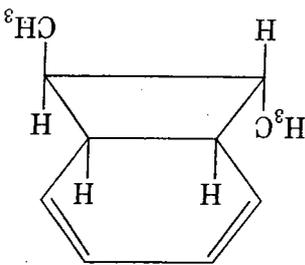
(4n + 2)π system

Ground state HOMO is ψ_3 which has *m*-symmetry.

Therefore, motion will be disrotatory



Disrotatory motion



Correlation diagram : →

The diagram that shows the similarity in energy and symmetry between relevant reactant and product orbitals is called orbital correlation diagram or simply correlation diagram. This method can be used for any pericyclic reaction, but is usually utilised only for electrocyclic reactions.

Correlation diagram is based on the fundamental rule of the conservation of orbital symmetry as proposed by Woodward & Hoffmann.

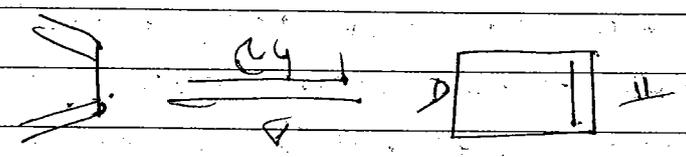
According to this rule, orbital symmetry must be conserved (maintain) throughout the course of reaction in concerted reaction.

This means that a symmetric orbital in the starting material must transform into a symmetric orbital in the product & asymmetric orbital must transform into an asymmetric orbital.

The orbitals that correlate are connected by lines, there keeping that there is correlation between orbitals of same symmetry having minimum energy difference. The diagram is constructed as follows.

In separate columns, orbitals of reactant & product are listed in their order of relative energies, each orbital is classified on the basis of the symmetry elements retained at all points along the reaction coordinate.

Transformation of cyclobutene to 1,3-butadiene in this interconversion, ring opening (or ring closing) may be concerted or distorting. The orbitals that undergo such changes in cyclobutene are σ & π , the highest antibonding orbitals. σ^* & π^* these orbitals pass on to the four π molecular orbitals of butadiene viz. $\psi_1, \psi_2, \psi_3^*, \psi_4^*$. For correlation diagram all these orbitals are listed in order of increasing energy along with their mirror plane (m) & (s) symmetries.



Correlation Diagram of the Electrocyclic reaction in which polyene has $4n+2$ electrons.

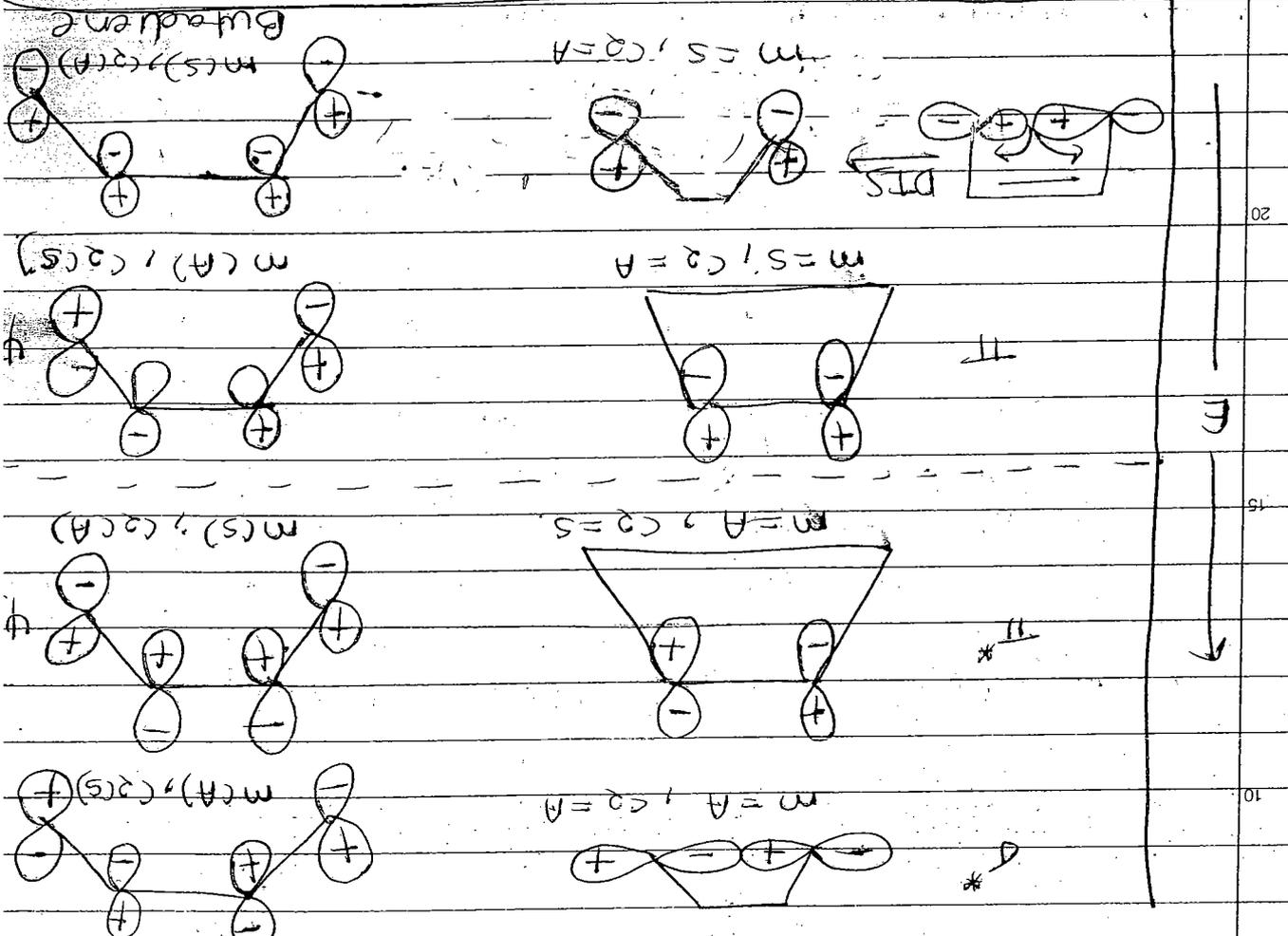
i) Thermal transformation is symmetry allowed when the ground state orbitals of the reactant correlate with ground state orbitals of the product. The reactant correlate with ground state orbitals of the reactant correlate with first excited state orbitals of the product when first excited state orbitals aligned when first excited state orbitals of the reactant correlate with first excited state orbitals of the product.

ii) Photochemical transformation is symmetry allowed when first excited state orbitals of the reactant correlate with first excited state orbitals of the product. The reactant correlate with ground state orbitals of the reactant correlate with first excited state orbitals of the product when first excited state orbitals of the reactant correlate with first excited state orbitals of the product.

iii) Thermal transformation is symmetry allowed when the ground state orbitals of the reactant correlate with ground state orbitals of the product.

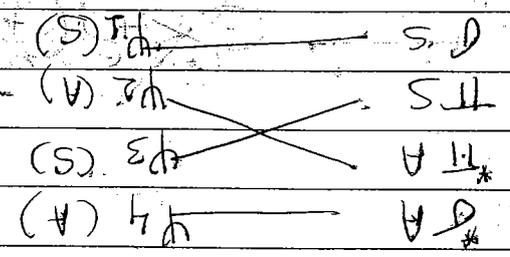
iv) Photochemical transformation is symmetry allowed when the ground state orbitals of the reactant correlate with first excited state orbitals of the product.

- a) under thermal condition : \rightarrow
- ! let us first analyse a distrotatory opening of cyclobutene under thermal condition.
- In a distrotatory opening always plane symmetry is maintained through the transition.
- correlation diagram can be represented as : \rightarrow

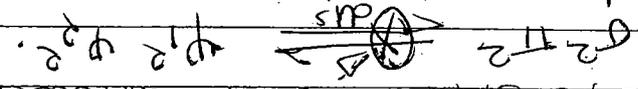


In the above correlation diagram which is orbital of cyclobutene correlate with ψ which is ground state $m=0$ of 1,3-butadiene.

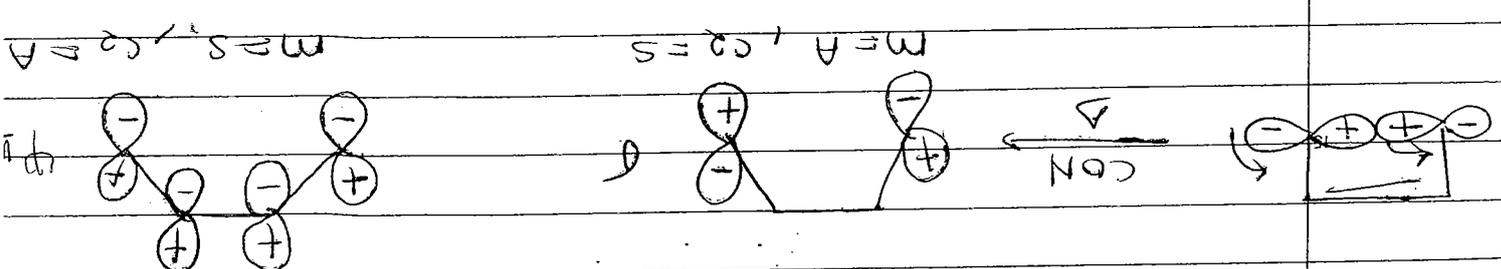
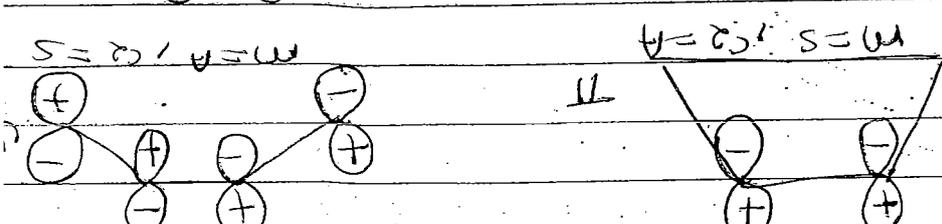
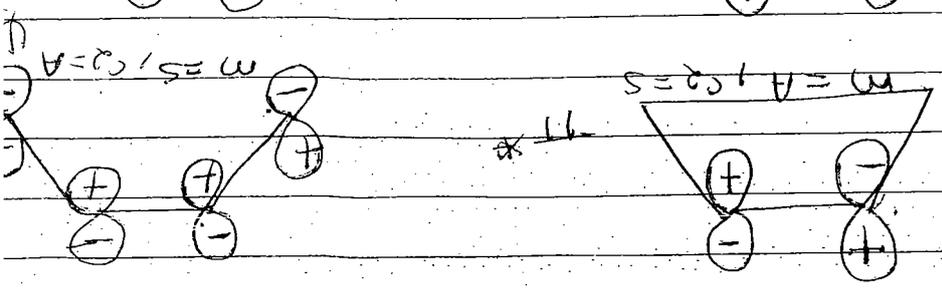
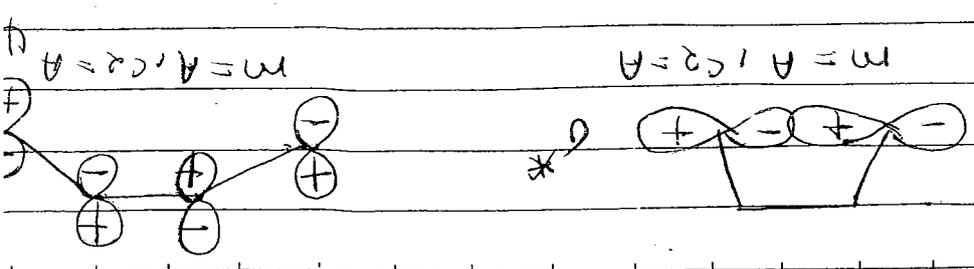
Let us analyse the ring opening (closing) by con rotation, in which (2) axis of symmetry is maintained throughout the transformation.



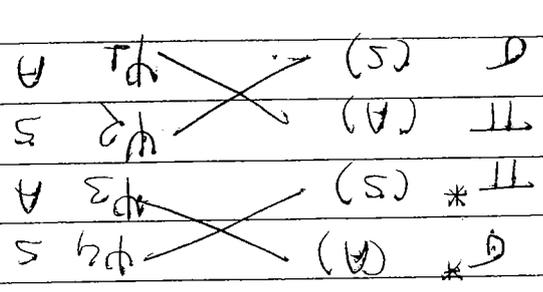
This correlation can also be represented as



symmetry forbidden (not allowed). Hence thermal transformation of cyclohexane to butadiene by distortion process is correlation, but their symmetry properties by distortions there is no such type of symmetry properties but in this interconversion with σ s. mo's of the product in their when σ s. mo's of the reactant correlate Thermal transformation takes place only orbital. ψ_3^* which is an excited state antibonding of 1,3 butadiene, but it correlate with ψ_2 which is another ground state mo of cyclohexane does not correlate with π which is another ground state of



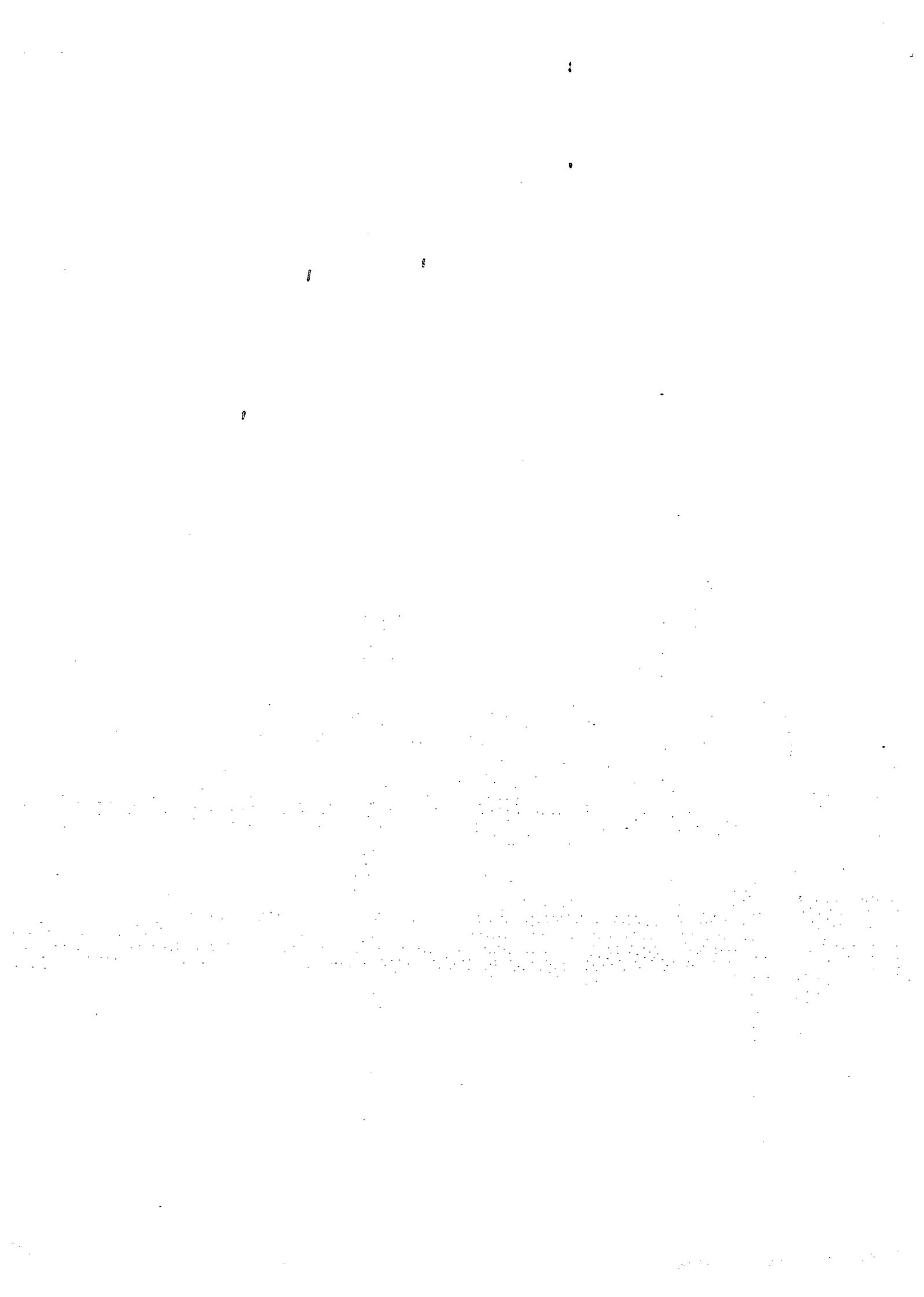
This correlation can also be represented as



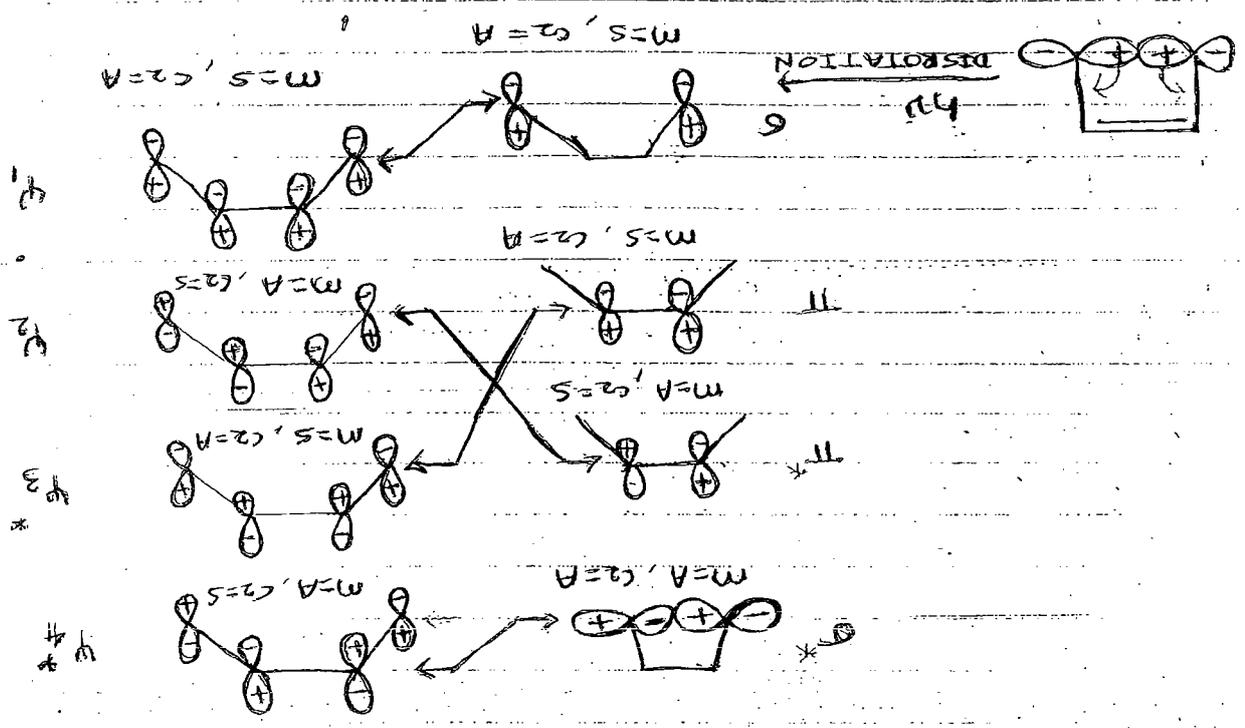
The above correlation diagram shows that σ -s MO's. σ π^2 of cyclobutene correlate with σ -s state MO's. π^2 of 1,3-butadiene.

Hence transformation of cyclobutene to 1,3-butadiene under thermal condⁿ by concerted

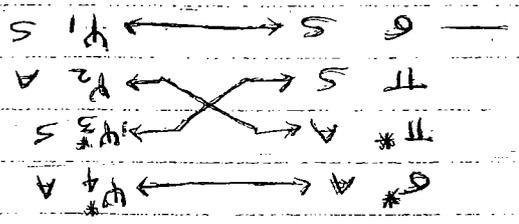
is symmetry allowed process.



Let us analyse transformation of cyclobutene to 1,3-butadiene under photochemical condition by disrotation in which plane of symmetry is maintained throughout the transformation. The correlation diagram can be shown as -

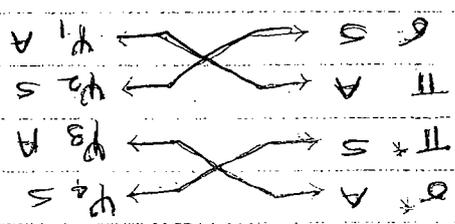


This correlation diagram can also be represented as -

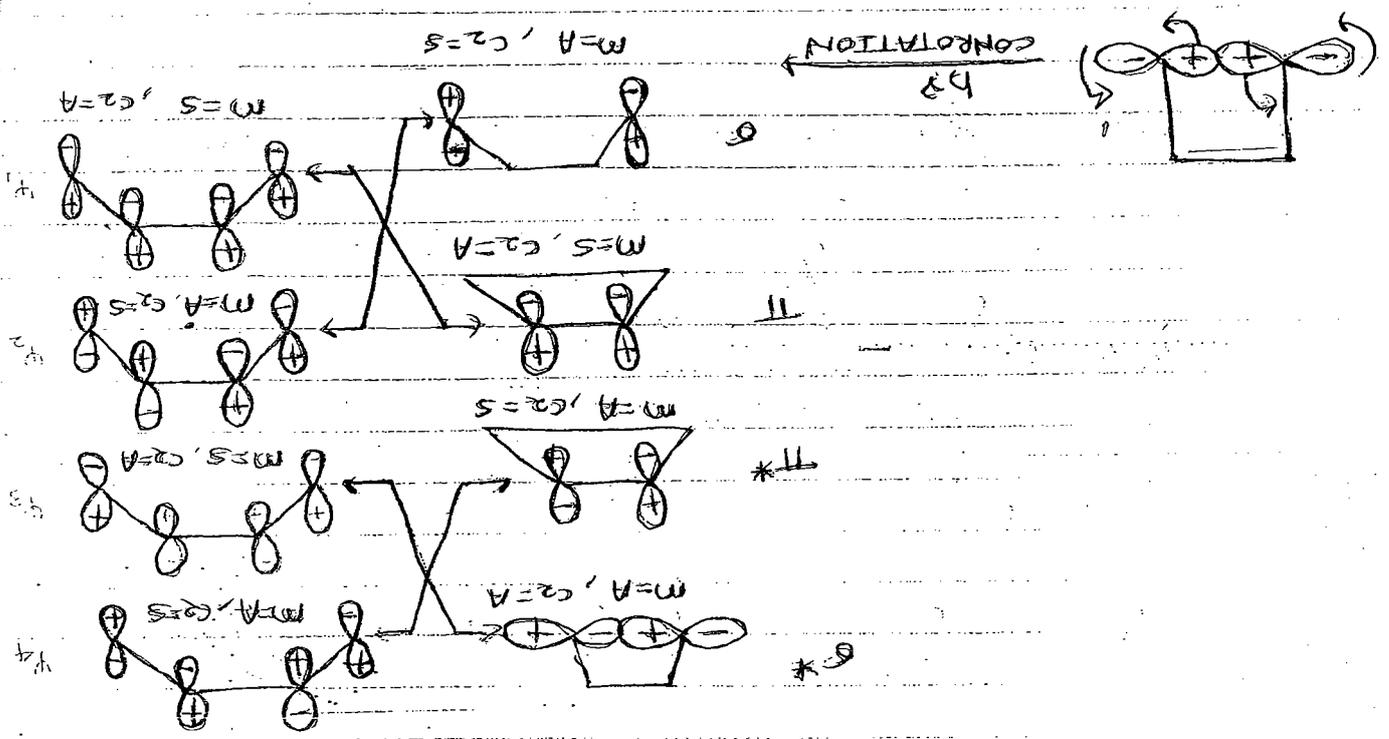


on irradiation with UV rays one electron from π orbital gets promoted to π^* . Hence first excited state of cyclobutene becomes $\pi^*\pi^*$.

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 33500
 2000

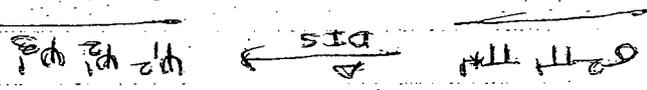


The correlation can also be represented as



The correlation diagram can be shown -

out the transformation.
 which a axis of symmetry is maintained through
 to butadiene under photochemical condition in
 Let us analyse the transformation of cyclobutene



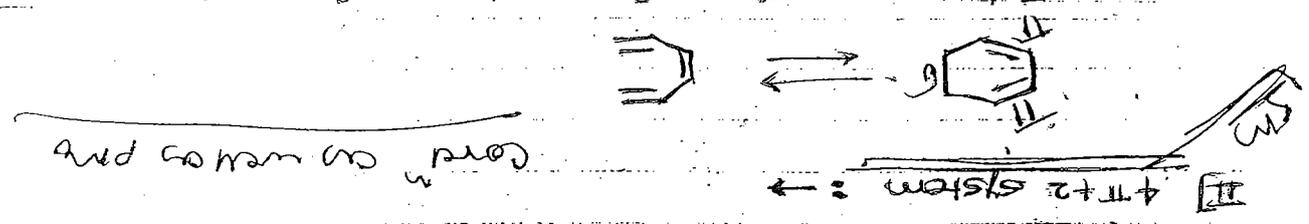
allowed process.

first excited state of cyclobutene $\psi_1^2 \psi_2^2 \psi_3^2$ correlate
 with first excited state of butadiene $\psi_1^2 \psi_2^2 \psi_3^2$ in
 their symmetric properties. Hence this transformation
 under h_2 condition by disrotation is symmetric

Dis-rotation (m) plane of system
 can-rotation (c) plane of system

Let us analyse ring opening (or ring closing) of cyclohexadiene under thermal condition by disrotation in which plane of symmetry is maintained throughout the transformation correlation diagram of symmetry properties of cyclohexadiene and 1,3,5-hexatriene can be represented as =

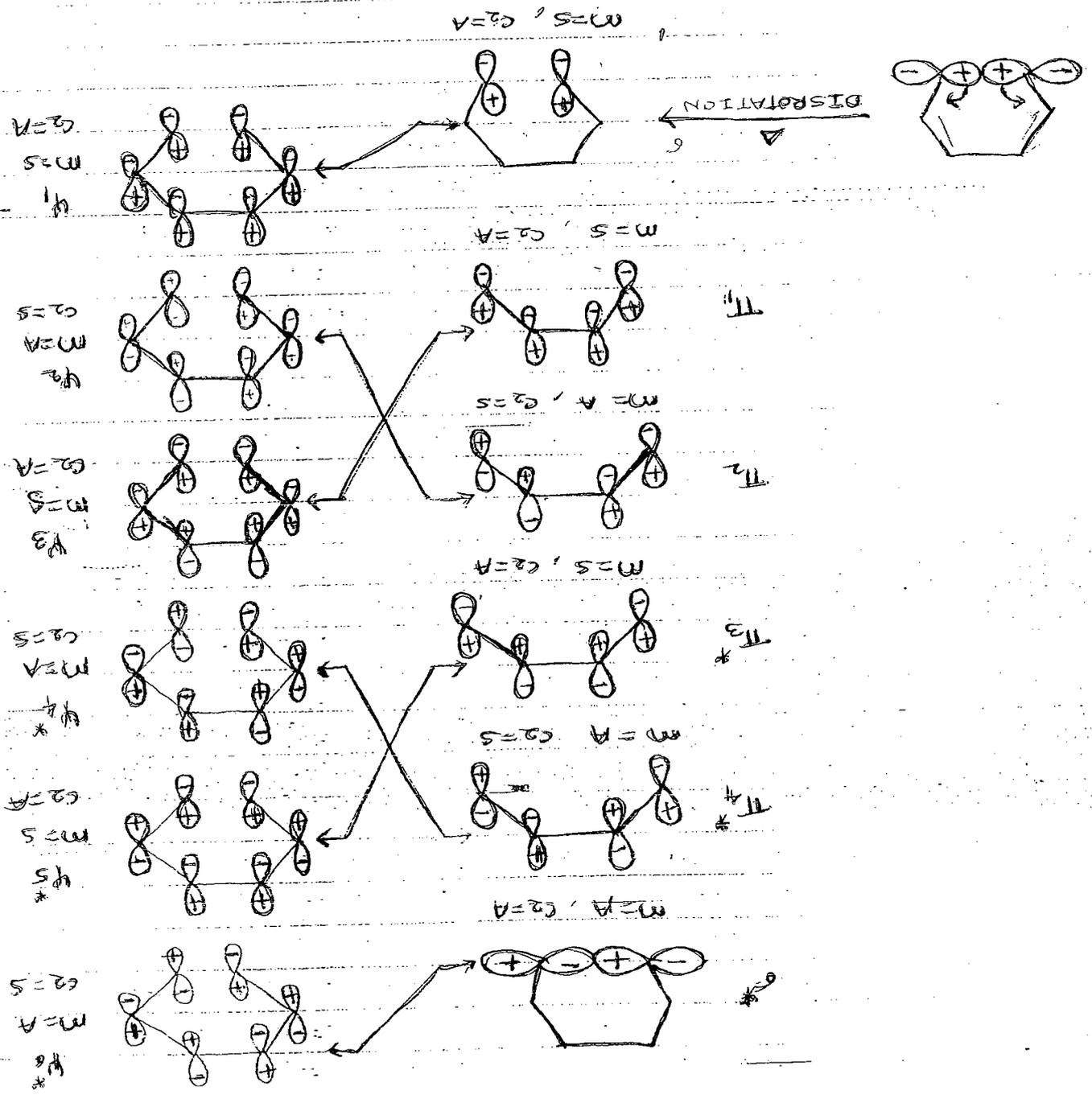
Interconversion of cyclohexadiene to 1,3,5-hexatriene is an example of $4\pi+2$ system. In this interconversion g, π, π_2 bonding MOs and g, π, π_2 antibonding MOs of cyclohexadiene and ψ_2, ψ_3 bonding MOs as well as ψ_4, ψ_5, ψ_6 antibonding MOs of 1,3,5-hexatriene are involved.



on irradiation with or rays one electron from π -orbital is promoted to π^* . Hence first excited state of cyclohexadiene becomes g, π, π^* . The above correlation diagram shows that first excited state of cyclohexadiene g, π, π^* correlates with the excited state of butadiene ψ_2, ψ_4 . But ψ_4 is second higher excited state. Hence this interconversion under the photochemical condition by con rotation is symmetry forbidden. All above are in agreement with Woodward-Hoffmann selection rule for electrocyclic reaction for 4π system.

Let us analyse ring opening of cyclohexadiene under photochemical condition by correlation in which axis of symmetry is maintained. The correlation diagram can be shown —

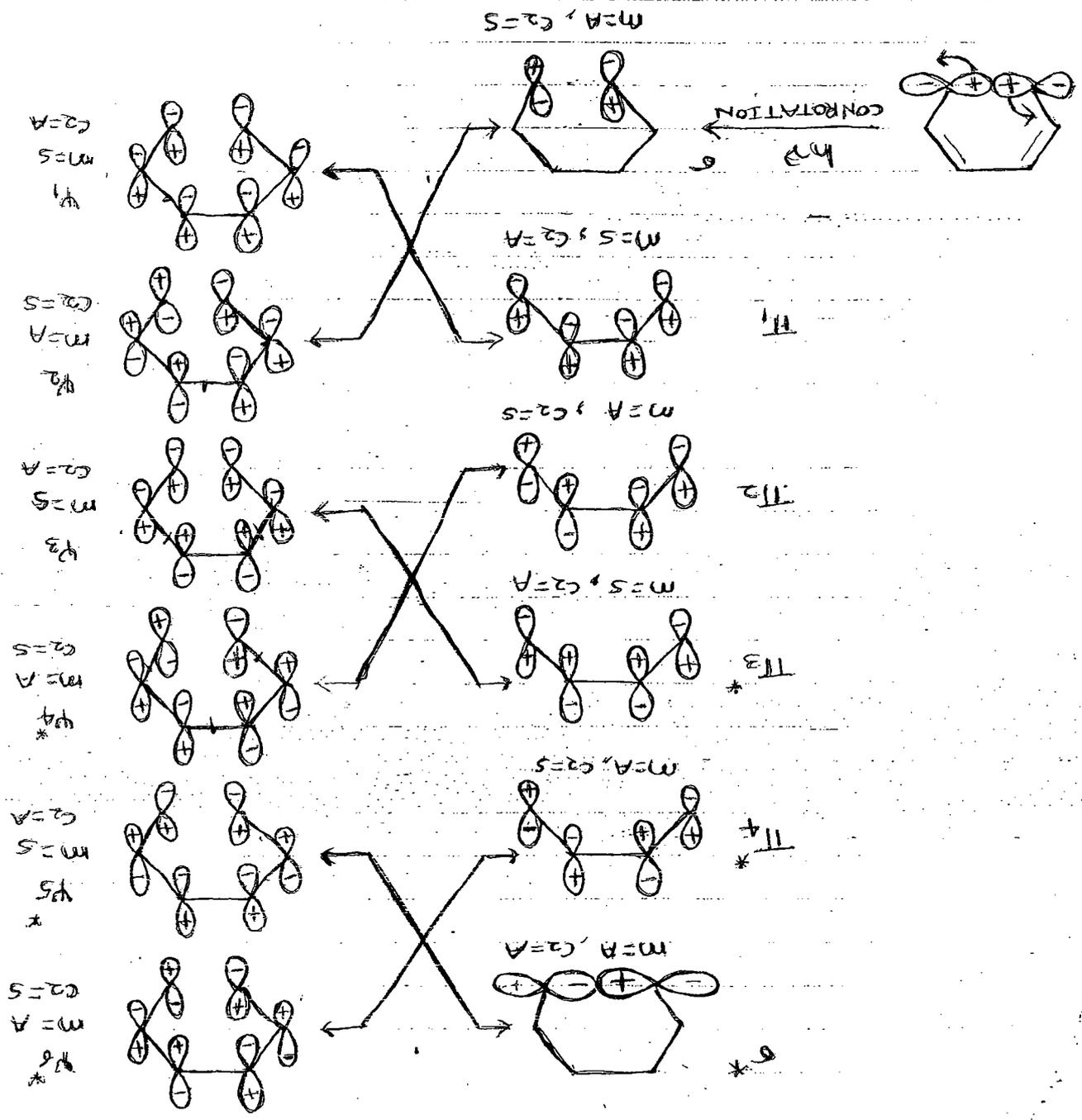
The above correlation diagram shows that under thermal condition ground state orbital of cyclohexadiene $\sigma^2 \pi^2 \pi^2$ correlates with ground state orbitals of 1,3,5-hexatriene $\psi_1^2 \psi_2^2 \psi_3^2$ in symmetry. Hence this interconversion under thermal condition by disrotation is symmetry allowed process.



$6^2\pi^2, \pi^1, \pi^1, \pi^1$ CONJUGATION \leftarrow $\psi^2, \psi^2, \psi^2, \psi^2, \psi^3, \psi^4$

1,3,5-hexatriene $\psi^2, \psi^2, \psi^3, \psi^4$

on irradiation with UV rays one electron from π -bonding orbital is promoted to π^* . Hence first excited state of cyclohexadiene becomes $6^2\pi^2, \pi^1, \pi^1$. This first excited state of cyclohexadiene correlate with the first excited state of



$m=1, g, 2=5$

CONJUGATION $h\nu$

$m=5, g=1$

$m=1, g=5$

$m=5, g=1$

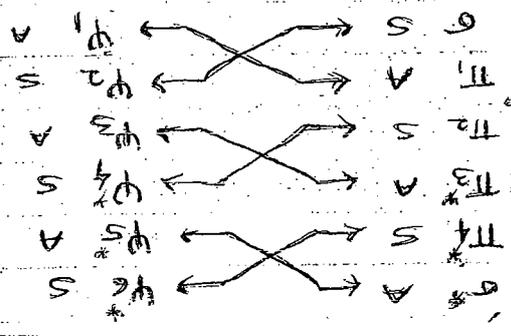
$m=1, g=5$

$m=1, g=1$

40	dis	dis
40	dis	dis
40	dis	dis

dis	dis	dis
dis	dis	dis
dis	dis	dis

The above facts are in agreement with the Woodward-Hoffmann selection rules for $\pi + 2$ system



Hence this interconversion under photochemical condition by conrotatory is symmetric allowed process. This correlation can also be represented as -

3)

Huckel-Mobius method or perturbation molecular orbital (PMO) method.

Another method for quickly predicting whether a given reaction is allowed by examining the cyclic array of orbitals at the transition state of the pericyclic reaction. Huckel rule of aromaticity states that a mono-cyclic, planar, conjugated system is aromatic if it has $(4n+2)\pi$ conjugated or delocalised electrons and consequently stable in ground state.

Similarly, monocyclic planar, conjugated systems are anti-aromatic if they have $4n\pi$ conjugated or delocalised electrons. This system is unstable in ground state. However, further calculation shows that these rules are reversed by the presence of a node in the array of atomic orbitals. Thus, system with $(4n+2)\pi e^-$ & a node is anti-aromatic while system with $4n\pi e^-$ & a node is aromatic. Thus, system has no node then:

$(4n+2)\pi$ electrons \rightarrow aromatic \rightarrow stable in ground state
 $4n\pi$ electrons \rightarrow anti-aromatic \rightarrow unstable in ground state

Similarly, system having a node then:

$(4n+2)\pi e^- \rightarrow$ aromatic \rightarrow stable in ground state
 $4n\pi e^- \rightarrow$ anti-aromatic \rightarrow unstable in ground state

If system has no node then it is called Huckel system and array is called Huckel array. Similarly, if system has node then it is called Mobius system and array is called Mobius array.

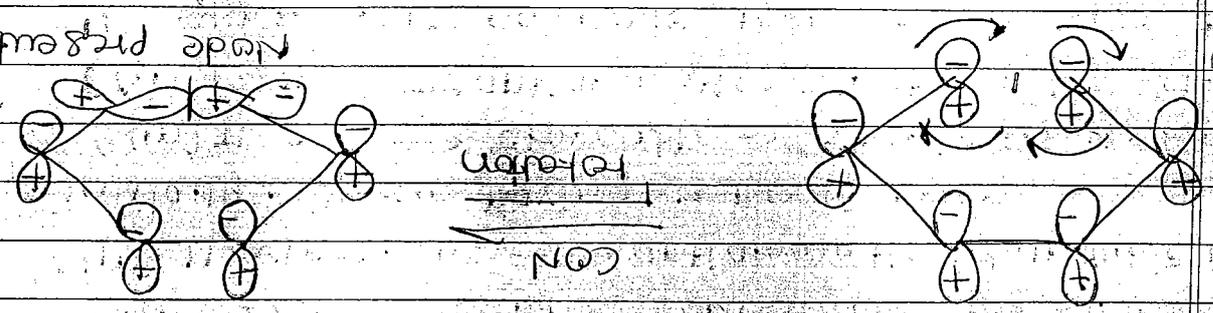
Application of these rules to pericyclic reactions led to the generalisation that thermal reactions -s takes place via aromatic transition state or $(4n+2)\pi$ electrons having no node or $(4n)\pi$ electrons having one node] whereas photochemical reaction proceed via antiaromatic transition state. (i.e. $(4n)\pi$ e- having no node or $(4n+2)\pi$ electrons having one node.]

A cyclic transition state is said to be aromatic or is conjugated with the corresponding aromatic system. Pericyclic reactions can be classified as aromatic or antiaromatic based on either Huckel or Mobius aromaticity.

According to the concept of aromatic and antiaromatic system,

Let us consider the following electrocyclic reaction of cyclohexadiene \rightleftharpoons cyclohexadiene

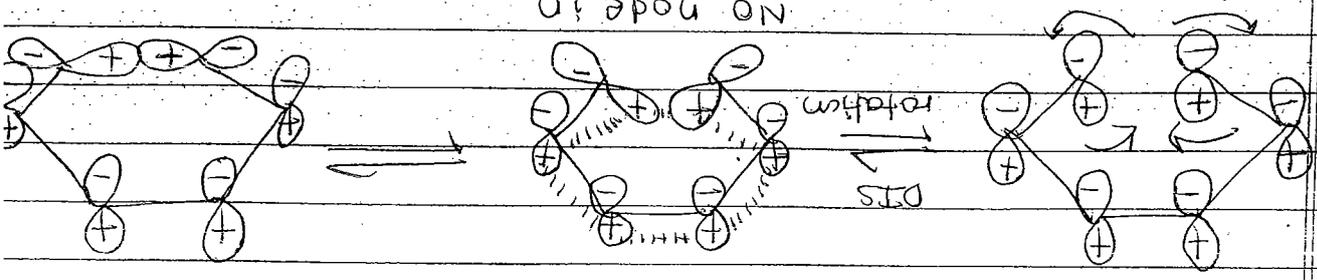
① Conrotatory motion \rightarrow



Conrotatory ring closure of 1,3,5-hexatriene system. The number of nodes = 1. Array of orbital arrangements :- Mobius. Number of π -electrons = 6. The system is antiaromatic according to Mobius.

and therefore, it is photochemically allowed.

Disrotatory motion: 7



NO node in T.S.

disrotatory ring closure of 1,3,5-hexatriene system.

The number of node = 0

Array of orbital arrangement: Hückel

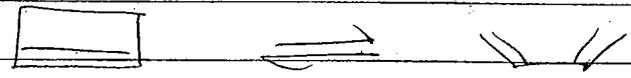
number of π electrons = 6

This system is aromatic according to Hückel and therefore, it is thermally allowed

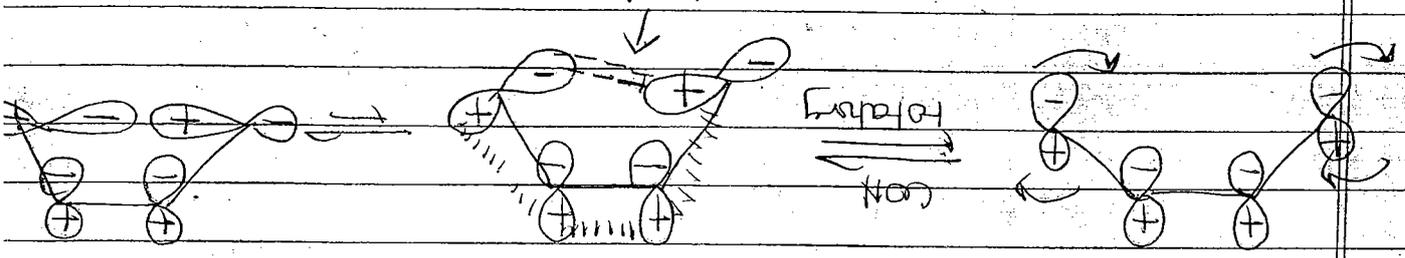
②

similarly for,

1,3-butadiene \rightleftharpoons cyclobutene



conrotatory motion: 7



NOTE: In T.S.

conrotatory ring closure of 1,3-butadiene system

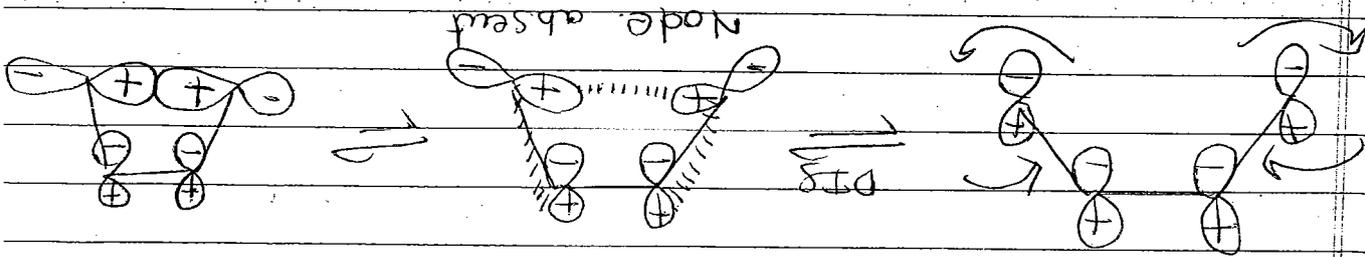
The no. of nodes = 1

Array of orbital arrangements: Möbius.

Number of π electrons = 4

The system is aromatic according to Möbius and therefore, it is thermally allowed

Disrotatory motion: \uparrow



Disrotatory ring closure of 1,3-butadiene system

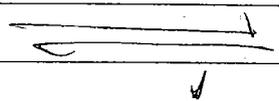
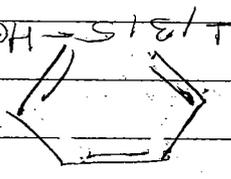
The number of nodes = 0

array of orbital arrangement: Huckel, number of π electrons = 4

The system is antiaromatic according to Huckel and therefore, photochemically allowed.

③

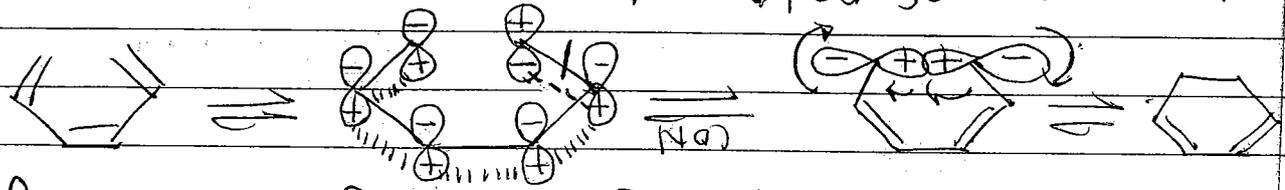
1,3-cyclohexadiene



Conrotatory motion: \uparrow

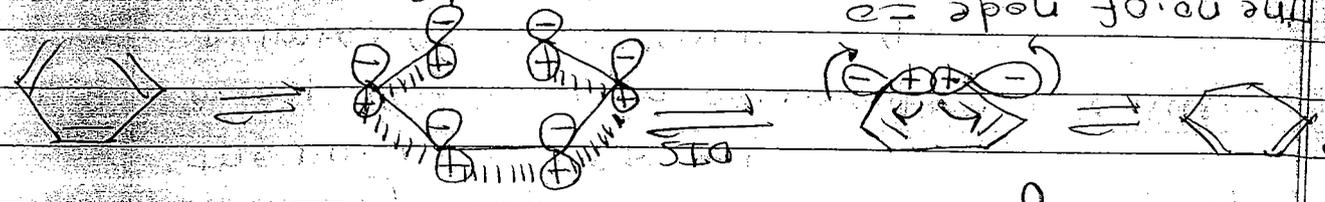
Conrotatory ring opening of 1,3-cyclohexadiene system

The number of nodes = 1



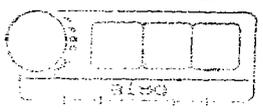
The system is antiaromatic according to Mobius and therefore, photochemically allowed.

Disrotatory motion: \uparrow



The no. of nodes = 2

array of orbital = Huckel No nodes

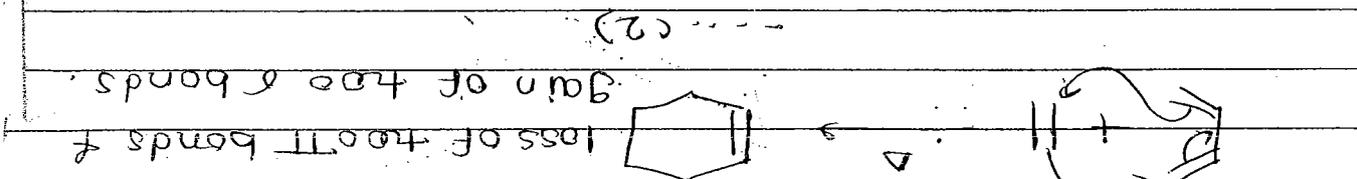
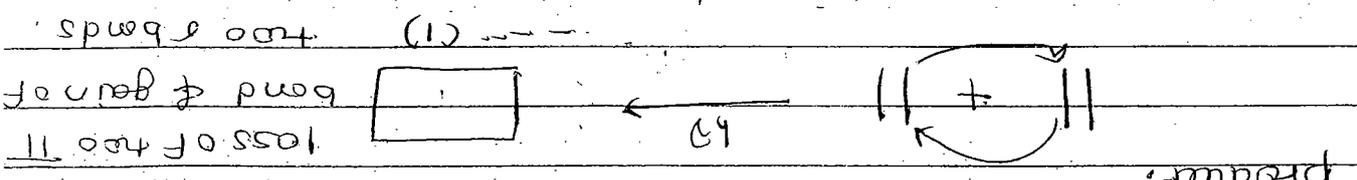


Cycloaddition Reaction :-

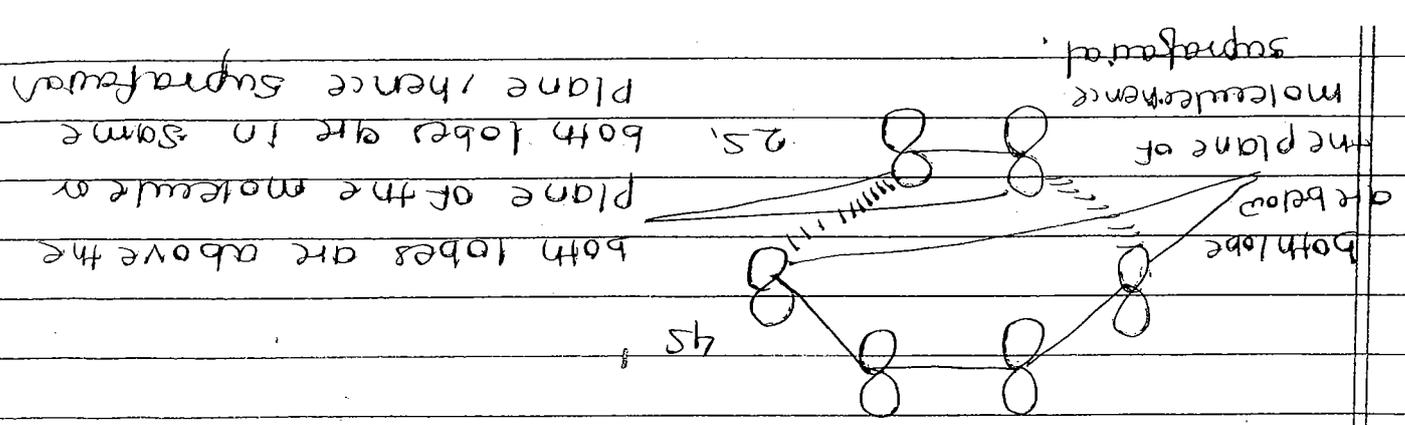
Introduction :-

A cycloaddition is a reaction in which two unsaturated molecules undergo an addition reaction to yield a cyclic product.

In this reaction there is loss of two π bonds of the reactants and gain of two σ bonds in the product.



The reaction in eqn (1) is a $[2+2]$ cycloaddition reaction because the reaction involves two electrons from one reacting component & also two electrons from the other. The reaction in eqn (2) is a $[2+2\pi]$ cycloaddition. The stereochemical mode is given by a subscript 's' or 'a' which indicates whether the addition occurs in a supra or antarafacial mode on each unit. If reaction occurs across the same face of π system the reaction is said to be suprafacial with respect to that π system, the suprafacial addn is nothing more than a syn addn.

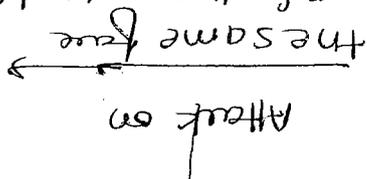


This addn reaction is thus $[4s+2s]$ cycloaddn

$[4s+2s]$



Attack on the same face of the molecule



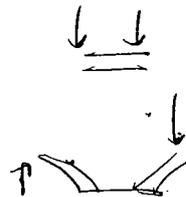
If the reaction bridges opposite faces of a π system it is said to be antarafacial. An antarafacial addn is just an anti addition

Antarafacial hence $4a$

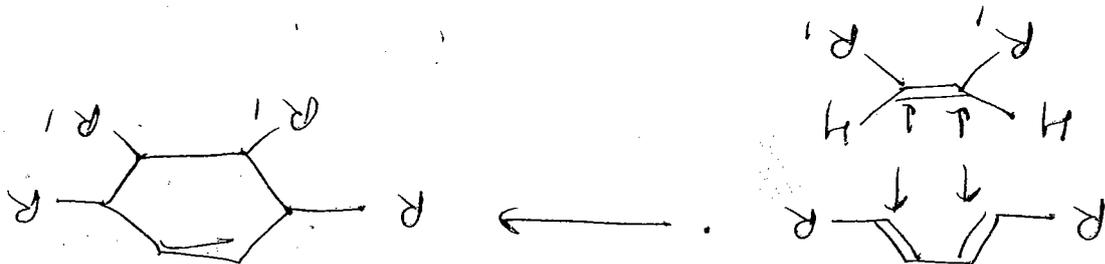
Suprafacial hence $2s$

This mode of addn reaction is thus $[4a+2s]$ cycloaddn. This can be represented as

$[4a+2s]$



Almost all cycloaddition reactions are suprafacial on both components.



Theory of cycloaddition reaction: FMO method
 For a cycloaddition between two components to occur, there must be bonding overlap between the p-orbitals at the terminal carbons of each π electron system.

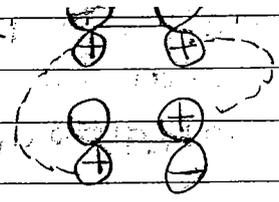
Overlap can occur between ground state HOMO of one component and ground state LUMO of another component under thermal condition and overlap can occur between first excited state HOMO of one component and ground state LUMO under photochemical condition.

I] [2+2] cycloaddition reactions: ->

a) Thermal induced [2+2] cycloaddition reaction: ->

Under thermal condition ψ_1 represents HOMO of one ethylene molecule LUMO of another ethylene molecule under thermal condition is represented by ψ_2

overlapping betⁿ HOMO of one ethylene molecule (ψ_1) and LUMO of another ethylene molecule (ψ_2) takes place by supra-ant^r process which is symmetrically forbidden. Hence cycloaddition reaction betⁿ two ethylene molecule under thermal condition is not possible



ψ_2 LUMO of one molecule, (2 symmetric) ψ_1 HOMO of other mol. (1 symmetric)

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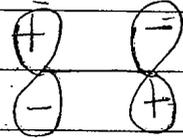
5

For bonding, the phase of the overlapping must be same. Hence thermally induced $[2+2]$ cycloaddition is said to a symmetry forbidden

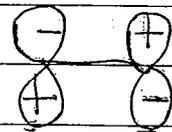
B) Photo-induced $[2+2]$ cycloaddition:

under photochemical condition one electron of ψ_1 of one ethylene molecule is promoted to ψ_2 .

Hence under photochemical condition ψ_2 become HOMO and ψ_1 is LUMO of another molecule



ground state LUMO, ψ_2 symmetry



excited state HOMO, ψ_1 symmetry

for cycloaddition. reaction both HOMO & LUMO should have same symmetry.

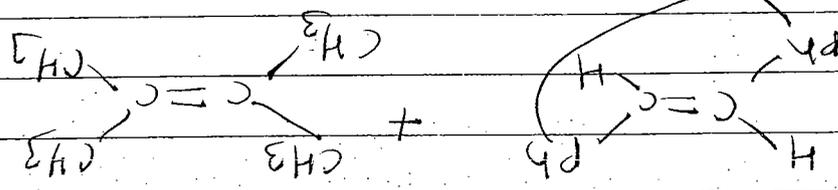
overlapping between HOMO of one ethylene molecule and LUMO of another ethylene molecule takes place by supra-supra process which is symmetrically allowed.

Hence cycloaddition can't be π to ethylene molecule takes place under photochemical condition.

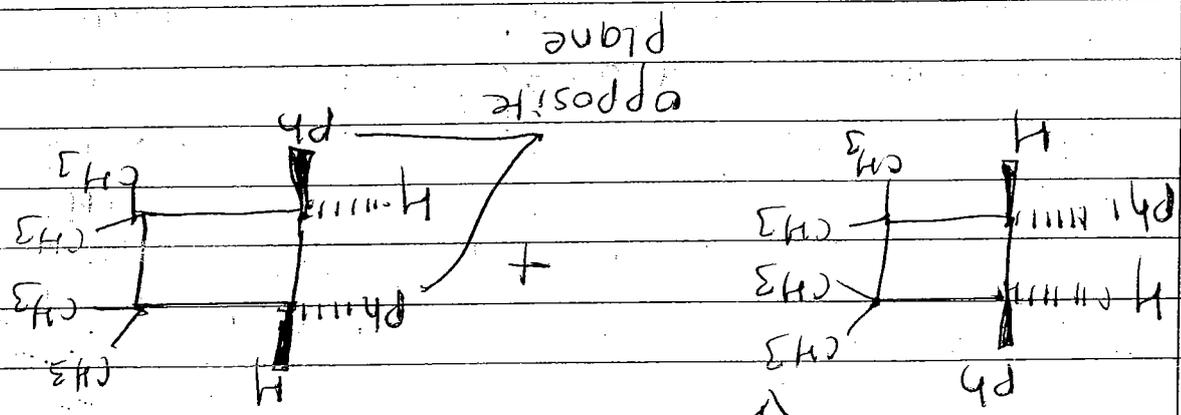
Hence for $[2+2]$ system cycloaddition reaction under thermal condition is supra-supra symmetry forbidden.

Stereochemistry :-

Stereochemical integrity is maintained in cyclic addition reaction because the reactants are



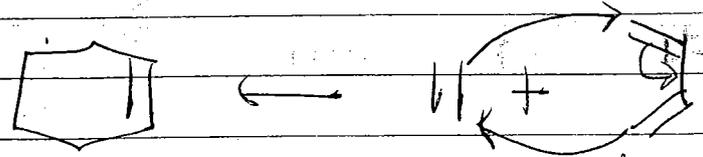
↑
opposite plane



opposite plane

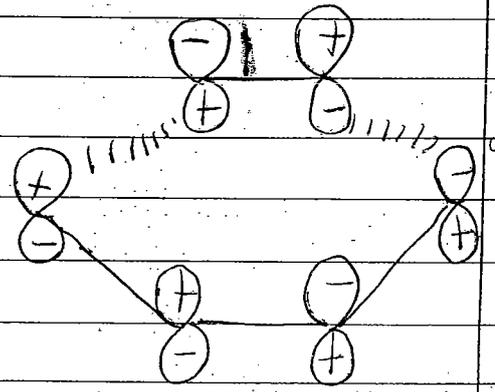
III) [4+2] cycloaddition reaction :- Diels-Alder

The best example of this type is diene and ethylene (dienophile) to form cyclohexene (product).



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a) Under thermal condition: \rightarrow
 Under thermal condition HOMO of 1,3-butadiene can be represented by ψ_2 while LUMO of ethylene can be represented by π_2 .
 Overlapping between these mo's is supra-supra

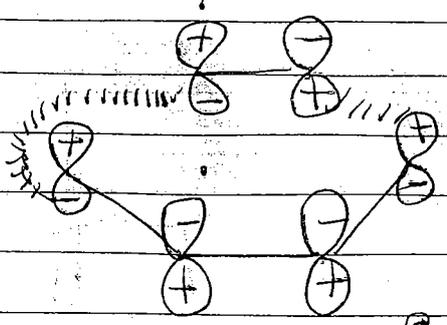


HOMO ψ_2 , CO symmetry

LUMO π_2 , CO symmetry

regioaddition reaction. Both HOMO of LUMO should have same symmetry. HOMO of LUMO have same symmetry. Hence, cycloaddition reaction between 1,3-butadiene and ethylene under thermal condition is symmetry allowed process.

b) Under photochemical condition: \rightarrow
 on irradiation with UV light one e^- excite from ψ_2 of 1,3-butadiene to ψ_3 . Hence ψ_3 becomes HOMO of LUMO of ethylene can be represented by π_2 .



HOMO ψ_3 , CO symmetry

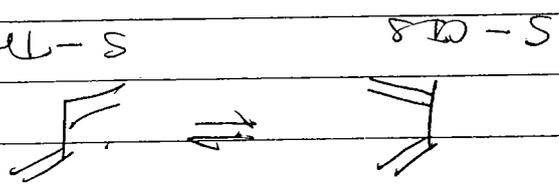
LUMO of π_2 , CO symmetry

overlapping betⁿ these two. Mos is supra-anti hence cycloaddition ratⁿ betⁿ 1,3-butadiene and ethylene under photochemical condition is symmetry forbidden condition.

No. of e ⁻	Mode of activation	Allowed Stereoche
4h ν (2+2)	Photochemical	supra-supra
(4h ν +2) ν	Thermal	supra-supra

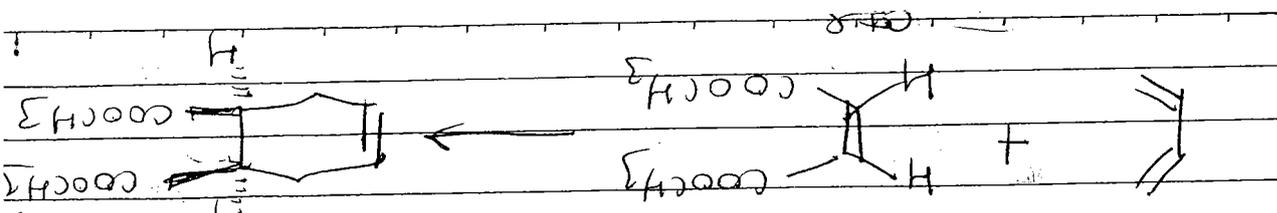
Stereochemistry of the Diels-Alder reaction

a] The diene must be in the conformation (s-c) that permits the end of the conjugated system to react the doubly bonded carbon of the dienophile.

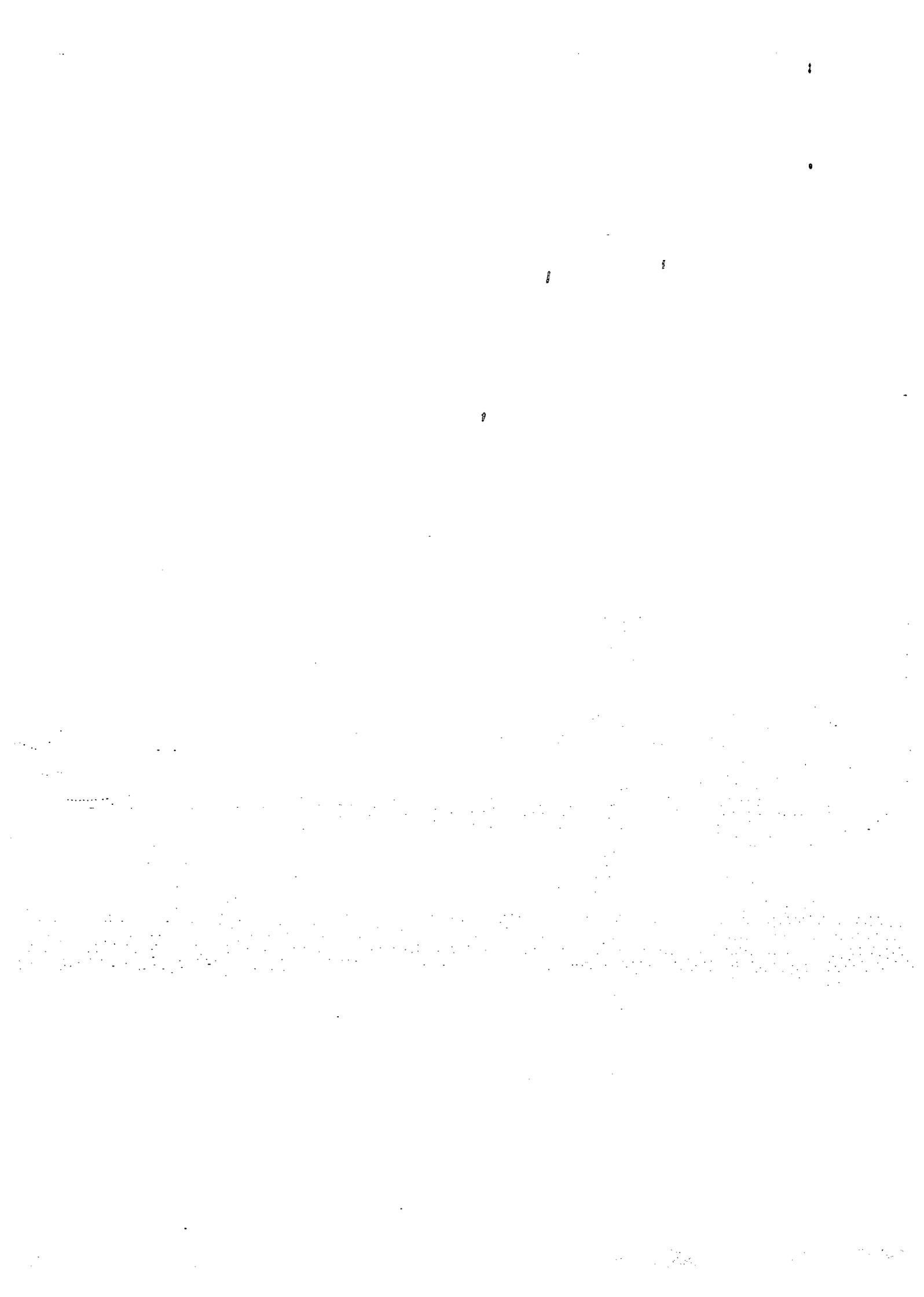


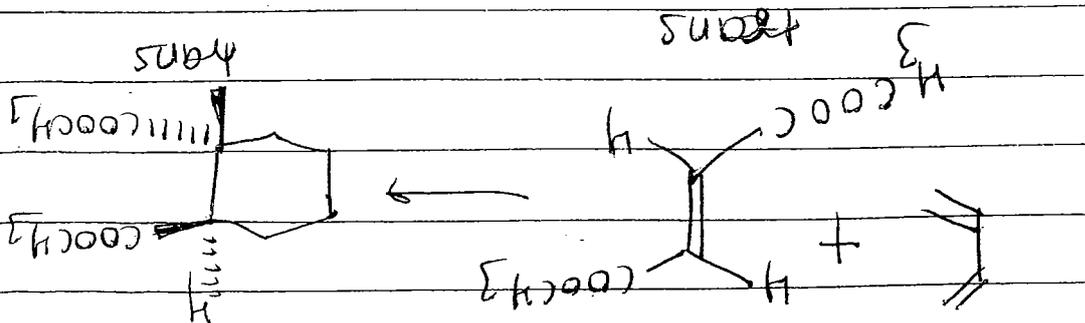
b] Stereochemistry of the dienophile = 7

The Diels-Alder reaction is stereospecific. Substituents that are cis in the dienophile remain cis in product. Substituents that are trans in the dienophile remain trans in the product.

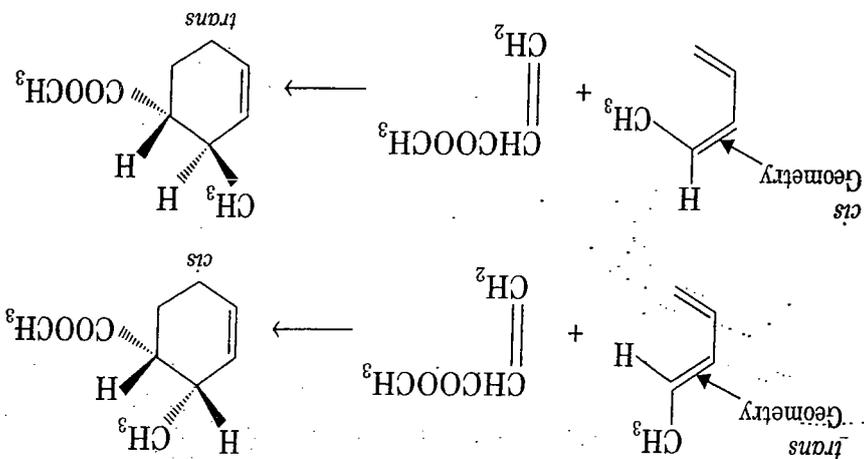


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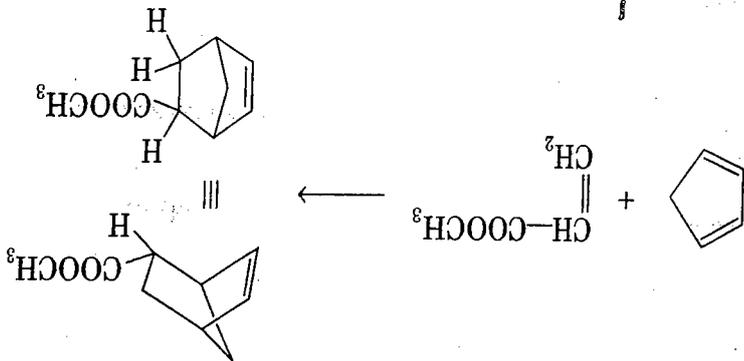




We also need to consider the stereochemistry in the product of the substituents on the diene relative to those on the dienophile. If *trans* 1,3-pentadiene reacts with methyl propenoate we know that in the product the methyl and ester groups could be either *cis* or *trans*. It is found, in fact, that the *cis* product is formed from *trans* diene and the *trans* product is formed from *cis* diene.



(iii) **Endo and Exo stereochemistry:** The Diels-Alder reaction will produce a bicyclic ring system if the diene is monocyclic. Cyclic dienes are particularly reactive in Diels-Alder reaction because the two double bonds are held in an *s-cis* conformation in five or six-membered rings. This can be seen in the reaction of 1,3-cyclopentadiene with methyl propenoate.



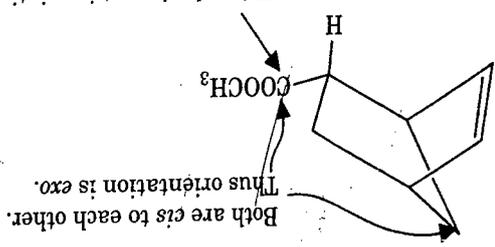
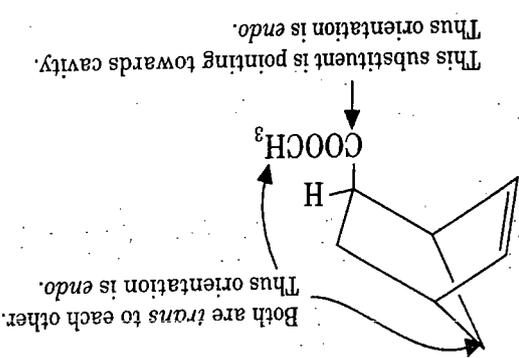
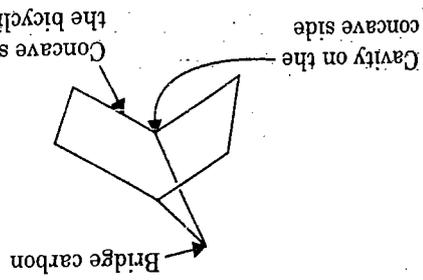
When a compound like this is synthesised, we introduce another stereochemical question. What will be the relative stereochemistry of the methylene bridge and the substituent (in this case COOCH_3)? Will they be *cis* or *trans*? Asking these questions is the same as asking whether the substituent will be *endo* or *exo* in the product. An orientation is said to be *endo* meaning that the substituent is *trans* to the bridge carbon or substituent projects into

ical question.
 (in this
 the same as
 is said to be
 projects into

duce a bicyclic
 in Diels-Alder
 six-membered
 enoate.

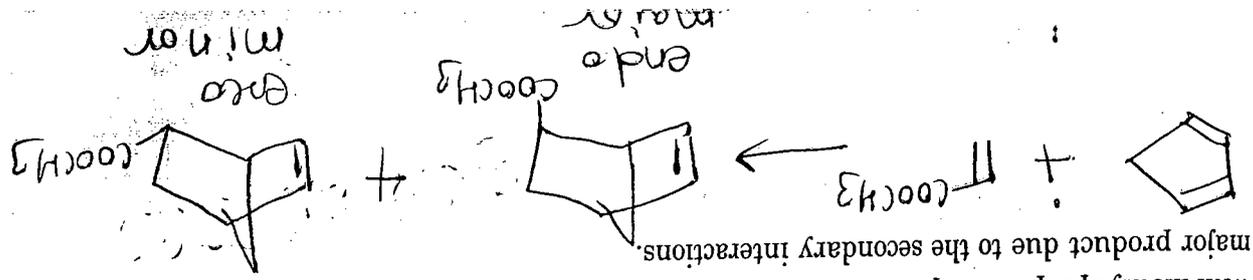
stituents on the
 ethyl propenoate
 or *trans*. It is
 product is formed

the cavity on the concave side of the bicyclic ring. Similarly, an orientation is said to be *exo* meaning that the substituent is *cis* to the bridge carbon or substituent projects out of the cavity on the concave side of the bicyclic ring.



The *exo* product is expected to be more stable than the *endo* product for steric reasons. In *exo* product, the *exo* substituent points away from the more congested part, i.e., bicyclic ring but in *endo* product the *endo* substituent points towards the more congested part. Thus steric repulsion in *endo* is more than in *exo*. Due to this reason, *exo* is expected to be more stable than *endo*.

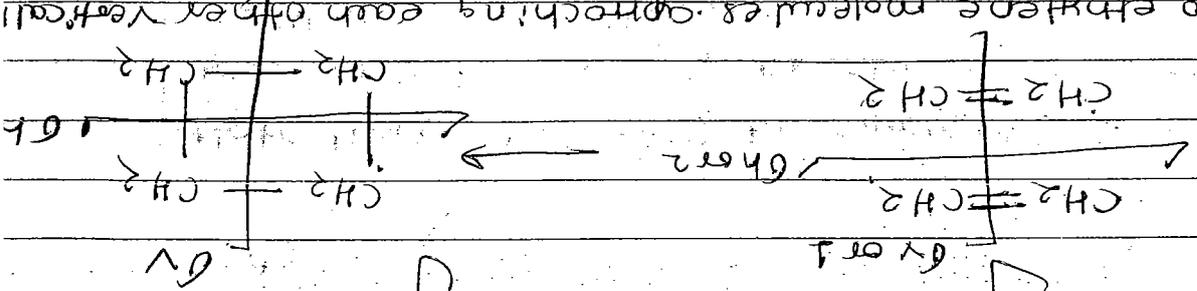
But in practice it has been found that if the diene has a π bond in its electron-withdrawing group then the *endo* product is more stable than the expected *exo* product. This stereochemical preference for the *endo* position is often called the *endo* rule. The reaction of 1,3-butadiene with methyl propenoate produces three times as much as *endo* as *exo* product. *Endo* product is major product due to the secondary interactions.



Correlation diagram method & \rightarrow

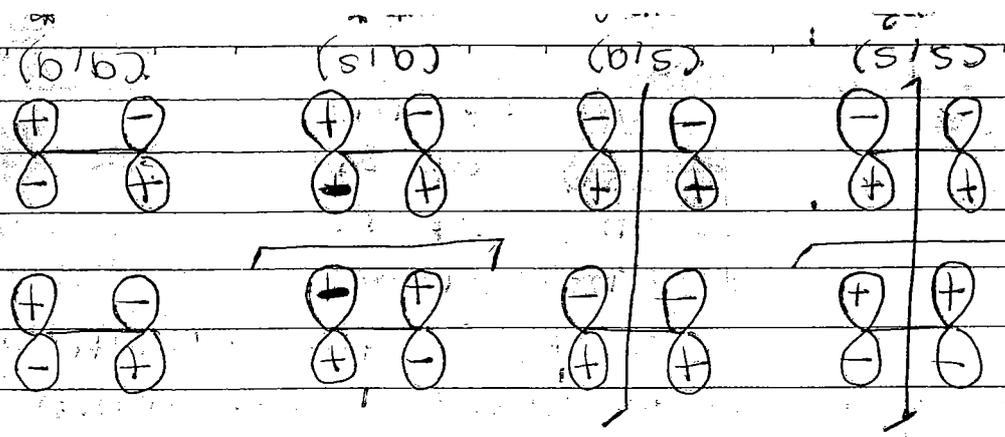
I) $(2+2) \pi$ system: \rightarrow

orbital symmetry arguments make useful predictions about concerted cycloaddition reactions. Consider the $[2+2]$ cycloaddition of ethylene molecules in parallel planes approaching each other vertically.



Two ethylene molecules approaching each other vertically & suprafacial-suprafacial.

This system contains vertical & horizontal plane of symmetry (i.e. mirror plane of symmetry) denoted by σ_v (or σ_1) and σ_h (or σ_2) which are useful in characterising the orbitals. In the transformation of ethylene molecules to cyclobutane we are mainly concerned with the four π orbitals of two ethylene molecules & the four σ orbitals of cyclobutane. Let us first take the σ of σ_h in two ethylene molecules.



30
25
(sigma/1, sigma/2)

σ_a to σ_a
 σ_s to σ_s
 σ_s to σ_s
 σ_a to σ_a

in the product σ_s to σ_s
 molecular into orbitals of the same symmetry
 We can now complete by combining energy
 levels feeding the orbitals in the starting
 lowest energy orbital.

σ_s σ_s σ_a σ_a

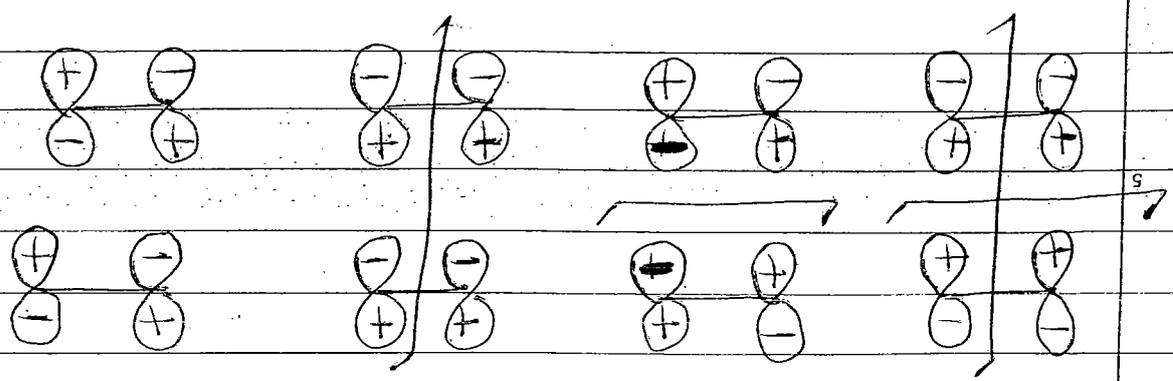
Energy of σ system is as follows in increasing
 order.

σ_s σ_a σ_s σ_a

Energy of π system is as follows in increasing
 order.

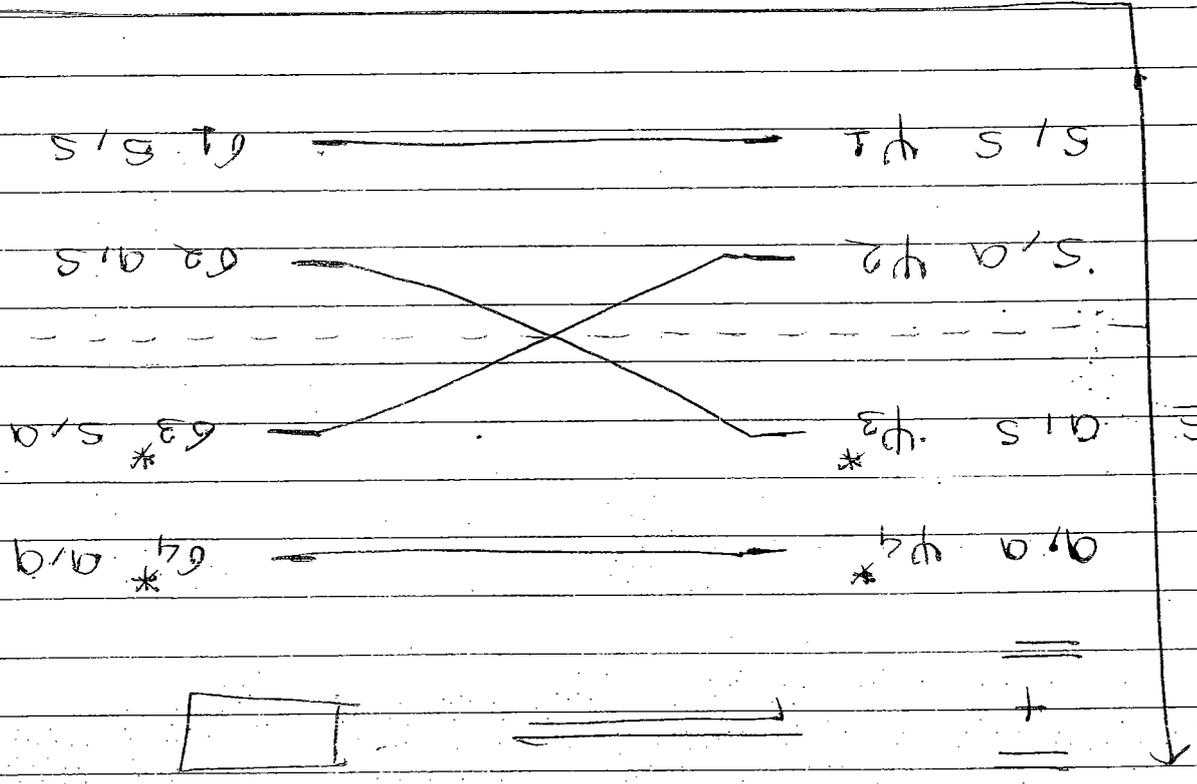
Note that more will be symmetry in the system
 less will be energy of the system for π as
 well as σ orbital.

(σ/s) σ_2^2 (σ/s) σ_2^2 (σ/s) σ_2^2
 (σ/a) σ_2^2 (σ/a) σ_2^2 (σ/a) σ_2^2
 (σ/a) σ_2^2 (σ/a) σ_2^2 (σ/a) σ_2^2



Now let us take the π of σ in cyclobutane

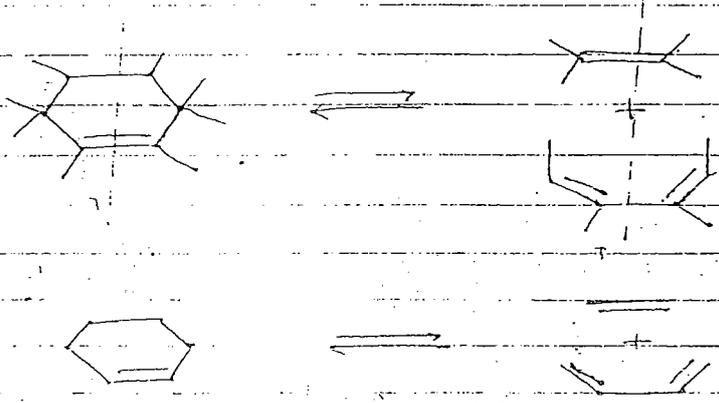
correlation dia. for cycloaddⁿ of ethylene into
 cyclobutane.
 The correlation dia. shows that ground state of
 two ethylene molecules $\pi_2^2 \pi_2^2$ correlate
 with $\sigma_1^2 \sigma_1^2$ but σ_1^* is the first excited.
 state. Hence cycloaddⁿ reaction between two
 ethylene molecule is symmetry forbidden.
 under photochemical condition the electron
 from π_2 get promoted to π_2^* . Hence first
 excited state of two ethylene molecule becomes
 $\pi_2^2 \pi_2^*$, $\pi_2^* \pi_2^*$. The above correlation dia.
 shows



on the basis of the above information, a
 correlation diagram may be drawn in which
 the levels of like symmetry are connected
 by lines.

Diagram shows that ground state orbitals correlate with ground state orbitals ($\sigma_1^2 \sigma_2^2 \pi_1^2$) of cyclohexene. Hence under thermal conditions this addition reaction is symmetry allowed. It is in agreement with the Woodward-Hoffmann selection rule.

q) Under Thermal condition: \rightarrow
 In this cycloaddition reaction, three π -ground state orbitals (2π ground state orbitals & 1,3-butadiene) of reactants (1,3-butadiene + ethylene) and three π^* orbitals and one π orbital & cyclohexene (product) and their respective antibonding orbitals are involved. For correlation diagram vertical plane of symmetry & these MOs is considered, correlation diagram can be represented as follows -



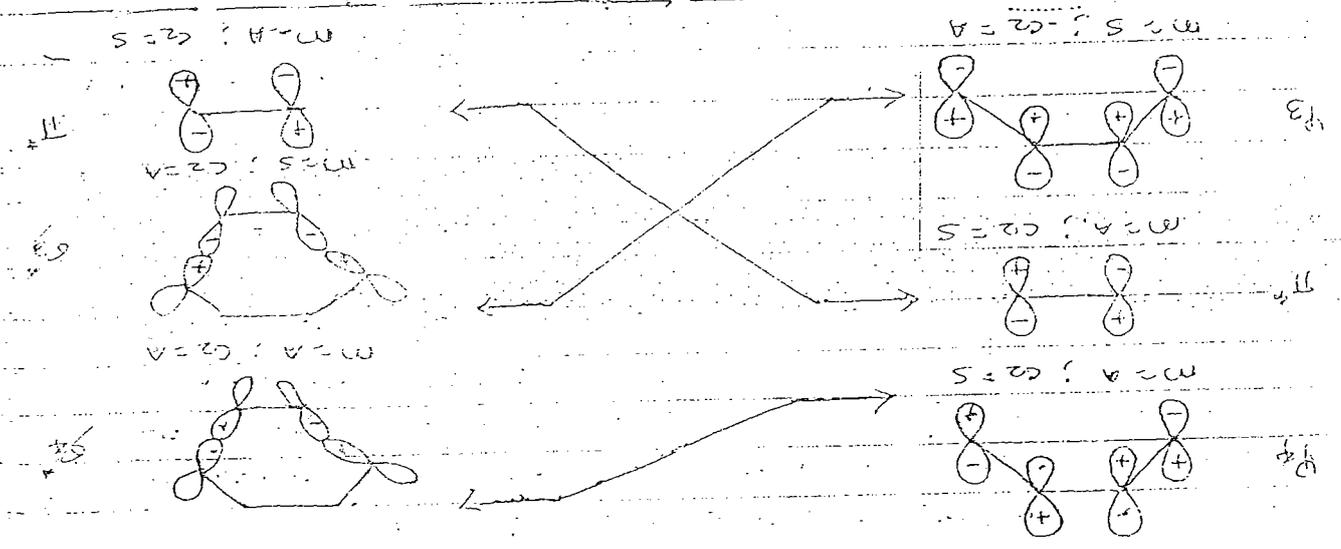
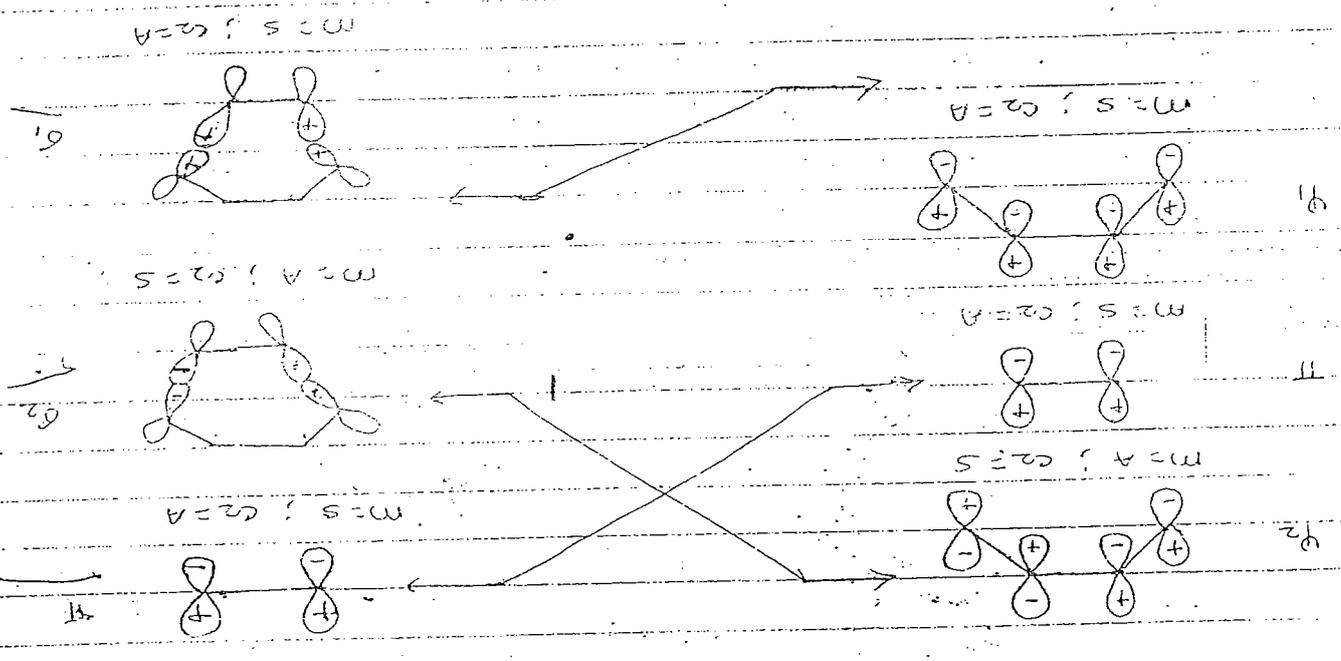
ii) ($2+2$) π system \rightarrow

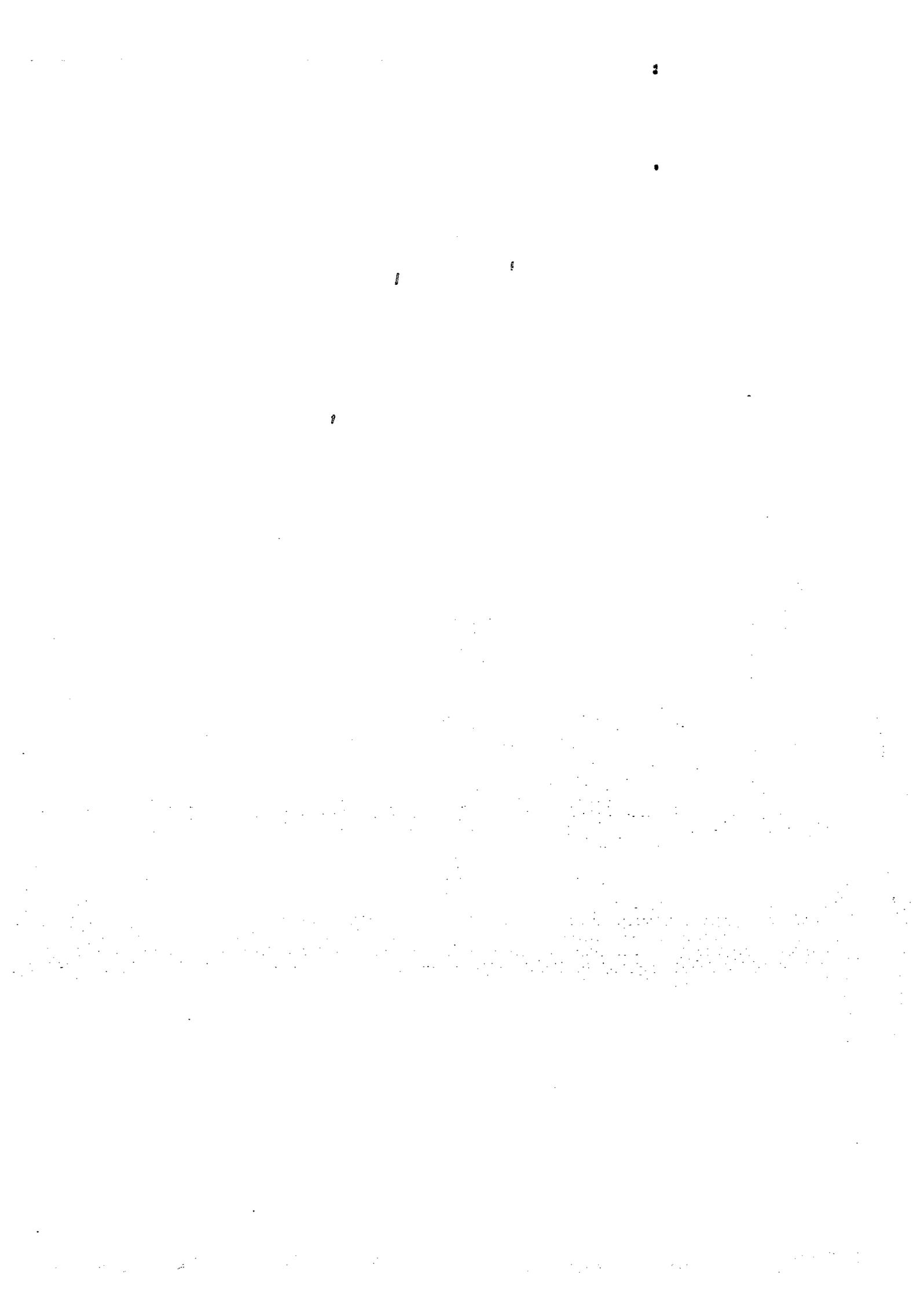
that this first excited state $\pi_1^2, \pi_2^2, \pi_1^1$ of two ethylene molecules correlates with the first excited state of cyclohexene $\sigma_1^2, \sigma_2^2, \pi_1^1$. Hence the cycloaddition reaction between two ethylene molecules under photochemical condition is symmetry allowed. These facts are in agreement with the Woodward-Hoffmann selection rule for $(2+2)\pi$ system cycloaddition reaction.

Hence under photochemical condition, this

on the other hand an irradiation with UV light, one electron from ψ_2 gets promoted to ψ_3 . Hence first excited state of reactants becomes $\psi_1^2 \pi^2 \psi_2^1 \psi_3^1$ which does not correlate with first excited state of product i.e. $\sigma_1^2 \sigma_2^2 \pi^1 \pi^1$

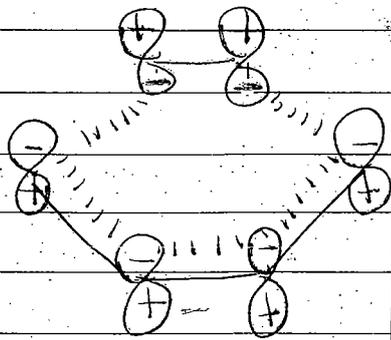
b] under photochemical condition, $\psi_1^2 \pi^2 \psi_2^2 \psi_3^2 \rightarrow \sigma_1^2 \sigma_2^2 \pi^2$





ii) $4+2$ cycloaddition: \rightarrow

S-S : \rightarrow



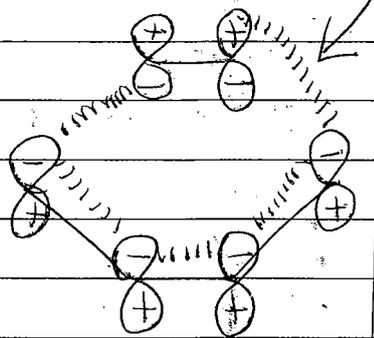
the no. of node = 0

no. of $\pi e^- = 6$

The system is aromatic due to Huckel's rule & therefore thermally allowed

-ally allowed

S-a : \rightarrow



The no. of node = 1

no. of $\pi e^- = 5$

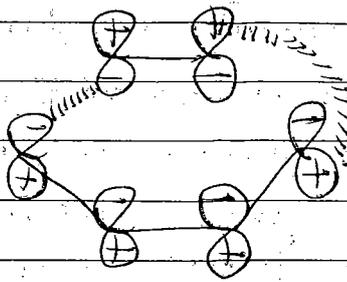
The system is antiaromatic due to the Mobius rule & therefore photochemically allowed

-mically allowed

a-s : \rightarrow

Similarly, a-s is. Mobius antiaromatic & therefore photochemically allowed

a-a



the no. of node = 0

no. of orbital arrangement = Huckel

no. of $\pi e^- = 6$

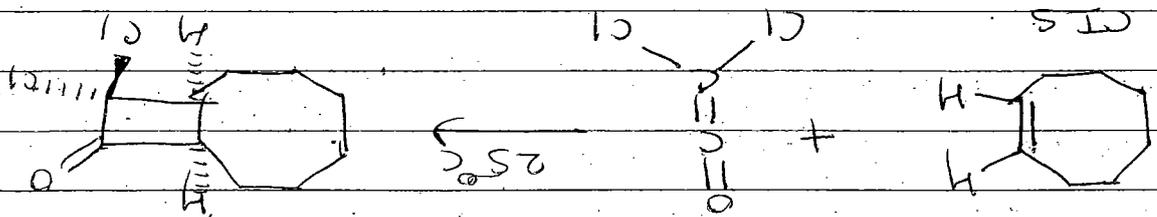
The system is aromatic according to Huckel's rule & therefore thermally allowed

allowed

[2+2] cycloaddition of ketene

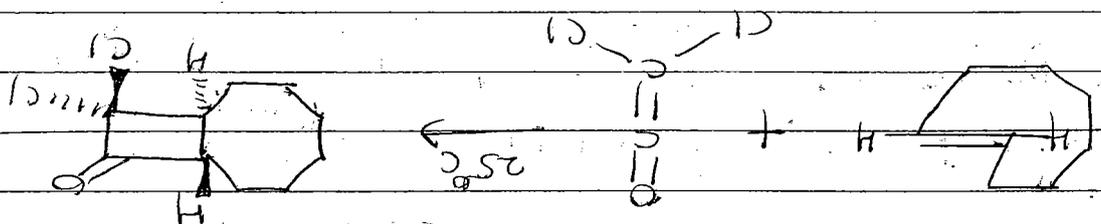
Let us first take some addition of ketene with alkene.

The reaction is syn addition and geometry of reactant is maintained in the product.



Both H' are cis

Both hydrogens are trans



In the give two examples. Stereochemistry of reactant is maintained in the product

These two reactions are pericyclic [2+2] cycloaddition reactions and thermally allowed reactions.

We know that [2+2] cycloaddition is photochemical reaction and supra-suprafacial.

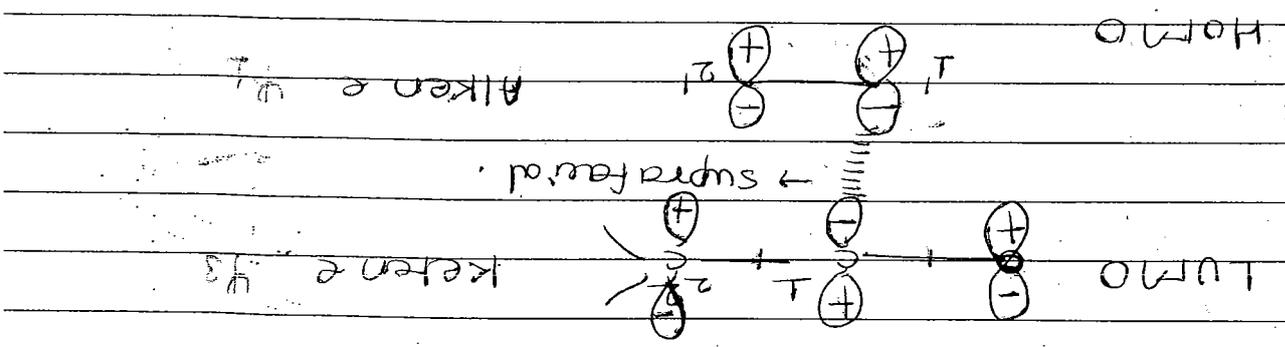
If reaction is thermally allowed then reaction should be suprafacial-antarafacial reaction.

The explanation for this is that it is suggested that two molecules approach each other at right angles for overlapping.

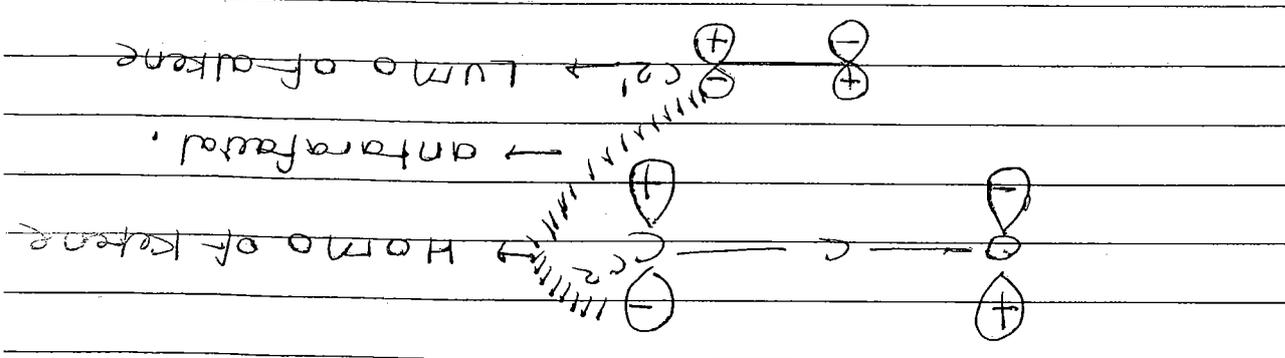
In an antarafacial sense of the ketene

FMO method for [2+2] cycloaddition

The FMO treatment shows that the bond formation between C-1 & C-1' develops mainly from the interaction of the LUMO of ketene and the bond between C-2 & C-2' develops mainly from the interaction of HOMO ketene (ψ₂) and LUMO of the alkene.

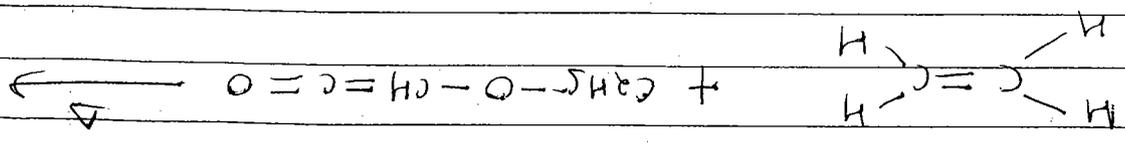


Bond formation betn C-1 of ketene & C-1' of alkene



Bond formation between C-2 of ketene & C-2' of alkene.

The reaction can be represented as follows



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25
20
15
10

