

B.sc I

Material Balance and process calculation

P-II

Semester - I

## Unit and Dimensions

A Unit is an arbitrarily selected standard of measure for physical quantity.

physical quantity that can be measured is always expressed as a product of its numerical value and units

physical quantity divided in two groups

- fundamental/basic such as length, mass, time
- derived quantities such as area, velocity and acceleration

system units divided as

- Base unit - These units for basic quantities such as length, mass, time etc.
- Derived unit : These are units obtained by multiplying and dividing base units eg.  $\text{cm}^2$ ,  $\text{m/s}$ , etc.
- multiple units : These are units which are multiple or fractions of base units eg. hour, minute, second etc.

### Unit systems

Various systems of units and basic quantities associated with them as given below

Fundamental quantity	System or units				Dimension
	SI	MKS	CGS	FPS	
Length	meter (m)	meter (m)	centimeter (cm)	foot (ft)	L
Mass	kilogram (kg)	kilogram (kg)	gram (g)	pound (lb)	M
Time	s	s	s	s	T
Temperature	kelvin (K)	celsius (°C)	celsius (°C)	fahrenheit (°F)	T



Derived units

The derived units are obtained from the base or fundamental unit using certain laws or definitions.

ex. ① Volume is a products of three lengths

Therefore unit of length is m

$$V = l \times l \times l = l^3 = \text{Unit is } m^3$$

② pressure is defined as force per unit area

$$P = \frac{F}{A} = \frac{\text{force}}{\text{area}} = \frac{N}{m^2}$$

Unit of pressure =  $N/m^2$

Derived Quantity	Units	System of Units	Dimensions
Volumetric flow rate	Cubic meters per hour ( $m^3/h$ )	SI	$L^3 \theta^{-1}$
	Cubic centimeters per second ( $cm^3/s$ )	MKS	$L^3 \theta^{-1}$
Volume	Cubic meters ( $m^3$ )	SI	$L^3$
	Litres (l)	MKS	$L^3$
Density	Kilograms per cubic meter ( $kg/m^3$ )	SI	$ML^{-3}$
	Grams per cubic centimeter ( $g/cm^3$ )	MKS	$ML^{-3}$
	Grams per millilitre ( $g/ml$ )	CGS	$ML^{-3}$
Force	Newtons (N)	SI	$ML \theta^{-2}$
	Dynes (Dyne)	CGS	$ML \theta^{-2}$
	Kilogram force (kgf)	MKS	F
Pressure	Newtons per square meter (Pascals) [ $N/m^2$ , (Pa)]	SI	$ML^{-3} \theta^{-2}$
	Kilograms force per square centimeter ( $kgf/cm^2$ )	MKS	$FL^{-2}$
Work / Energy	Joules (J)	SI	$ML^2 \theta^{-2}$
	Meters kilogram force (m.kgf)	MKS	MF
	Ergs (erg)	CGS	$ML^2 \theta^{-2}$
Heat / Enthalpy	Joules (J)	SI	$ML^2 \theta^{-2}$
	Kilocalories (kcal)	MKS	$ML^2 \theta^{-2}$
	Calories (cal)	CGS	$ML^2 \theta^{-2}$
Mass flow rate	Kilograms per hour (kg/h)	SI	$M \theta^{-1}$
Heat capacity	Joules per kilogram per degree Kelvin [ $J/(kg \cdot K)$ ]	SI	$L^2 \theta^2 T^{-1}$
	Kilocalories per kilogram per degree Celsius [ $kcal/(kg \cdot deg C)$ ]	MKS	$L^2 \theta^2 T^{-1}$
Molar heat capacity	Joules per kilogram mole per degree Kelvin [ $J/(kmol \cdot K)$ ]	SI	$ML^2 \theta^{-2} n^{-1} T^{-1}$
	Kilocalories per kilogram mole per degree Celsius [ $kcal/(kmol \cdot deg C)$ ]	MKS	$ML^2 \theta^{-2} n^{-1} T^{-1}$

## Force

force is proportional to the product of mass and acceleration

$$F \propto m \cdot a$$

$$F = k \cdot m \cdot a$$

Unit is Newton

work - is defined as product of the force acting on a body and distance travelled by the body in the direction of the applied force

$$W = F \cdot X \cdot L$$

$$= \text{kg} \cdot \text{m} \cdot \text{s}^{-2}$$

$$= \text{m} \cdot \text{kg} \cdot \text{s}^{-2}$$

## Some prefixes for the S I Units

- |                    |               |           |
|--------------------|---------------|-----------|
| 1) giga (G)        | - multiply by | $10^9$    |
| 2) mega (M)        | - multiply by | $10^6$    |
| 3) kilo (K)        | - multiply by | $10^3$    |
| 4) milli (m)       | - multiply by | $10^{-3}$ |
| 5) micro ( $\mu$ ) | - multiply by | $10^{-6}$ |
| 6) nano (n)        | - multiply by | $10^{-9}$ |
| 7) deci (d)        | - multiply by | $10^{-1}$ |
| 8) deka (da)       | - " -         | $10^1$    |
| 9) hecto (h)       | - " -         | $10^2$    |
| 9) centi (c)       | - " -         | $10^{-2}$ |



## Conversion of Unit.

It is often necessary to convert a physical quantity from one system of Unit to another.

example

Area  $ft^2 \rightarrow m^2$

multiply by  
0.0929  
 $10^{-4}$

$cm^2 \rightarrow m^2$

Volume

$ft^3 \rightarrow m^3$

$10^{-6}$

Velocity  $ft/s \rightarrow m/s$

0.3048

mass

$lb \rightarrow kg$

0.4536

## Conversion factors to SI units :

To convert from	To	Multiply by
1. Length, L :		
ft	m	0.3048
cm	m	0.01
in	mm	25.4
in	m	0.0254
2. Area, L <sup>2</sup> :		
ft <sup>2</sup>	m <sup>2</sup>	0.0929
cm <sup>2</sup>	m <sup>2</sup>	10 <sup>-4</sup>
3. Volume, L <sup>3</sup> :		
ft <sup>3</sup>	m <sup>3</sup>	0.02832
cm <sup>3</sup>	m <sup>3</sup>	10 <sup>-6</sup>
l	m <sup>3</sup>	10 <sup>-3</sup>
4. Velocity, L/θ :		
ft/s	m/s	0.3048
ft/h	m/s	8.467 × 10 <sup>-5</sup>
5. Volumetric flow rate, L <sup>3</sup> /θ		
ft <sup>3</sup> /s	m <sup>3</sup> /s	0.02832
ft <sup>3</sup> /h	m <sup>3</sup> /s	7.867 × 10 <sup>-6</sup>
l/h	m <sup>3</sup> /s	2 × 10 <sup>-7</sup>
l/s	m <sup>3</sup> /s	10 <sup>-3</sup>
6. Mass, M :		
lb	kg	0.4536
t	kg	1000
g	kg	10 <sup>-3</sup>
7. Density, M/L <sup>3</sup> :		
lb/ft <sup>3</sup>	kg/m <sup>3</sup>	16.019
g/cm <sup>3</sup>	kg/m <sup>3</sup> = g/l	1000
8. Mass flow rate, M/θ :		
lb/s	kg/s	0.4536
lb/h	kg/s	1.26 × 10 <sup>-4</sup>
9. Force, F :		
lbf	N	4.448
kgf	N	9.807
dyn	N	10 <sup>-5</sup>
10. Pressure, F/L <sup>2</sup> :		
lbf/ft <sup>2</sup>	N/m <sup>2</sup> = Pa	47.88
std. atm	N/m <sup>2</sup> = Pa	1.01325 × 10 <sup>5</sup>
std. atm	kPa	101.325
in Hg	N/m <sup>2</sup> = Pa	3.386
in H <sub>2</sub> O	N/m <sup>2</sup> = Pa	249.1
dyn/cm <sup>2</sup>	N/m <sup>2</sup> = Pa	10 <sup>-1</sup>
mmHg	N/m <sup>2</sup> = Pa	133.3
torr	N/m <sup>2</sup> = Pa	133.3
bar	N/m <sup>2</sup> = Pa	10 <sup>5</sup>
kgf/cm <sup>2</sup>	N/m <sup>2</sup> = Pa	9.808 × 10 <sup>4</sup>



i. Energy, work, heat, FL :		
cal	N·m = J	4.187
Btu	N·m = J	1055
kcal	N·m = J	4187
erg	N·m = J	$10^{-7}$
kW·h	N·m = J	$3.6 \times 10^6$
Enthalpy, FL/M :		
Btu/lb	(N.m)/kg = J/kg	2326
cal/g	(N.m)/kg = J/kg	4187
kcal/kg	(N.m)/kg = J/kg	4187
Molar enthalpy, FL/mole		
Btu/lbmol	(N.m)/mol = J/mol	2326
cal/mol	(N.m)/mol = J/mol	4187
Heat capacity, specific heat, FL/MT :		
Btu/(lb · °F)	N.m/(kg·K) = J/(kg·K)	4187
cal/(g · °C)	N.m/(kg·K) = J/(kg·K)	4187
Molar heat capacity, FL/mole T :		
Btu/(lbmol · °F)	N.m/(kmol·K) = J/(kmol·K)	4187
cal/(mol · °C)	N.m/(kmol·K) = J/(kmol·K)	4187
Energy flux, FL/L <sup>2</sup> θ :		
Btu/(ft <sup>2</sup> · h)	N.m/(m <sup>2</sup> · s) = W/m <sup>2</sup>	3.155
cal/(cm <sup>2</sup> ·s)	N.m/(m <sup>2</sup> · s) = W/m <sup>2</sup>	$4.187 \times 10^4$
Power, FL/θ		
(ft·lbf)/s	(N.m)/s = W	1.356
hp	(N.m)/s = W	745.7
Btu/h	(N.m)/s = W	0.2931
kcal/h	(N.m)/s = W	1.163
Viscosity, M/Lθ		
P [poise ≡ g/(cm.s)]	kg/(m.s) = (N.s)/m <sup>2</sup>	0.10
cP	kg/(m.s) = (N.s)/m <sup>2</sup>	0.001
	= Pa·s	
lb/(ft.s)	kg/(m.s)	1.488

While writing the units of fundamental or derived quantities, please remember the following :

Correct : 10 kgf·m

incorrect : 10 kgfm

... two unit symbols should be separated by dot or space

Correct : 10 kg

incorrect : 10 kgs

... no plural form of the unit symbol

Correct : 10 cm

incorrect : 10 cm.

... no period/full stop at the end of the unit symbol

Correct : 10000 W/(m<sup>2</sup>·K)

incorrect : 10000 W/m<sup>2</sup>·K

Correct : 10 kW

incorrect : 10 k W

... no space between the prefix symbol and the unit symbol

P A force of 19.635 kgf is applied on a piston of diameter 5 cm. Find the pressure exerted on the piston in Kpa

$$P = F/A$$

$$A = \frac{\pi d^2}{4}$$

$$A = \frac{\pi (5)^2}{4}$$

$$A = \frac{22.7 \times 25}{4} \\ = 19.635 \text{ cm}^2$$

$$P = \frac{19.635}{19.635} = 1 \text{ kgf/cm}^2$$

$$= 1 \times \frac{100000}{1.033227} \left[ \frac{\text{Kpa}}{\text{kgf/cm}^2} \right]$$

$$= 98.066 \text{ Kpa}$$

Pressure - pressure is defined as force per unit area

$$P = \frac{F}{A} = \frac{\text{force}}{\text{Area}} = \frac{\text{N}}{\text{m}^2} (\text{Pa}) \text{ - SI}$$

$$= \frac{\text{kgf}}{\text{cm}^2} \text{ - MKS}$$

Types of pressure

- 1) atmospheric pressure
- 2) Gauge pressure (g)
- 3) Absolute pressure
- 4) Vacuum pressure

atmospheric pressure - The atmospheric pressure is the pressure that an area experiences due to the force exerted by atmosphere

$$1 \text{ atm} = 101.325 \text{ Kpa} \\ = 101325 \text{ N/m}^2 \text{ or Pa}$$



or  $1.033 \text{ kgf/m}^2$  — MKS

Gage pressure  $\rightarrow$  is the pressure relative to the atmospheric pressure. In other words, how much above or below is the pressure with respect to with respect to the atmospheric pressure.

Absolute pressure — is the sum of atmospheric pressure and the gage pressure

- If the gage pressure has a positive value the absolute pressure will be greater than the atmospheric pressure.
- If the gage pressure has a -ve value the absolute pressure will be less than the atmospheric pressure.
- it is also called as actual pressure
- Absolute pressure = Atmospheric pressure - Vacuum
- Absolute pressure = Atmospheric pressure + gage pressure

Vacuum pressure —

The pressure below the atmospheric pressure are called vacuum pressure measured by vacuum gauge

it is usually expressed in mmHg or (torr)

p. In a multiple effect evaporator system, the second effect is maintained under vacuum of 475 mmHg (torr), find the absolute pressure in kpa

$$\text{Absolute pressure} = \text{atmospheric pressure} - \text{Vacuum}$$

$$= 760 \text{ mmHg} - 475$$

$$= 285 \text{ torr (mmHg)}$$

$$= 285 \text{ mmHg}$$

$$1 \text{ atm} = 101.325 \text{ kpa}$$

$$= \frac{285 \times 101.325}{760} = 38 \text{ kpa}$$

OR

mmHg converted to Pa multiply by 133.3

there for

$$= 285 \times 133.3 = 37990.5 \text{ pa}$$

$$= \frac{37990}{1000} = 37.99$$

$$= 38 \text{ kpa}$$



- ③ The force of 19.635 kgf is applied to piston of diameter 5 cm. Find the pressure exerted on the piston kpa

$$P = \frac{F}{A}$$

$$A = \frac{\pi}{4} \times d^2$$

$$A = \frac{\pi}{4} \times (5)^2$$

$$A = 19.635 \text{ cm}^2$$

$$P = \frac{19.635}{19.635} = 1 \text{ kgf/cm}^2$$

∴ kgf/cm<sup>2</sup> is converted in kpa then multiply by  $\frac{9.808 \times 10^4}{1000}$

$$1 \times \frac{9.808 \times 10^4}{10^3} =$$

$$1 \times 9.808 \times 10 = 98.080 \text{ kpa}$$

- ④ Convert pressure of 2 atm to mm Hg

$$1 \text{ atm} = 760 \text{ mm Hg}$$

$$2 \times 760 = 1520 \text{ mm Hg.}$$

5) Convert Volumetric flow rate to  $2 \text{ m}^3/\text{s}$  to  $\text{l/s}$

Soln

$$1 \text{ m}^3 = 1000 \text{ l}$$

$\therefore \text{m}^3/\text{s}$  convert to  $\text{l/s}$  multiplied by  $10^3$

$$2 \times 1000 = 2000 \text{ l/s.}$$

6) Convert  $2000 \text{ W}$  in  $\text{HP}$  — Unit of power

Conversion factor for

$$\text{HP} \text{ — } \text{W (N.m/s)}$$

$$\text{HP} \times 745.7 = \text{W}$$

$$\therefore \text{HP} = \frac{2000}{745.7} = 2.68 \text{ HP.}$$

7) Convert  $1000 \text{ dyn}$  to Newton — (force.)

Conversion factor

$$\text{dyn} \text{ — } \text{N}$$

$$\text{dyn} \times 10^{-5} = \text{N}$$

$$1000 \times 10^{-5} = \text{N}$$

$$0.01 = \text{N}$$

8) Convert  $1400 \text{ mm Hg}$  to  $\text{atm}$  — (Pressure)

Soln

$$\text{atm} \times 760 \text{ mmHg} = 1400 \text{ mmHg}$$

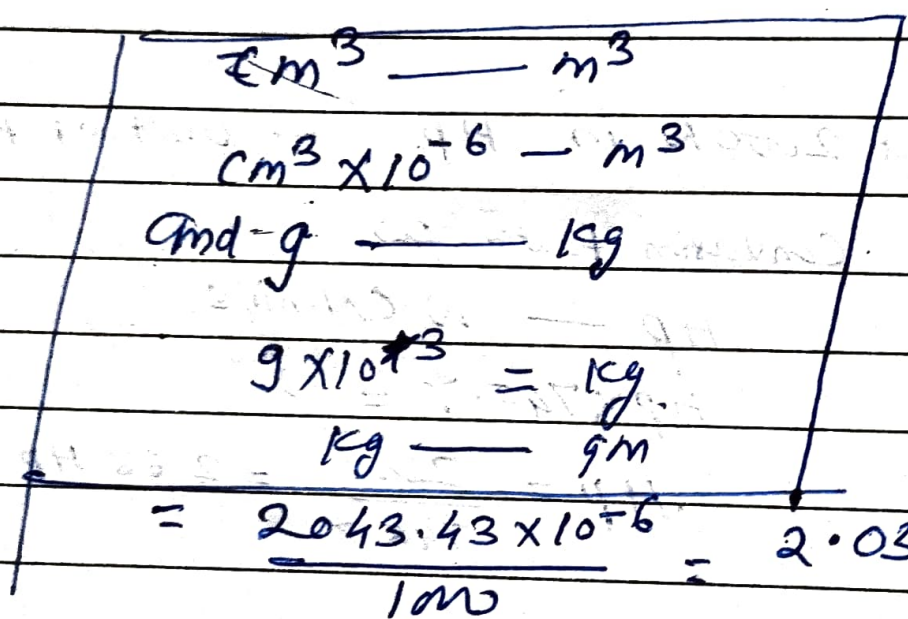
$$\text{atm} = \frac{1400}{760} = 1.842 \text{ atm}$$



Convert  $127 \text{ lb/ft}^3$  to  $\text{g/cm}^3$  — Density  
 $16 \text{ ft}^3$  to  $1 \text{ m}^3$  mult. by  $\approx 16.019$   
 $127 \times 16.019 = 1 \text{ m}^3$

$$= 2043.43 \text{ kg/m}^3$$

$$= 2043.43 \text{ kg/m}^3$$



mean.

$$\frac{\text{kg}}{\text{m}^3} \longrightarrow \frac{\text{g}}{\text{cm}^3} \text{ multiplied by } 10^{-3}$$

Basic chemical calculationGram atom

It is defined as the mass in gram of an element which is numerically equal to its atomic weight

Gram atoms of an element

$$= \frac{\text{Weight in gram of an element}}{\text{atomic weight}}$$

Gram atom of element A

$$= \frac{\text{Weight in gram of A}}{\text{atomic weight of A}}$$

Kilogram atom of element A

$$= \frac{\text{Weight in kilogram of A}}{\text{atomic weight of A}}$$

Gram mole: It is defined as the mass in gram of a substance that is equal to numerically to its molecular weight.

Gram mole of comp B

$$= \frac{\text{Weight in gram of B}}{\text{molecular weight of B}}$$

Similarly kilogram mole of B

$$= \frac{\text{Weight in kilogram of B}}{\text{molecular wt of B}}$$



p. Calculate the kilogram atom of carbon which weight 36 kg.

Base kg of carbon 36

Atomic weight of carbon = 12

$$\text{K atom of carbon} = \frac{\text{Weight in kg of carbon}}{\text{Atomic weight of carbon}}$$

$$= \frac{36}{12} = 3$$

p. Calculate the kilogram of 'Na' which the amount is specified as 3 k atom

soln

3 k atom 'Na'

Atomic weight of Na = 23

$$\text{K atom of Na} = \frac{\text{kg of Na}}{\text{Atomic weight of Na}}$$

Atomic weight of Na

$$3 = \frac{\text{kg of Na}}{23}$$

23

$$\text{kg of Na} = 23 \times 3 = 69 \text{ Ans}$$

p. find the molecular weight

1)  $\text{H}_2\text{SO}_4$  2)  $\text{Na}_2\text{CO}_3$  3)  $\text{KMnO}_4$

$$\text{H}_2\text{SO}_4 = 2 \times 1 + 1 \times 32 + 4 \times 16 = 98$$

$$\text{Na}_2\text{CO}_3 = 2 \times 23 + 1 \times 12 + 3 \times 16 = 106$$

$$\text{KMnO}_4 = 1 \times 39 + 1 \times 55 + 4 \times 16 = 158$$

P How many Kilogram of ethane are there in 210 kmol

Base - 210 kmole ethane

$$\text{sol}^n \quad \text{K mole of ethane} = \frac{\text{Weight of Kg in ethane}}{\text{molecular wt of ethane}}$$

$$210 = \frac{\text{Weight in Kg of ethane}}{\text{mol. wt of ethane}}$$

mol. wt of ethane

$$= \text{C}_2\text{H}_6 = 2 \times 12 + 6 \times 1 = 30$$

$$210 = \frac{\text{Weight in kg of ethane}}{30}$$

$$210 \times 30 = \text{Weight in kg of ethane}$$

$$6300 =$$

P Convert 88 kg of carbon dioxide into its amount in ~~mole~~

molar units

soln Basis 88 kg of  $\text{CO}_2$

$$\text{mol. wt of } \text{CO}_2 = 12 + 16 \times 2 = 44$$

$$\text{K mole of } \text{CO}_2 = \frac{\text{kg of } \text{CO}_2}{\text{mol. wt of } \text{CO}_2}$$

$$= \frac{88}{44} = 2$$

$$= 2 \text{ K mole of } \text{CO}_2$$



P. Find mole of oxygen present for 500 gm

Basis - 500 gm of oxygen

$$\text{moles of } O_2 = \frac{\text{Weight of } O_2}{\text{mol. wt of } O_2}$$

$$= \frac{500}{32} = 16.625 \text{ mol.}$$

P. convert 499 gm of  $CuSO_4 \cdot 5H_2O$  into moles

Soln mol. wt of  $CuSO_4$

$$= Cu = 63.5, S = 32, O = 16$$

$$CuSO_4 \cdot 5H_2O = 63.5 + 32 + 64 + 5(2 + 16)$$

$$= 249.5$$

$$\text{moles of } CuSO_4 \cdot 5H_2O = \frac{499}{249.5} = 2 \text{ mol.}$$

## Normality

Number of gram-equivalent of solute dissolved in 1 lit of solution

it is denoted by (N)

$$\text{Normality} = \frac{\text{gram-equivalent of solute}}{\text{Volume of solution in lit}}$$

## Molarity

Number of gram moles of solute dissolved in one litre of solution

it is denoted by M

$$M = \frac{\text{gm moles of solute}}{\text{Volume of solution in litres}}$$

## Molality

it is defined as number of gram moles of solute dissolved in one kilogram of solvent

$$\text{molality} = \frac{\text{gm moles of solute}}{\text{mass of solvent in kg}}$$

$$\text{Concentration} = \text{Normality} \times \text{equivalent weight}$$

equivalent weight : It is defined as the ratio of the atomic weight or molecular weight to its valence.

The valence of an element or a compound depends on number of Hydroxyl ions ( $\text{OH}^-$ ) donated or Hydrogen ions  $\text{H}^+$  accepted for each atomic weight or molecular weight

$$\text{equivalent weight} = \frac{\text{molecular weight}}{\text{valence}}$$



Q 98 gm of Sulphuric Acid ( $H_2SO_4$ ) are dissolved in water to prepare 1 lit of solution. Find Normality and Molarity.

Soln Amount  $H_2SO_4$  dissolved = 98 gm  
 mol. wt of  $H_2SO_4$  = 98 gm

$$\begin{aligned} \text{equivalent weight of } H_2SO_4 &= \frac{\text{mol. wt}}{\text{valence}} \\ &= \frac{98}{2} = 49 \end{aligned}$$

$$\begin{aligned} \text{gm. equivalent of } H_2SO_4 &= \frac{\text{mole}}{\text{Weight of } H_2SO_4} \\ &\quad \frac{\text{equivalent weight}}{\text{equivalent weight}} \\ &= \frac{98}{49} = 2 \\ &\quad \text{gm of equivalent} \end{aligned}$$

$$\text{Normality} = \frac{2}{1} = 2$$

$$\text{molarity} = \frac{\text{gm moles of solute}}{\frac{\text{molecular weight}}{\text{Volume of solution in lit}}}$$

$$\begin{aligned} \text{gm moles solute} &= \frac{\text{Weight of substance}}{\text{molecular weight}} \\ &= \frac{98}{98} = 1 \end{aligned}$$

$$M = \frac{1}{1} = 1$$

p2) 20 gm of caustic soda is dissolved in water to prepare 500 ml solution find normality and molarity

sol<sup>n</sup> -

Amount of caustic soda = 20 gm

molecular weight = 40

equivalent weight =  $\frac{\text{mol. wt}}{\text{valence}} = \frac{40}{1} = 40$

Volume of sol<sup>n</sup> in lit = 500 ml

=  $\frac{500}{1000} = 0.5 \text{ lit.}$

Normality =  $\frac{\text{gm. equivalent NaOH}}{\text{Volume of sol<sup>n</sup> in lit}}$

gm. eq. of NaOH =  $\frac{20}{40} = 0.5 \text{ gmeq.}$

=  $\frac{0.5}{0.5} = \underline{\underline{1}}$

molarity =  $\frac{\text{gram mole of NaOH}}{\text{Volume of sol<sup>n</sup> in lit}}$

gram moles of NaOH =  $\frac{\text{Weight of substance}}{\text{molecular weight}}$

=  $\frac{20}{40} = 0.5$

molarity =  $\frac{0.5}{0.5} = \underline{\underline{1}}$



p. Find gram of HCl needed to prepare 1 lit 2N HCl solution.

Basis 1 lit 2N HCl soln

$$\text{Normality} = \frac{\text{gram eq. of HCl}}{\text{Volume of solution lit}}$$

$$2 = \frac{\text{gm eq of HCl}}{1}$$

$$\text{Equivalents of HCl} = 2 \text{ gm-eq}$$

$$\text{gm equivale} = \frac{\text{Weight of substance}}{\text{Equivalent weight}}$$

$$2 = \frac{36.5}{\text{Weight of substance}}$$

$$36.5 \times 2 = \text{Weight of substance}$$

$$73 \text{ gm} = \text{''}$$

p. The concentration of an aqueous solution of acetic acid is specified as 30% on weight basis. Find the molality of solution.

Basis 100 kg of solution

Amount of Acetic Acid in it = 30 kg

Amount of Water solvent = 70 kg.

Amount of acetic acid in gm =  $30 \times 10^3 \text{ gm}$

molecular weight of  $\text{CH}_3\text{COOH} = 60$

gm. moles of Acetic acid =  $\frac{\text{Weight of acid}}{\text{mol. wt}}$   
 $= \frac{30 \times 10^3}{60} = 500$  ~~moles~~ mole

Molality of solution =  $\frac{\text{moles of acetic acid}}{\text{kg of solvent}}$   
 $= \frac{500}{70} = 7.142$

p- A solution of caustic soda contain 20% NaOH taking density of the solution 1.196 kg/l find normality, Molarity and molality of solution

Solution → Volume of soln - 100 kg.

The solution contain 20% NaOH.

means

20 kg of NaOH  
and 80 kg of solvent

Density = 1.196 kg/lit

Normality of NaOH =  $\frac{\text{gm equivalent}}{\text{Volume of soln in Lit}}$

gm. equivalent of NaOH =  $\frac{\text{Mol wt of substance}}{\text{equivalent wt}}$

$= \frac{20 \text{ kg}}{40} = 0.5$

$= \frac{20 \times 10^3}{40} = 500$  ~~moles~~



∴ Volume of solution is 100 cc It is convert into litre

$$\therefore \text{density} = \frac{\text{mass}}{\text{Volume}}$$

$$\text{Volume} = \frac{\text{mass}}{\text{density}} = \frac{100 \text{ kg}}{1.196 \text{ kg/litre}}$$

$$= \underline{\underline{83.61 \text{ litre}}}$$

$$\text{Normality} = \frac{500}{83.61} = 5.98$$

$$\text{Normality} = \text{molarity} = 5.98$$

∴ mol. wt = eq. wt of NaOH.

$$\text{Molarity} = \frac{\text{gram mole of NaOH}}{\text{kg of solvent}}$$

$$= \frac{500}{80} = 6.25 \text{ mol/kg.}$$

p.  $\text{H}_2\text{SO}_4$  solution has a molarity 11.24 and molality of 94. calculate the density of solution

soln consider soln is 1 ltr

$$\text{Given molarity} = 11.24$$

$$\text{molality} = 94$$

$$\text{molarity} = \frac{\text{gm moles of } H_2SO_4}{\text{Volume of soln in ltr}} = \frac{11.24}{1} = \frac{\text{gm. M}}{1}$$

$$11.24 = \frac{\text{gm moles of } H_2SO_4}{1}$$

$$= 11.24$$

~~Weight of substance =~~

$$\text{gm mole of } H_2SO_4 = \frac{\text{Weight of substance}}{\text{molecular weight}}$$

$$11.24 \times 98 = \text{Weight of substance}$$

$$1101.52 \text{ gm} = \text{Weight of substance}$$

$$1.101 \text{ gm/kg} = \text{substance weight}$$

$$\text{Molarity} = \frac{\text{gm-moles of substance}}{\text{Volume of solvent in kg.}}$$

$$94 = \frac{11.24}{\text{Volume of solvent in kg.}}$$

$$\text{Volume of solvent in kg} = \frac{11.24}{94} = 0.1195 \text{ kg}$$

$$\text{Amount of solution} = 1.101 + 0.1195$$

$$= 1.2205 \text{ kg.}$$

$$\text{Density} = \frac{\text{Mass}}{\text{Volume}} = \frac{1.2205}{1}$$

$$= 1.2205 \text{ kg/lit.}$$



## Method of expressing the composition of mixtures and solution.

The composition of mixture or solution can be expressed in weight percent, volume percent and mole percent.

The composition of solid and liquid is expressed in terms of weight percent and mole percent.

The composition of gases is expressed in terms of volume percent.

### Weight percent:

It is the weight of any component expressed as percentage of total weight of the system.

$$\text{Weight \% of A} = \frac{\text{Weight of A}}{\text{Total weight of system}} \times 100$$

$$= \frac{W_A}{W} \times 100$$

$W = W_A + W_B$  — weight of system

$W_A =$  weight of component 'A'

### Volume percent

It is a pure component volume of any component expressed as a percentage of the total volume of the system

$$\text{Volume \% of A} = \frac{\text{Pure component volume of A}}{\text{Total volume of system}} \times 100$$

$$= \frac{V_A}{V} \times 100$$

$V_A =$  pure component volume of A

$V =$  Total volume of system  $V_A + V_B$

Mole percent:

It is mole of component expressed as a percentage of the total moles of the system

$$\text{mole \% of A} = \frac{\text{moles of A}}{\text{Total moles of system}} \times 100$$

$$= \frac{W_A}{M_A} \times 100$$

$$\frac{W_A}{M_A} + \frac{W_B}{M_B}$$

Where  $M_A$  and  $M_B$  are the molecular weights of component A & B respectively.

Mole fraction:

It is the ratio of the number of moles of a particular component to the total moles of system for binary system A and B

$$\text{mole fraction of A} = \frac{\text{Moles of A}}{\text{Total moles of system}}$$

$$X_A = \frac{W_A}{M_A} \div \left( \frac{W_A}{M_A} + \frac{W_B}{M_B} \right) \quad \text{--- (1)}$$

$$X_A = \text{mole fraction of A}$$

$$X_B = \text{mole fraction of B}$$



$$X_B = \frac{W_B}{M_B}$$

②

$$\frac{W_A}{M_A} + \frac{W_B}{M_B}$$

mole % of A = mole fraction A  $\times 100$

adding ① and ② we get

$$X_A + X_B = \frac{W_A}{M_A} + \frac{W_B}{M_B}$$

$$= \frac{W_A + W_B}{M_A + M_B} = 1$$

Sum of mole fraction all the component present in a given system is equal to unity

$$\sum_{i=1}^n X_i = 1.0$$

Sum of all mole % for given system total a 100

Date \_\_\_\_\_

p. an aqueous soln of sodium chloride is prepared by dissolving 25 kg of sodium chloride in 100 kg water.

Determine (a) weight % and mole % composition of solution

Soln

Amount of solution

$$25 \text{ kg of NaCl} + 100 \text{ kg water} \\ = 125 \text{ kg}$$

$$\text{Weight \% of NaCl} = \frac{\text{kg of NaCl}}{\text{kg of solution}} \times 100$$

$$= \frac{25}{125} \times 100 = 20$$

$$\text{Weight \% H}_2\text{O} = \frac{100}{125} \times 100$$

$$= 80 \%$$

$$\text{Mol. wt of NaCl} = 58.5$$

$$\text{mol. wt of H}_2\text{O} = 18$$

$$\text{moles of NaCl} = \frac{25}{58.5} = 0.427 \text{ kmol}$$

$$\text{moles of H}_2\text{O} = \frac{100}{18} = 5.56 \text{ kmol}$$

$$\text{Total moles of solution} = 0.427 + 5.56 \\ = 5.987 \text{ kmol}$$



mole % of NaCl solution

$$= \frac{\text{Kmol NaCl}}{\text{Kmol. solution}} \times 100$$

$$= \frac{0.427}{5.987} \times 100$$

$$= 7.13$$

mole % H<sub>2</sub>O in solution

$$= 100 - \text{mole % NaCl}$$

$$= 100 - 7.13$$

$$= 92.87 \%$$

OR

$$= \frac{\text{K mole of H}_2\text{O}}{\text{K mole of solution}} \times 100$$

$$= \frac{5.56}{5.987} \times 100$$

$$= 92.87$$

p → Sodium chloride weighing 200 kg is mixed with 600 kg potassium chloride calculate the composition mix in (i) Weight % and (ii) mole %.

Soln

$$\text{Weight of NaCl in mixture} = 200 \text{ kg}$$

$$\text{Weight of KCl in mixture} = 600 \text{ kg}$$

$$\text{Total weight of mix} = 800 \text{ kg}$$

## Ideal gas Law

There are several ways to derive the Ideal Gas Law but the simplest way to use the three Simple gas Law

### Avogadro's Law

- State that Volume of a gas is directly proportional to the Number of moles.

$$V \propto n$$

Boyle's Law - State that the volume of a gas is inversely proportional to its pressure

$$V \propto \frac{1}{P}$$

### Charles's Law

State that the volume of a gas is directly proportional to its Kelvin temperature

$$V \propto T$$

We combine these three equation  
we get

$$V \propto \frac{nT}{P}$$

$$\therefore V = \frac{k n T}{P} \quad \text{K is proportionality constant}$$

We replace  $k$  with Universal gas constant

$$\text{We get } V = \frac{R n T}{P}$$



$$PV = nRT$$

P: absolute pressure kpa  
 V in m<sup>3</sup> and T - temp in Kelvin.  
 and n - k mole

$$\text{The unit of } R = \frac{\text{m}^3 \cdot \text{kpa}}{\text{kmol} \cdot \text{K}}$$

$$\text{value} = 8.31451$$

$$\text{Unit } R = \frac{\text{Kcal}}{\text{kmol} \cdot \text{K}} = 1.987$$

$$R = \frac{\text{J}}{\text{mol} \cdot \text{K}} = 8.31451$$

P. Calculate the volume occupied by 20kg of chlorine gas at a pressure of 100 kpa and 298 K (25°C)

sol

basis 20kg of Cl<sub>2</sub> gas

$$PV = nRT$$

$$V = \frac{nRT}{P}$$

$$V = \frac{n \times 8.31451 \times 298}{100}$$

$$n = \text{no. of moles} = \frac{\text{Weight of substance}}{\text{M.W.}}$$

$$= \frac{20}{71} = 0.2817 \text{ kmol}$$

$$= \frac{0.2817 \times 8.31451 \times 298}{100} = 6.98 \text{ m}^3$$

P. 15 kg of carbon dioxide is compressed at a temp of 303 K (30°C) to a volume of 0.5 m<sup>3</sup>. Calculate the pressure required for given duty. Assume ideal gas law is applicable.

soln 15 kg of CO<sub>2</sub>

$$PV = nRT$$

$$P = \frac{nRT}{V}$$

$$n = \text{no. of moles} = \frac{15}{44} = 0.341 \text{ kmol}$$

$$P = \frac{0.341 \times 8.31451 \times 303}{0.5}$$

$$= 1718.16 \text{ kPa}$$

P. 5 kg of oxygen containing is a closed container of volume 1 m<sup>3</sup> is heated without exceeding a pressure of 709.28 kPa. Calculate maximum Temp in gas attained.

Basis: 5 kg of oxygen

$$\text{m.w. weight } O_2 = 32$$

$$\text{moles of } O_2 = \frac{5}{32} = 0.1562 \text{ kmol}$$

$$PV = nRT$$

$$T = \frac{PV}{nR}$$

$$= \frac{709.28 \times 1}{0.1562 \times 8.31451} = 543.13 \text{ K}$$

$$= 543.13 \text{ K} - 273 = (273.13^\circ \text{C})$$



Calculate the weight of  $1 \text{ m}^3$  of chlorine gas at a temperature of  $298 \text{ K}$  ( $25^\circ \text{C}$ ) and pressure of  $101.325 \text{ kPa}$  ( $1 \text{ atm}$ )

Soln  $1 \text{ m}^3 \text{ Cl}_2 \text{ gas}$

$$PV = nRT$$

$$\therefore n = \frac{PV}{RT}$$

$$= \frac{101.325 \times 1}{8.31451 \times 298}$$

$$= 0.0409 \text{ kmol}$$

$$\text{no. moles} = \frac{\text{Weight of sub.}}{\text{mol. wt}}$$

$$\text{Weight of substance} = \text{no. moles} \times \text{mol wt}$$

$$= 0.0409 \times 71 = \underline{\underline{2.904 \text{ kg}}}$$

## Material balance with chemical Reaction

A chemical process is required to carry out of raw material into product effectively and economically. Material and energy balance calculation is required for desired product. It is help us (i) to evaluate specific consumption of material (ii) to evaluate losses of materials and energy (iii) to find out reason for malfunctioning of processing unit.

### **Outline of a Procedure for Material Balance Calculations :**

- (1) Assume a suitable basis of calculation such as quantity or flow rate of the entering or leaving stream. If basis is not specified in the statement of the problem, assume a new convenient basis (quantity or flow rate of a suitable stream of which the composition data is given).
- (2) Adopt weight units such as grams or kilograms in case of problems of processes without chemical reactions (i.e., wherein no chemical reactions occur) and adopt/use molar units such as gram moles or kilogram moles in case of problems of processes with chemical reactions, i.e., involving chemical reactions as far as possible for the purpose of simplification.
- (3) Draw a block diagram of the process wherein each operation is represented by a rectangular block wherein the input and output streams are represented by an inflow and outflow arrow.
- (4) In the block diagram drawn, indicate the information provided regarding the input and output streams given in the problem statement such as quantity, flow rate, composition, materials, etc.
- (5) Search out the unknown quantities or composition, flow rates, etc.
- (6) Search out the unknowns involved in the problem and ascertain them some  $x, y, z$ , etc. (depending upon a number of unknowns) and generate, with the help of data given, the material balance equations in terms of  $x, y, z$ , etc. equal to the number of unknowns. Equations can be generated (independent) by making the overall material balance and individual material balance of components involved and solve them.
- (7) In case of problems involving a chemical reaction, write a balanced chemical equation, search out a limiting component and so on - as the quantities produced during the chemical reaction or components reacted/consumed are to be calculated on the basis of the limiting reactant reacted and the chemical reaction under consideration.



Material balance

It means that

$$\text{Input} = \text{output}$$

ex. A is a solid

A input to the reactor = A output from the  
Reactor + A unreacted

or  
Accumulation

## Distillation:

This operation is used for the separation of the components of a liquid mixture by partial vaporization and condensation.

Distillation with rectification or (fractional distillation) gives almost pure product. The product removed from the top is called as distillate or overhead product and that removed from bottoms or bottom product, material is generally based on the more volatile component. The vapour phase is created by supplying thermal energy to the liquid to be distilled and this method of separation depends on the difference in vapour pressure of different components at a given temperature.

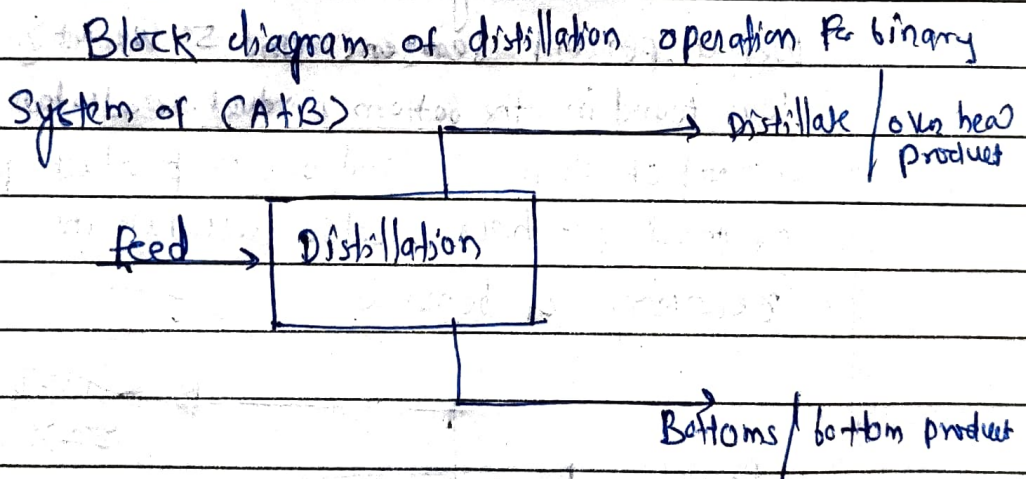


Fig. Distillation

## Overall material balance

$$\text{Feed} = \text{Distillate} + \text{Bottoms}$$

$$F = D + B$$

where  $F$  is feed to a distillate column

in  $\text{kg}$  or  $\text{kg/h}$



D is the distillate in kg or kg/h. and K bottom product in kg or kg/h.

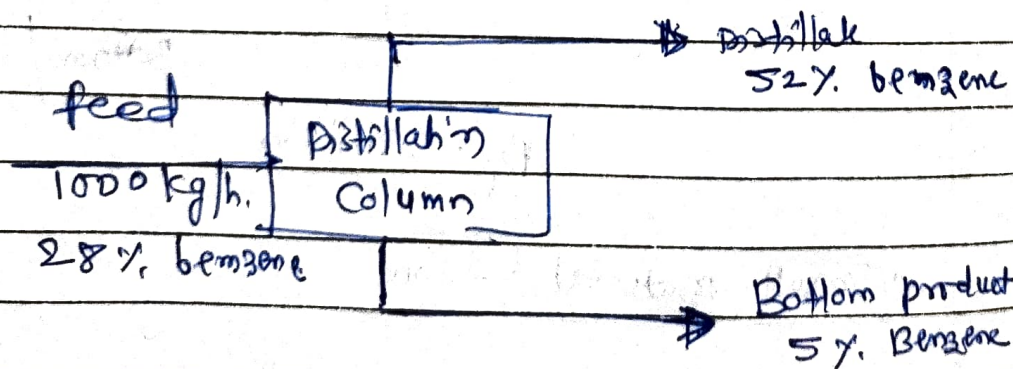
Material balance for Component

$$A \text{ in feed} = A \text{ in distillate} + A \text{ in bottom}$$

$$X_f \cdot F = X_D \cdot D + X_W \cdot K$$

$X_f$ ,  $X_D$  and  $X_W$  are the weight fractions of A in feed, distillate and bottoms.

P. A feed Continuous fractionating column analysed by weight 28 percent benzene and 72 percent toluene. the analysis of the distillate shows 52 weight percent benzene and 5 weight % benzene was found in the bottom product. calculate the amount of distillate and bottom product per 1000 kg of feed per hour. also calculate the percent recovery of benzene.



Overall material balance = Feed = Distillate + Bottom product  
 $1000 = x + y$

$$\therefore x + y = 1000$$

material balance of Benzene

$$x + y = 1000 \quad \text{--- (1)}$$

material balance of benzene

Benzene in feed = Benzene in distillate + Benzene in Bottom product

$$0.28 \times 1000 = 0.52x + 0.05y$$

$$280 = 0.52x + 0.05y \quad \text{--- (2)}$$

$$0.05y = 280 - 0.52x \quad \text{---}$$

$$y = \frac{280 - 0.52x}{0.05}$$

$$y = \frac{280}{0.05} - \frac{0.52x}{0.05}$$

$$y = 5600 - 10.4x \quad \text{--- (3)}$$

put the value of y from eqn (3) in eqn (1)

$$x + y = 1000$$

$$x + 5600 - 10.4x = 1000$$

$$\cancel{x} - 10.4x = 1000 - 5600$$

$$9.4x = 4600$$

$$x = \frac{4600}{9.4} = 489.4 \text{ kg/hr}$$

$$y = 1000 - 489.4 = 510.6 \text{ kg/hr}$$

(X) Distillate flow rate = 489.4

(Y) Bottom product flow rate = 510.6 kg/hr



$$\text{Benzene in feed} = 0.28 \times 1000 = 280 \text{ kg/hr}$$

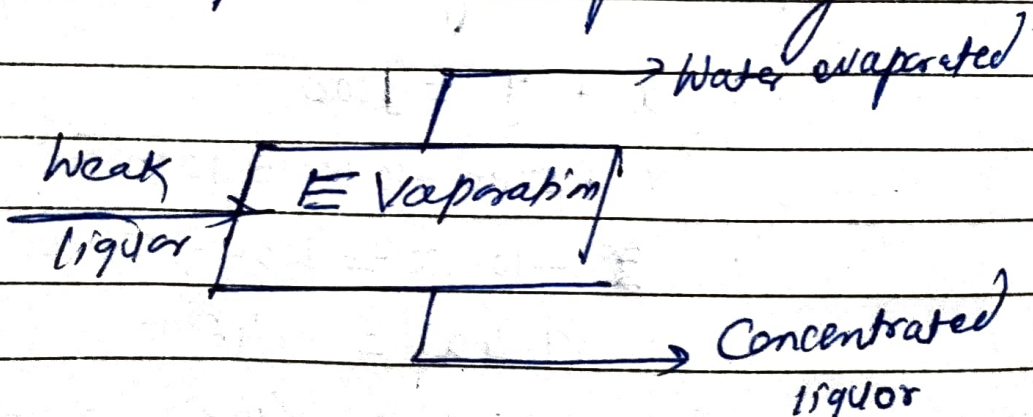
$$\text{Benzene in distillate} = 0.52 \times 489.4 = 254.49 \text{ kg/hr}$$

$$\begin{aligned} \checkmark \text{ Recovery of Benzene} &= \frac{\text{Benzene in Distillate}}{\text{Benzene in Feed}} \times 100 \\ &= \frac{254.49}{280} \times 100 \\ &= \underline{\underline{90.89}} \end{aligned}$$

### Evaporation:

This operation used in a Chemical industry for the concentration of weak liquor to produce a thick liquor by evaporating a portion of the solvent (generally water) by means of condensing steam.

It may be carried out in a single or multiple effect evaporation system.



### Overall Material balance

$$\text{Weak liquor} = \text{Water evaporated} + \text{Crystallized product} + \text{Thick liquor}$$

If Crystallized product is nil

$$\text{Weak liquor} = \text{Water evaporated} + \text{Thick liquor}$$

Material balance of solid (solute):

$$\text{Solids (solute) in Weak liquor} = \text{Solids (solute) in thick liquor}$$

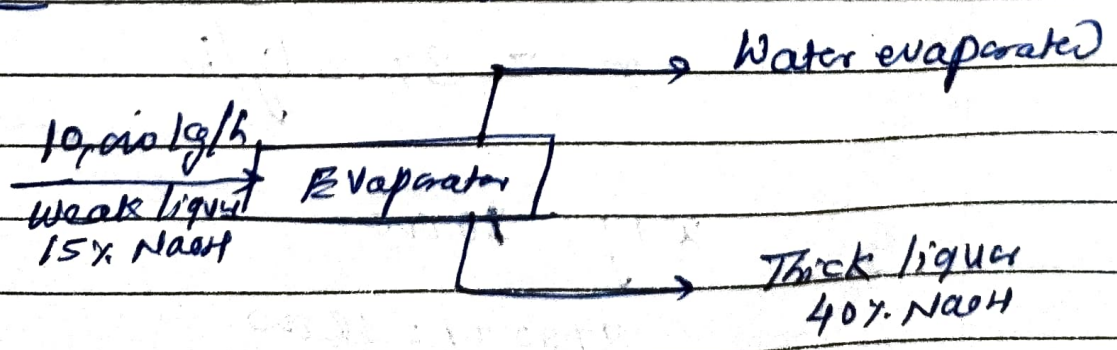
Material balance of Water

$$\text{Water in Weak liquor} = \text{Water evaporated} + \text{Water in thick liquor}$$

1. A single effect evaporator is fed with 10,000 kg/hr of weak liquor containing 15% caustic by weight and is concentrated to get thick liquor containing 40% by weight caustic NaOH

- a) Calculate @ kg/h of water evaporated
- b) kg/h thick liquor obtained

Soln Basis 10,000 kg/h of weak liquor





let  $x$  be the kg/h thick liquor obtained  
and  $y$  be the kg/h water evaporated

Overall material balance

$\Sigma$  kg/h Input =  $\Sigma$  kg per hour output

Weak liquor = Thick liquor + kg/h evaporated

$$10000 = x + y$$

Material balance of NaOH

NaOH in the input = NaOH in the output

NaOH in weak liquor = NaOH in thick liquor

~~0.15x~~

$$\frac{15}{100} \times 10000 = 0.40x$$

$$0.15 \times 10,000 = 0.40x$$

$$x = \frac{0.15 \times 10,000}{0.40}$$

$$0.40$$

$$x = 3750 \text{ kg/hr}$$

$$x + y = 10,000$$

$$3750 + y = 10,000$$

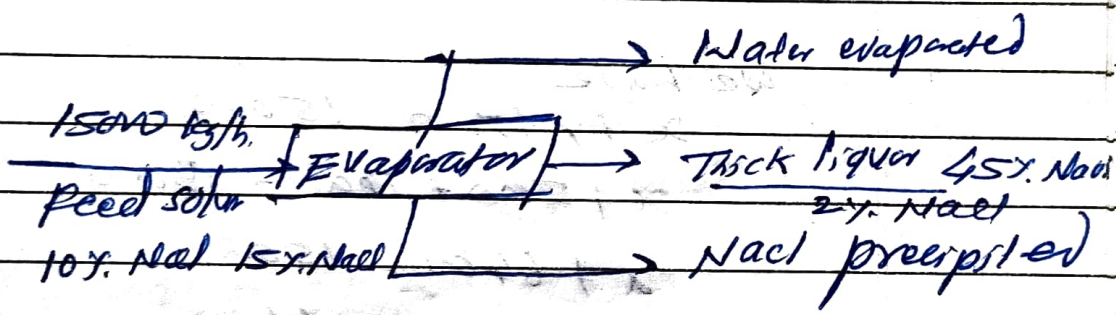
$$y = 10,000 - 3750$$

$$\text{Water evaporated} = 6250 \text{ kg/hr}$$

2) An water evaporated is fed with 15000 l/h of solution containing 10% NaCl and 15% NaOH and rest water. In the operation, water is evaporated and NaCl is precipitated as crystals. The Thick liquor leaving the evaporator contain 45% NaOH 2% NaCl and rest water.

- Calculate
- (a) kg/h water evaporated
  - (b) kg/h. salt precipitated
  - (c) kg/h Thick liquor

soln



Overall Material balance

$$\text{Input} = \text{out put}$$

$$\text{feed} = \text{Thick liquor} + \text{NaCl precip} + \text{Water evap}$$

$$\text{feed} = \text{Water eva} + \text{Thick liq} + \text{NaCl precip}$$

$$15000 = x + y + z$$

Material balance for NaOH

$$\text{NaOH in feed solution} = \text{NaOH in thick soln}$$

$$0.15 \times 15000 = 0.45 \times y$$

$$\frac{0.15 \times 15000}{0.45} = y$$

$$y = 5000 \text{ kg/hr}$$



Material balance for NaCl

NaCl in feed solution = NaCl in thick liquor  
+ NaCl precipitated  
as a crystal

$$0.10 \times 15000 = 0.02 \times 5000 + Z$$

$$1500 = 100 + Z$$

$$1500 - 100 = Z$$

$$1400 \text{ kg/h} = Z$$

We have

$$x + y + z = 15000$$

$$x + 5000 + 1400 = 15000$$

$$x + 6400 = 15000$$

$$x = 15000 - 6400$$

$$x = 8600 \text{ kg/hr}$$

Water evaporated (x) = 8600 kg/hr

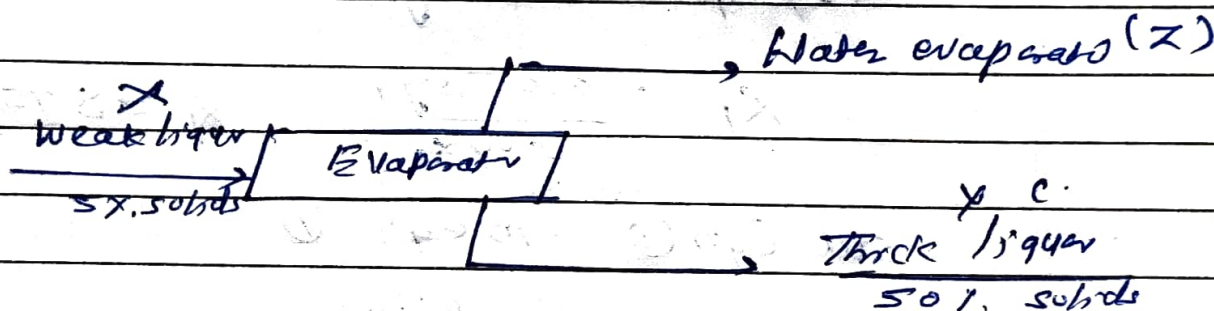
Thick liquor obtained = 5000 kg/hr

NaCl precipitated = 1400 kg/hr

3. An evaporator system concentrating liquor 5% solids. Solids handles 100 kg of solid per hour. If the same system is to concentrate a weak liquor from 4% to 35%. Find the capacity of system in term of solid that can be handled per hour assuming water evaporation capacity to be same in both the cases.

Soln Case I

Basis 100 kg/h. of solid handling capacity of the evaporator.



Let  $x$  be the kg/h of weak liquor then we have

$$0.05x = 100$$

$$x = \frac{100}{0.05} = 2000 \text{ kg/h}$$

Let  $y$  be the kg of thick liquor then we have

$$0.5y = 100$$

$$y = \frac{100}{0.5} = 200 \text{ kg/h}$$

Overall M.B :

kg of weak liquor = kg/h of thick liquor + kg/h. water evaporated

$$2000 = 200 + \text{water evaporated}$$

$$\text{Water evaporated} = 2000 - 200$$

$$Z = 1800 \text{ kg/h}$$



## Case II

1000 kg/h water evaporated

let  $x_1$  &  $y_1$  be the weak liquor and thick liquor leaving evaporator

Overall M.B

$$x_1 = y_1 + 1800$$

$$x_1 = y_1 + 1800 \quad \text{--- (1)}$$

Material balance for solid

$$\text{Weak liquor} \\ 0.04 x_1 = 0.035 y_1$$

$$x_1 = \frac{0.035 y_1}{0.04} \quad \rightarrow \quad x_1 = 8.75 y_1 \quad \text{--- (2)}$$

Sub. eqn (2) in eqn (1)

$$8.75 y_1 = y_1 + 1800$$

$$8.75 y_1 - y_1 = 1800$$

$$7.75 y_1 = 1800$$

$$y_1 = \frac{1800}{7.75} = 232.26$$

$$x_1 = y_1 + 1800$$

$$x_1 = 232.26 + 1800$$

$$= 2032.26 \text{ kg/hr}$$

Solid in weak liquor

$$= 0.04 \times 2032.26$$

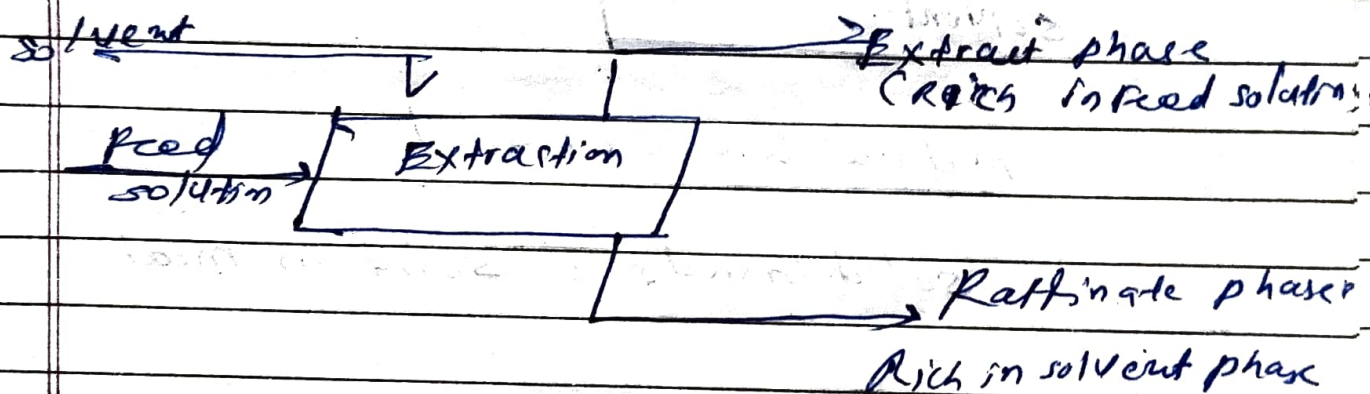
$$= 81.3 \text{ kg/hr}$$

Handling Capacity in case II = 81.3 kg/hr

Extraction

This operation used in the chemical industry for the separation of the component of liquid mixture with help of suitable liquid solvent where in the solute from the feed solution is a transferred in the solvent yielding the raffinate phase (rich in feed solvent) and extract phase (rich in solvent used). It does not give a pure product and need further processing

Mixer settler, packed column, etc

Overall M.B

$$\text{Feed solution} + \text{solvent} = \text{Extract phase} + \text{Raffinate phase}$$

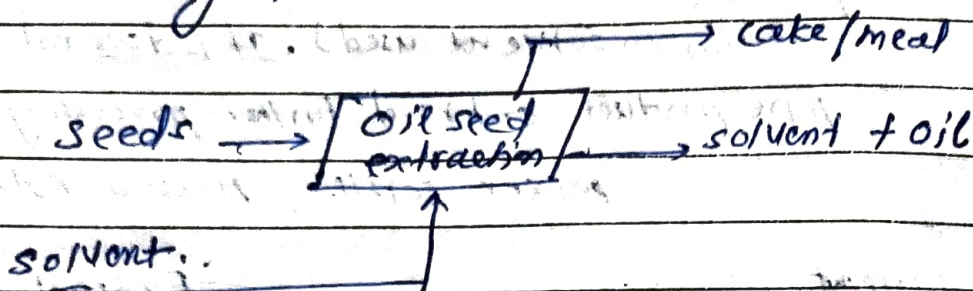
M.B. for solute

$$A \text{ in feed solution} = A \text{ in extract phase} + A \text{ in raffinate phase}$$



Extraction operation is also carried out for removal of a soluble constituent of solids with help of suitable liquid solvent (Here it is a solid extraction)

For example oil seed extraction or leaching of valuable metals from minerals ores.



material balance of solid

$$\text{solid in seeds} = \text{solid in meal}$$

material balance of oil

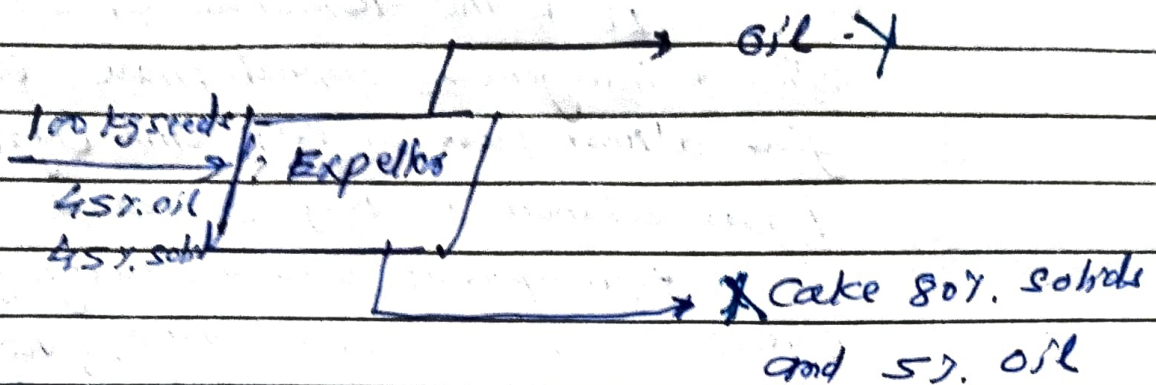
$$\text{oil in seeds} = \text{oil in meal}$$

+ oil in solvents

(extracted oil)

- p. The ground nut seeds containing 45% oil and 45% solids are fed to expeller the cake coming out of expeller is found to contain 80% solids and 5% oil. find the % recovery of oil.

soln 100 kg of ground nut seeds



Material balance of solids

solid in ~~cake~~ seeds = solid in cake

$$0.45 \times 100 = 0.8 \times X$$

$$X = \frac{0.45 \times 100}{0.8} = 56.25 \text{ kg}$$

cake solid = 56.25 kg

Material balance of oil

oil in seeds = oil in cake + oil recovered

$$0.45 \times 100 = 0.05 \times 56.25 + \text{oil recovered}$$

$$45 = 2.81 + \text{oil recovered}$$

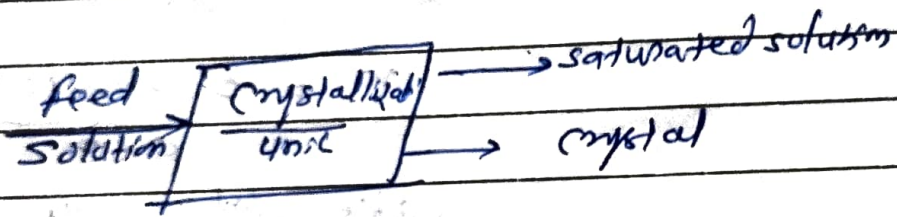
$$\begin{aligned} \text{oil recovered} &= 45 - 2.81 \\ &= 42.19 \text{ kg} \end{aligned}$$

$$\begin{aligned} \text{y. recovery of oil} &= \frac{\text{kg of oil recovered}}{\text{kg of oil seeds}} \times 100 \\ &= \frac{42.19}{45} \times 100 = 93.75 \text{ Ans.} \end{aligned}$$



Crystallization :-

It is the formation of solid particles within a homogeneous liquid phase. Crystallization gives almost pure product and crystallization from solution is very important. Industrially equipment used for carrying out crystallization are stirred tank, vacuum crystallizer. Crystallization of the dissolved solid from a solution is based on the difference in solubilities at different temperature. It is usually consist of concentration of solution and cooling of solution until it become supersaturation.



Overall material balance :-

$$\text{feed solution} = \text{saturated solu} + \text{crystal}$$

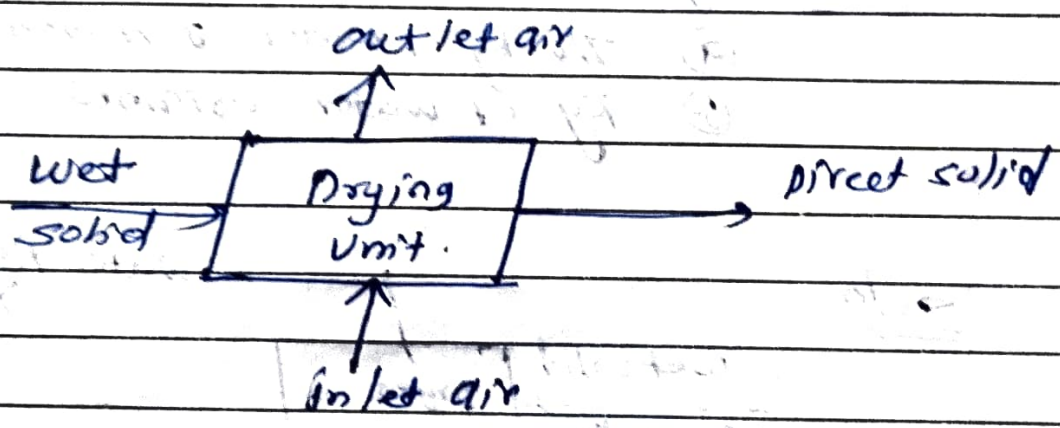
Material balance of solute (crystals)

$$\text{Crystal in feed solution} = \text{Crystal obtained} + \text{Crystal in saturated solution.}$$

## Drying -

This operation is carried out in the chemical industry for the removal of a residual mixture (water) or volatile liquid associated with wet solids with the help of hot air or inert gas (N<sub>2</sub>) (drying medium). When the hot air is circulated over wet solids, the moisture from the solids evaporates and get added in the air is circulated over wet solid.

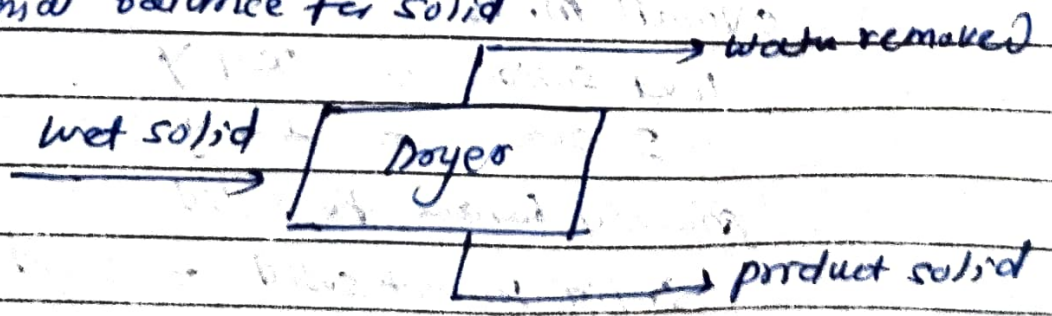
In industry there are mainly used Tray dryer, spray dryer etc.



### Material balance of Moisture

$$\text{Moisture removed from solid} = \text{moisture added in air}$$

### Material balance for solid



$$\text{Solid in wet solid} = \text{solid in product}$$



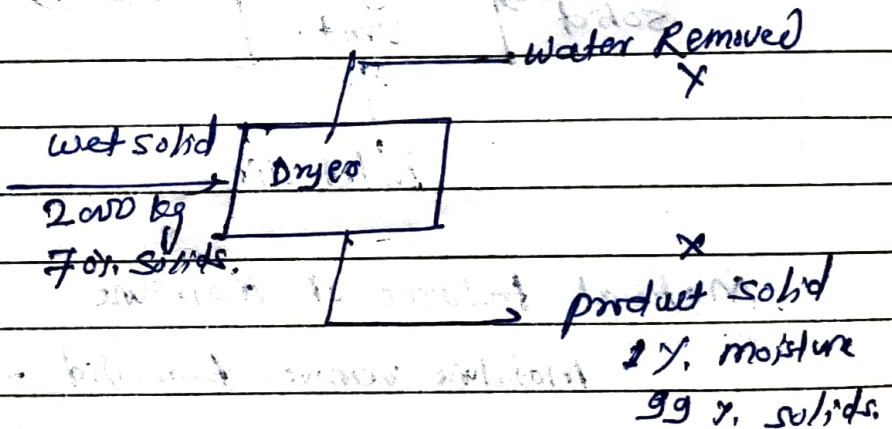
Overall material balance

Wet solid = Water ~~removed~~ removed + product solids.

P → 2000 kg of wet solids containing 70% solids by weight are fed to a tray dryer where it is dried by hot air. The product finally obtained is found to contain 1% moisture by weight. Calculate.

- (a) The kg of water removed from wet solid
- (b) kg of water obtained

Soln



Overall m. B

Wet solid =  $x + y$

2000 =  $x + y$

Material balance for solid

Solid in wet solid = solid in product

$0.7 \times 2000 = 0.99 \times x$

$x = \frac{0.7 \times 2000}{0.99} = 1414.14 \text{ kg}$

Overall material balance

$$2000 = x + y$$

$$2000 = 1414.14 + y$$

$$y = 2000 - 1414.14$$

$$y = 585.86 \text{ Kg}$$

$$\text{Water removed (y)} = 585.86 \text{ kg}$$

$$\text{kg of product solid} = 1414.14 \text{ kg}$$



# Material balance with chemical reaction

completion of the reaction or vice-versa.

## Definitions of Terms Involved :

**Stoichiometry :** It is the theory of the proportions in which chemical species combine with one another.

**Stoichiometric Equation :** The stoichiometric equation of a chemical reaction is the statement indicating relative moles of reactants and products that take part in the reaction.

For example, the stoichiometric equation



indicates that one molecule (mol or kmol) of CO reacts with two molecules (mol or kmol) of hydrogen to produce one molecule (mol or kmol) of methanol.

**Stoichiometric Coefficient :** It is the number that precede the formula of each component involved in a chemical reaction.

Thus, for example, in the above cited reaction, the stoichiometric coefficient of CO is one, the stoichiometric coefficient of H<sub>2</sub> is two and that of methanol is one. The stoichiometric requirements of components are given as :

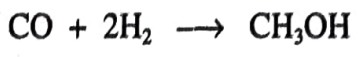
$$1 \text{ kmol CO} \quad \blacksquare \quad 1 \text{ kmol CH}_3\text{OH} \\ \quad \quad \quad \blacksquare \quad 2 \text{ kmol H}_2$$

**Stoichiometric Ratio :** It is the ratio of stoichiometric coefficients of two molecular species/components in the balanced reaction equation.

e.g., stoichiometric ratio of H<sub>2</sub> to CO is 2/1 = 2.

**Stoichiometric Proportion :** Two reactants, A and B, are said to be present in the stoichiometric proportion if the ratio of moles of A present to the moles of B present is equal to the stoichiometric ratio obtained from the balanced reaction equation.

Consider the following chemical reaction :



For the reactants in the above reaction to be present in the stoichiometric proportion, there must be 2 moles of H<sub>2</sub> for every mole of CO (so that  $n_{H_2} / n_{CO} = 2/1 = 2$ ) present in the feed to any reactor.

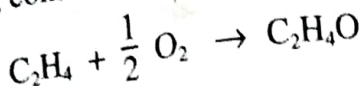
When the reactants are fed to a reactor in the stoichiometric proportion and the reaction goes to completion, all of the reactants are consumed. In case of the above cited reaction, for example, if 200 mol of H<sub>2</sub> and 100 mol of CO are initially present, the H<sub>2</sub> and CO would disappear at the same instant. It follows that if we start with 100 mol of CO and less than 200 mol of H<sub>2</sub> (i.e., if H<sub>2</sub> is present in less than its stoichiometric proportion) H<sub>2</sub> disappears before the CO<sub>2</sub>, on the other hand, if there are more than 200 mol of H<sub>2</sub> initially present the CO disappears first.

**Limiting Reactant / Component :** It is defined as the reactant that would disappear first if a reaction goes to completion. It is the one which decides the extent to which a reaction can proceed. The limiting reactant is always present in less than its stoichiometric proportion relative to the other reacting components. It is the reactant which is present in the smallest stoichiometric amount, i.e., the reactant which is not present in excess of that required to combine with any of the other reactants.

It is the reactant which is present in such proportions that its consumption/disappearance by the reaction will limit the extent to which the reaction can proceed (i.e., the extent of reaction).

**Excess reactant :** It is defined as the reactant which is in excess of the theoretical or stoichiometric requirement as determined by the desired reaction. The excess component / reactant always found in the product stream though the reaction proceeds to completion.

For example, consider the following reaction :



4.2

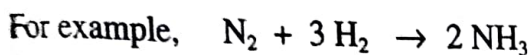
Stoichiometry

Material Balances with Chemical Reactions  
Material Balances with Chemical Reactions

In industrial practice of producing ethylene oxide by oxidation of ethylene, oxygen/air to the reactor is always in excess of that theoretically required. Thus, ethylene is the limiting reactant and oxygen/air is the excess reactant.

**It is a reactant present in excess of the limiting reactant.**

When all reactants are present in the stoichiometric proportion, then none of the reactants involved is limiting.



$N_2$  and  $H_2$  are always fed to reactor in their stoichiometric proportion i.e. 1 mole  $N_2$  to 3 moles  $H_2$  so no reactant is limiting.

**Percent Excess :** The excess reactant involved in the reaction is generally specified in terms of percent excess. It is the amount in excess of the stoichiometric (theoretical) requirement expressed as a percentage of the stoichiometric/theoretical requirement.

Consider the reaction :  $A + B \rightarrow C$

wherein B is the excess reactant. Then

$$\therefore \left[ \text{Percent excess of B} \right] = \left[ \frac{\text{moles of B supplied or fed} - \text{moles of B theoretically required}}{\text{moles of B theoretically required}} \right] \times 100 \quad \dots (4.1)$$

Moles of B theoretically required are the moles of B that would correspond to stoichiometric proportion and are calculated based on limiting reactant charged.

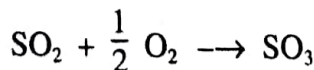
Equation (4.1) is also valid on weight basis.

The above equation can be rearranged to calculate the quantity of the excess reactant actually supplied.

$$\left[ \text{moles of B actually fed or supplied} \right] = \left[ \text{Stoichiometric requirement or theoretical requirement of B} \right] \left( 1 + \frac{\% \text{ excess B}}{100} \right) \quad \dots (4.2)$$

The quantity of excess reactant must be found based on the quantity of limiting reactant fed to the reactor.

Consider, for example, the reaction



and suppose that 100 mol  $SO_2/h$  and 75 mol  $O_2/h$  are fed to a reactor.  $SO_2$  is clearly the limiting reactant, and to be in stoichiometric proportion, moles of  $O_2$  would have to be 50 mol/h. The percent excess of  $O_2$  is therefore

$$\% \text{ excess } O_2 = \left( \frac{75 - 50}{50} \right) \times 100 = 50$$

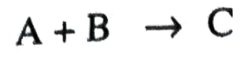


Chemistry

**Conversion** : The conversion is always based on the limiting reactant and it gives idea regarding the degree of completion of a reaction. The unreacted quantities of raw materials are easily obtained knowing the charged quantities with the help of conversion. This, in turn, gives us idea regarding whether recycling is to be done or not for the process to be economically feasible.

**Conversion is the fraction of some key reactant that is converted into products.**

Consider the chemical reaction :



where A is the limiting reactant and B is the excess reactant. Then,

The conversion or fractional conversion of A is the ratio of the amount of A reacted to amount of A charged or fed to the reactor. The percentage conversion of A is the amount reacted expressed as a percentage of the amount of A charged or fed to the reactor.

The amount of A can be expressed on mole or weight basis. If amount of A is expressed in moles then

$$\% \text{ conversion of 'A'} = \frac{\text{moles (or mass) of A reacted}}{\text{moles (or mass) of 'A' charged or fed}} \times 100$$

In case of recycle operations, the term namely per pass conversion is commonly used. Per pass conversion is defined as the quantity of limiting reactant reacted/consumed expressed as the percentage of the limiting reactant in the mixed feed.

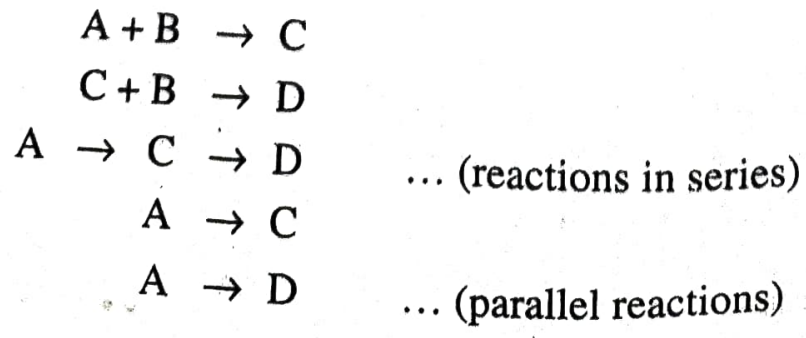
If 100 mol of reactant A are fed and 75 of them react, the fractional conversion is 0.75 (percentage conversion is 75%) and the fraction unreacted is 0.25. If 50 mol of reactant A are fed and the percentage conversion is 80%, then  $(0.80)(50) = 40$  mol of reactant A are reacted and  $(0.20)(50) = 10$  mol of A remain unreacted.

Degree of completion of a reaction is expressed as the percentage of the limiting reactant converted into the product.

**Yield and Selectivity** : In most of the chemical processes, though the objective is to produce a desired product, the raw materials may also undergo a series of parallel reactions (side reactions) resulting into production of undesired materials which has reverse effect on economics of the process. In such cases (in industrial practice), the steps are taken to suppress the side reactions by use of selective catalyst, addition of inhibitors in the feed, etc.

The terms yield and selectivity are used in case of multiple reactions to give the information regarding the degree to which the desired reaction predominates over the side reaction (or reactions) involved.

Consider the reactions :



C is the desired product, D is the undesired product and A is the limiting reactant. The yield of 'C' is given as :

$$\text{Yield of C} = \frac{\text{moles of A reacted to produce C}}{\text{moles of A totally reacted}} \times 100$$

Yield of the desired product is the quantity of the limiting reactant reacted to produce it expressed as the percentage of the quantity of the limiting reactant reacted totally (i.e. by all reactions).

Selectivity is the ratio of the moles of the desired product produced to the moles of the undesired product (by-product) produced.

Consider the parallel reactions :

$A \rightarrow C$  and  $A \rightarrow D$ , where C is the desired product and D is the undesired product, in this case, selectivity is given as :

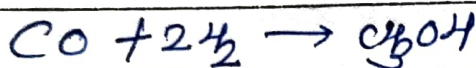
$$\text{Selectivity of C relative to D} = \frac{\text{moles of C (desired product) formed}}{\text{moles of D (undesired product) formed}}$$

Selectivity is also defined as the ratio of the amount of the limiting reactant reacted to the desired product to the amount of it reacted to produce the undesired product. If yield is 100% then the selectivity is 1.



Material balances with chemical reaction

- 1) The Carbon monoxide is reacted with hydrogen to produce methanol. calculate from the reaction
- Stoichiometric ratio  $H_2$  to  $CO$
  - Kmol of  $CH_3OH$  produced per kmol  $CO$  reacted
  - Weight ratio of  $CO$  to  $H_2$  if both are fed to reactor in a stoichiometric proportion
  - The quantity of  $CO$  required to produce 100 kg of  $CH_3OH$ .

Soln

Stoichiometric Co. efficient

$$CO = a = 1$$

$$H_2 = b = 2$$

- a) Stoichiometric ratio
- $H_2$
- to
- $CO$

$$\frac{b}{a} = \frac{2}{1} = 2 \quad \underline{\text{Ans}}$$

- b) Co. reacted to produce
- $CH_3OH$

$$= \frac{1}{1} = 1$$

- c)
- Weight ratio  $CO$  to  $H_2$

CO used in kg

$$\text{Moles} = \frac{\text{Weight of substance}}{\text{Molecular weight}}$$

$$1 = \frac{\text{Weight of sub. (CO)}}{28}$$

$$28 \times 1 = \text{Weight of sub.}$$

$$28 \text{ kg} = \text{CO used. to Fed}$$

$H_2$  fed to reactor in kg

$$\text{moles} = \frac{\text{weight of } H_2}{\text{mol. weight}}$$

$$2 = \frac{\text{weight of } H_2}{2}$$

$$4 = \text{weight of } H_2$$

Weight ratio

$$= \frac{28}{4} = 7$$

d) The quantity CO required to produce 1000 kg of  $CH_3OH$

28 kg requires to produce 32 kg  $CH_3OH$

for 1000 kg  $CH_3OH$  produce?

$$= \frac{32}{28} \times \frac{1000}{1} = 875 \text{ kg } \underline{\underline{\text{ans}}}$$



2) Ammonia is produced by following reaction



Calculate (a) molar flow rate of hydrogen corresponding to nitrogen feed rate of 25 kmol/h if they are fed in stoichiometric proportion

(b) The kg of ammonia produced per hour if conversion is 25% and nitrogen feed rate is 25 kmol/h.

soln



Stoichiometric proportion of  $\text{N}_2$  to  $\text{H}_2$  from the reaction is 1:3.

• molar flow rate of Hydrogen in stoichiometric proportion

$$= \frac{3}{1} \times 25 = 75 \text{ kmol/h}$$

• moles of  $\text{N}_2$  reacted = kmole of  $\text{N}_2$  fed per hour

~~% Conversion of  $\text{NH}_3$~~

X % Conversion of  $\text{N}_2$

$$= 25 \times \frac{25}{100}$$

$$= 6.25 \text{ kmol/h}$$

• 1 kmol of  $\text{N}_2$  produces 2 kmol of  $\text{NH}_3$

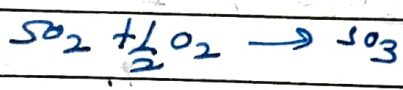
$$\text{NH}_3 \text{ produced} = 2 \times 6.25$$

$$\text{with 1 kmol } \text{N}_2 \text{ reacted} = 12.50 \text{ kmol/h}$$

$$\begin{aligned}
 \text{Amount of } \text{NH}_3 \text{ produced} &= \text{NH}_3 \text{ produced} \times \text{mol. weight} \\
 &= 12.50 \times 17 \\
 &= 212.5 \text{ kg/hr}
 \end{aligned}$$

③ In a production of sulphur trioxide, 100 kmol of  $\text{SO}_2$  and 200 kmol of  $\text{O}_2$  are fed to a reactor. The product stream is found to contain 80 kmol  $\text{SO}_3$ . Find the % conversion of  $\text{SO}_2$ .

Reaction



1 kmol  $\text{SO}_3$  produce to require 1 kmol  $\text{SO}_2$

$$80 \text{ kmol of } \text{SO}_3 \rightarrow$$

$$\text{SO}_2 \text{ reacted} = \frac{80}{1} \times 1 = 80 \text{ kmol}$$

$$\% \text{ Conversion of } \text{SO}_2 = \frac{\text{kmol of } \text{SO}_2 \text{ reacted}}{\text{kmol of } \text{SO}_2 \text{ charged}} \times 100$$

$$= \frac{80}{100} \times 100 = 80$$

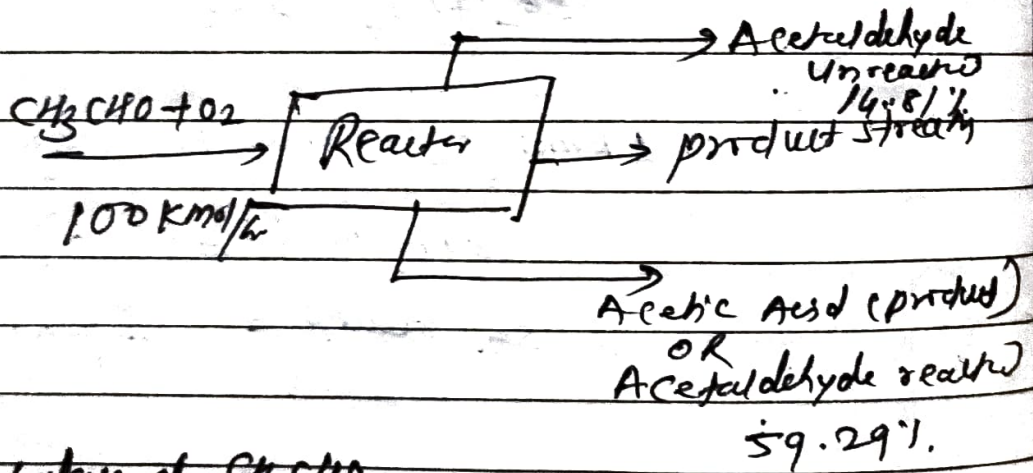
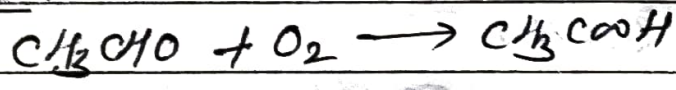


4)

In Manufacture of acetic acid by oxidation of acetaldehyde 100 kmol of acetaldehyde is fed to reactor per hour. The product leaving the reactor contain 14.81% acetaldehyde, 59.29% acetic acid, and rest oxygen (on mole basis) find the % conversion of acetaldehyde.

Sol<sup>n</sup> 100 kmol/h acetaldehyde charged to reactor

Reaction



M. balance of  $CH_3CHO$

$$CH_3CHO \text{ fed To Reactor} = \text{acetaldehyde reacted} + CH_3CHO \text{ unreacted}$$

$$100 = 0.5929x + 0.1481x$$

$$100 = 0.741x$$

$$\frac{100}{0.741} = x$$

$$x = 134.95 = 135$$

∴ Acetaldehyde reacted =  $0.5929(135)$

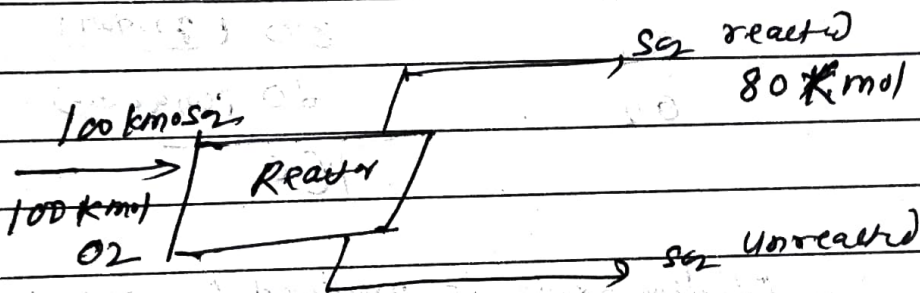
=  $\frac{80.04}{kmol/hr}$

% Conversion of acetaldehyde

$$= \frac{\text{Acetaldehyde reacted}}{\text{acetaldehyde charged}} \times 100$$

$$= \frac{80}{100} \times 100 = \underline{\underline{80}}$$

⑤ A production of sulphur tri oxide, 100 kmol of  $\text{SO}_2$  and 100 kmol of  $\text{O}_2$  are fed to reactor. If % Conversion of  $\text{SO}_2$  is 80. calculate the composition of the product stream on mole basis.



Material balance of  $\text{SO}_2$

$$\text{SO}_2 \text{ charged to reactor} = \text{SO}_2 \text{ reacted} + \text{SO}_2 \text{ unreacted}$$

$$100 = 80 + \text{SO}_2 \text{ unreacted}$$

$$\text{SO}_2 \text{ unreacted} = 100 - 80$$

$$= 20 \text{ kmol}$$

$$1 \text{ m kmol of SO}_2 \equiv 1 \text{ kmol SO}_3$$

$$80 \text{ kmol of SO}_2 \text{ reacted} = 80 \text{ kmol of SO}_3 \text{ produced}$$

Similarly

From reaction  $2 \text{ kmol SO}_2 \text{ reacted} = \frac{1}{2} \times 2 \text{ kmol of O}_2 \text{ reacted}$

$80 \text{ kmol SO}_2 \text{ reacted} \Rightarrow \frac{1}{2} \text{ kmol of O}_2 \text{ reacted}$

means half of the  $\text{SO}_2$

$$\frac{1}{2} \times 80 = \underline{\underline{40 \text{ kmol}}}$$



Material balance of  $O_2$ 

$$O_2 \text{ charged} = O_2 \text{ reacted} + O_2 \text{ unreacted}$$

$$100 = 40 + O_2 \text{ unreacted}$$

 $O_2$  char:

$$100 - 40 = O_2 \text{ unreacted}$$

$$60 = O_2 \text{ unreacted}$$

$$O_2 \text{ reacted} = 60 \text{ kmol}$$

Composition of product stream

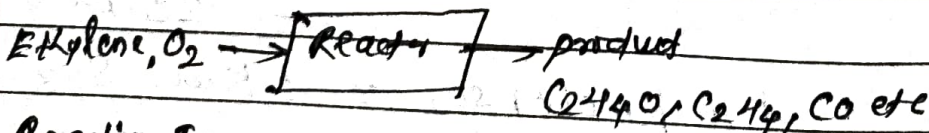
Component	Quantity kmol	mol %
$SO_2$	20 (unreacted)	$20/160 = 12.5$ X100
$SO_2$	80 (product)	$80/160 = 50$ X100
$O_2$	60 (unreacted)	$60/160 \times 100 = 37.5$
	<u>160</u>	<u>100</u>

p.6. Ethylene oxide is produced by oxidation of ethylene. 100 kmol of ethylene are fed to reactor and product is found to contain 80 kmol ethylene oxide and 10 kmol of  $CO_2$ . calculate

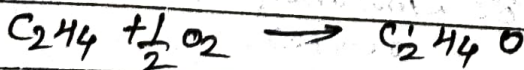
a) the % conversion of ethylene

b) % yield of ethylene oxide

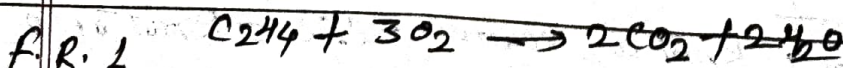
Soln 100 kmol of ethylene fed to reactor



Reaction I



Reaction II



80 kmol of ethylene oxide produce means 80 kmol of  $C_2H_4$  reacted

From Reaction II

1 kmole of  $C_2H_4$  reacted and 2 kmole of  $CO_2$  produced

$\therefore$  10 kmole of  $CO_2$  produced mean 5 kmole of  $C_2H_4$  reacted

$\therefore$   $C_2H_4$  totally reacted from Reaction I & Reaction II

$$C_2H_4 \text{ totally reacted} = C_2H_4 \text{ reacted Reaction I} + C_2H_4 \text{ reacted Reaction II}$$

$$= 80 + 5$$

$$= 85$$

$$\% \text{ conversion of } C_2H_4 = \frac{C_2H_4 \text{ reacted}}{C_2H_4 \text{ Fed}} \times 100$$

$$= \frac{85}{100} \times 100 = 85 \%$$

$$\therefore \text{ yield of } C_2H_4O = \left( \frac{\text{kmole of } C_2H_4 \text{ reacted to produce } C_2H_4O}{\text{kmol } C_2H_4 \text{ totally reacted}} \right) \times 100$$

$$= \frac{80}{85} \times 100$$

$$= \underline{\underline{94.12 \%}}$$