

# Divisibility

What exactly does it mean?

# “Divisible by” means...

- If you divide one number by another, the result is a whole number **WITHOUT** a remainder.
- Examples:
  - 12    6 = 2  
No remainder, so 12 is divisible by 6.
  - 15    5 = 3  
No remainder, so 15 is divisible by 3.

# “Divisible by” means...

- Another way of saying this is that every whole number is divisible by its factors.
  - Ex. The factors of 12 are 1, 2, 3, 4, 6, 12
- Every number is divisible by itself and by 1, but most numbers are also divisible by other factors.

# Ch. 1.1

Divisibility by 2, 5, and 10.



# Divisibility Rules (2)

- A number can be divided by 2 if
  - the last digit is even (0, 2, 4, 6, 8)



# Divisibility Rules (5)



- A number is divisible by 5 if
  - the last digit is a 5 or a 0

# Divisibility Rules (10)

- A number can be divided by 10 if
  - the last digit is a 0





# Ch. 1.2

Divisibility by 3 and 9.



# Divisibility Rules (3)



- a number is divisible by 3 if
- the sum of the digits is 3 or a multiple of 3



# Divisibility Rules (9)



- A number is divisible by 9 if
- the sum of all the digits will add to 9 or a multiple of 9



# Check Divisibility (9)



a) 627

b) 3278

c) 4002

d) 37782



# Regrouping to show Divisibility

- One way to help show divisibility is to regroup the number using place value charts.
- This sometimes makes it clear whether the number is divisible.
- Ex.  $1240 =$ 
  - 124 tens + 0 ones
- Ex.  $52\,255 =$ 
  - 52 thousands + 2 hundreds + 5 tens + 5 ones

# Ch. 1.3

Divisibility by 6.

# Divisibility Rules (6)

- A number can be divided by 6 if
- the last digit is even **and** the sum of all the digits is 3 or a multiple of 3.



# Divisibility Rules (6)

- In other words, it must be divisible by both:
- 2 and 3





# Check Divisibility (6)

- a) 348
- b) 2987
- c) 5630
- d) 46 524



# Ch. 1.4

Divisibility by 4 and 8.

# Divisibility Rules (4)



- a number is divisible by 4 if
  - the number made by the last two digits can be divided by 4



# Check Divisibility (4)



a) 3466

b) 1288

c) 39804

d) 64 684



# Divisibility Rules (8)

- A number is divisible by 8 if
- the number made by the last three digits will be divisible by 8



# Check Divisibility (8)

- a) 3466
- b) 1288
- c) 39804
- d) 64 684



Ch. 1.1 – 1.4

Divisibility Rules Review

# Divisibility Rules Review

- 2, the last digit will be an even number
- 3, all the digits will add to a multiple of 3
- 4, the number made by the last two digits can be divided by 4
- 5, the last digit will be a 5 or 0



# Divisibility Rules Review

- 6, the last digit will be even (rule for 2) and the digits will add to a multiple of 3
- 8, the number made by the last three digits will be divisible by 8

# Divisibility Rules Review

- 9, the sum of the digits will be 9 or a multiple of 9
- 10, the last digit will be a 0
- There is no easy test for 7. Although some methods have been invented, however it is easier to simply do the regular division.

# Divisibility Rules

➤ Apply divisibility rules to these numbers:

a) 74,673,042

b) 444,555,448

c) 61,616,168

d) 732,510

e) 66,666,666

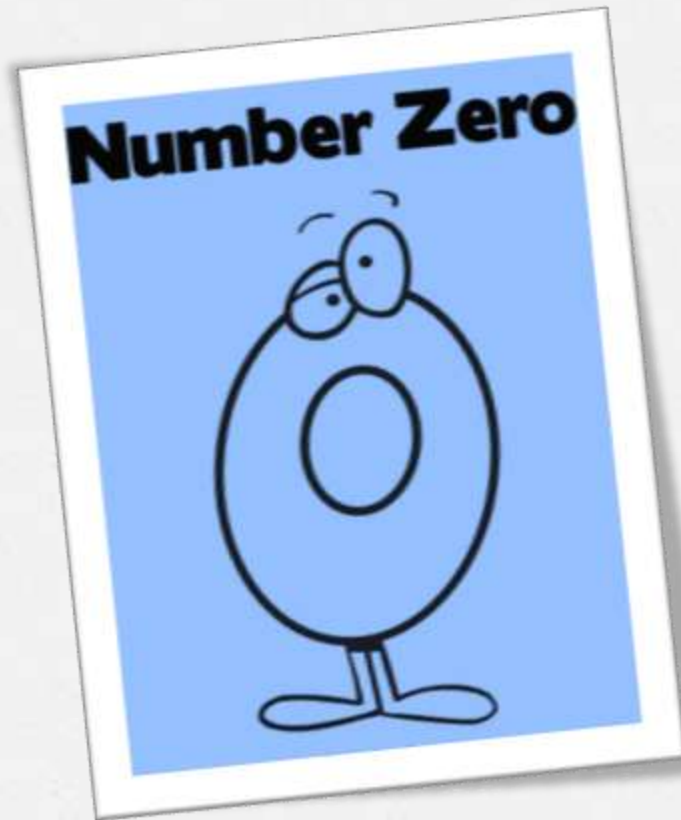
f) 179,131,590

# Ch. 1.5

## Divisibility by 0

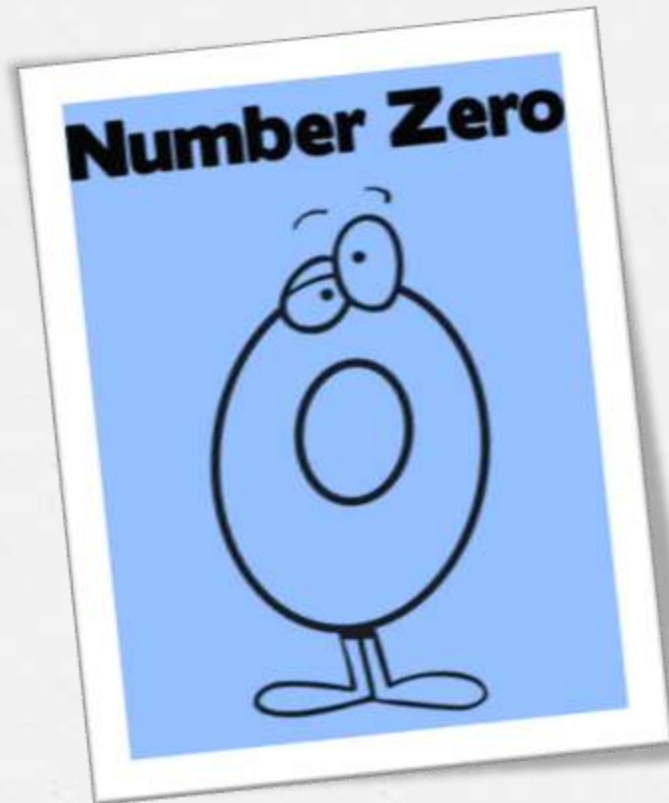


# Why can't you divide by zero?



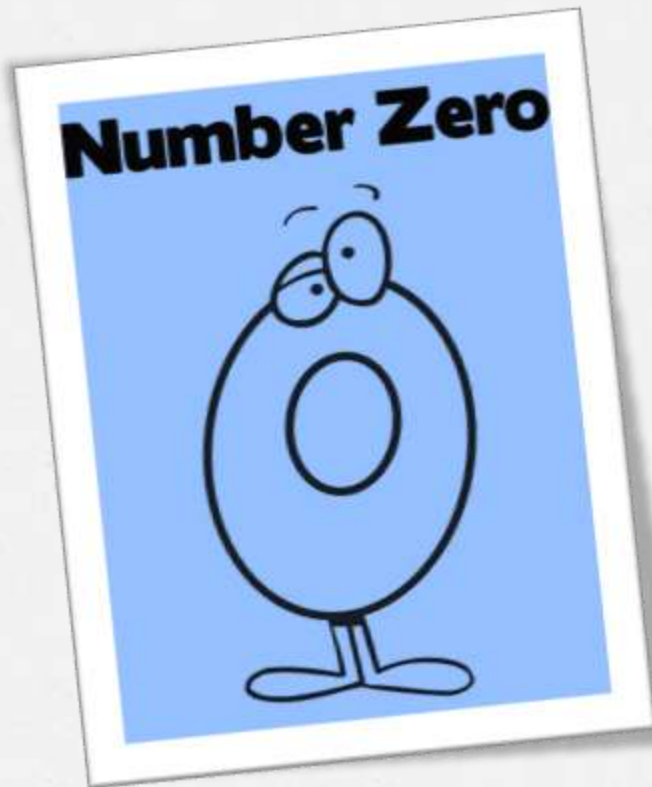
- $12 \div 4 = 3$
- $4 \times 3 = 12$
  
- $12 \div 0 = ?$
- $? \times 0 = 12$
  
- What  $x 0 = 12$ ? Is there any answer?
- What does your calculator say?

# Why can't you divide by zero?



- Or, another way to think of it:
- $12 \div 4 = 3$  means 12 divided into groups of 4 gives 3 groups of 4.
- $12 \div 0 = ?$  Means 12 divided into ? groups of 0.
- How many groups of 0 do you need to equal 12?

# Why can't you divide by zero?



- Or, another way to think of it:
- What is...
  - $12 \div 0.1$ ?
  - $12 \div 0.01$ ?
  - $12 \div 0.001$ ?
  - $12 \div 0.000001$ ?
  - $12 \div 0.00000001$ ?
- As you divide by numbers closer and closer to zero, what happens to the answer?